

Combining forecasts for electricity prices

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Abstract: This paper considers how well the approach of combining forecasts extends to the context of electricity prices. With the increasing popularity of regime switching and time-varying parameter models for predicting power prices, the multi model and evolutionary considerations that usually support the combining of simpler time series methods may be less applicable when the individual models incorporate these features. We address this question with a backtesting analysis on British day-ahead prices. Furthermore, given the volatility of power prices and concerns about accurate forecasting under extreme price excursions, we evaluate the results using various error metrics including expected shortfall. The comparisons are furthermore carefully simulated to consider model selection uncertainty in order to realistically test the value of combining as an ex ante policy. Overall, our results support combining for both accurate operational planning and risk management.

Keywords: Forecasts combination, Prediction accuracy, ARMAX, Timevarying parameter regression, Markov regime switching, Electricity price forecasting.



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1 Introduction

The value of combining forecasts to achieve accurate predictions is now well-established, with extensive research and convincing applications extending back over 50 years to the work of Granger and his colleagues at Nottingham, Reid (1968, 1969), Bates and Granger (1969) and Newbold and Granger (1974). Despite this body of knowledge, it is quite surprising to observe the absence of substantial research on combining in the context of forecasting electricity prices. Since the established research on electricity markets suggests a wide variety of candidate methods for price forecasting (see, for example, Bunn, 2004; Weron, 2006; Serati et al., 2008) but without any predominant method having emerged, and with model selection varying over time (Chen and Bunn, 2010), the benefits of combining would appear to be very propitious. However, given that the approaches of regime switching, which has an implicit multimodel structure, and time-varying parameter models, which capture model evolutions, have become widely advocated to represent power price dynamics, it is possible that these specifications, to the extent that such models are included

in the candidate set of predictive models, may encapsulate and thereby preclude any benefits of simple combinations. We therefore investigate this open question through a detailed study of the effectiveness of combining a set of four carefully specified models, ARMAX, linear regression, Markov regime switching and time-varying regressions, as applied to day-ahead forecasting of British half-hourly power prices.

Methods of increasing sophistication followed the simple adaptive time series approach of Bates and Granger (1969), including Bayesian (Bunn, 1975, 1977), and econometric (Granger and Ramanathan, 1984), as well as extensions to large data sets (Stock and Watson, 2001, 2004), but, for robust forecasting, it has appeared hard to improve upon simple averaging (Makridakis and Winkler, 1983; Clemen, 1989; Stock and Watson, 2001, 2004; Smith and Wallis, 2009). We therefore do not address the question of developing combining methods to improve on simple averaging. We do, however, consider the less commonly addressed question of effectiveness at extreme outcomes. Because the spiky nature of power prices has been one of the motivations for regime switching methods, it seems appropriate that, when combinations include regime switching methods, the accuracy of the combination should be assessed not only in terms of the expected value, but also on a quantile defined value-at-risk ("expected shortfall") measure. In this research, we are therefore motivated to analyse the results using a number of error metrics including expected shortfall.

Many research papers have suggested that combining will perform better than individual methods (Clemen, 1989; Clements and Hendry, 1998; de Menezes et al., 2000; Riedel and Gabrys, 2005; Altavilla and De Grauwe, 2006; Timmermann, 2006; Chen and Yang, 2007; Clark and McCracken, 2009), including some applications to electricity demand forecasting (see Taylor and Majithia, 2000; Taylor, 2010). In the context of electricity prices, García-Martos et al. (2007) similarly advocate combining, but within a single model class (ARIMA), to deal with specification uncertainty. Despite the volume of comparisons published, it is an open question how many of the results in favour of combining are actually statistically significant. Moreover, in addition to this question, we are careful in our comparisons to consider, not simply the usual ex post evaluation of whether combining would have outperformed the best individual methods, but the more realistic setting of whether combining would have performed better than the individual method which would have be chosen ex ante. Given that part of the motivation for combining is that individual model performances are unstable, it is important to evaluate the procedures with a backtesting experiment that incorporates this unstable model selection aspect in a simulated ex ante way.

The paper is organized as follows. In Section 2 we present the price data from the UK Power Exchange (UKPX). The individual models and price drivers included therein as regressors are described in Section 3. Section 4 introduces the combination methodology and explains how the forecasts are evaluated. Section 5 contains the experimental design and the results of our work. Section 6 concludes.

Section 2 The data 3

2 The data

This work considers price data from the UK Power Exchange (UKPX) for the period April 1st, 2005 - September 30th, 2006: the choice of the starting date is important because it refers to the market that had just been extended to include Scotland. The British power market is considered to be a fully competitive market and one of the most mature in the world (see Karakatsani and Bunn, 2008b for a detailed exposition).

The price series have half-hourly frequency, so that each day consists of 48 observations, one for each load period. We denote by P_{it} the spot price at day t and load period j (t = 1, 2, ..., N, j = 1, 2, ..., 48). Since our interest lies mainly in price modelling and prediction during working days, weekends and holidays were removed from the data following the approach used by Ramanathan et al. (1997) and Karakatsani and Bunn (2008a), among others. Moreover, in adopting an intradaily approach, we consider separately each load period, according to a well-established precedent for electricity loads and prices (Ramanathan et al., 1997; Bunn, 2000; Bunn and Karakatsani, 2003). Results were analysed in detail for five representative periods of the day: load periods 6 (02:30-03:00am), 18 (08:30-09:00am), 28 (13:30-14:00pm), 38 (18:30-19:00pm) and 44 (21:30-22:00pm). The night-time load period 6 is the least volatile; periods 18, 28 and 38 represent peak hours, and show a high volatility with sudden peaks during winter and summer in both 2005 and 2006. Finally, period 44 is relatively stable, with moderate volatility. These characteristics are common in electricity price dynamics as indicated, amongst others, in Huisman and Mahieu (2003) and Knittel and Roberts (2005).

Each series has length n=380. Figure 1 contains the plots of the five log-price time series considered; the logarithmic transformation was used to stabilize variance. The log-price series show neither a well-defined long-run behaviour nor a clear seasonal dynamics. However, levels change with the seasons, with an increase during the winter season. Moreover, the application of unit root tests indicates that the series are not stationary. In fact, the Augmented Dickey-Fuller test (Said and Dickey, 1984) rejects the null hypothesis of unit root only for period 28 and KPSS test (Kwiatkowski et al., 1992) always rejects the null hypothesis of stationarity (see Table 1).

Since some of the models considered or analysis require stationarity, in order to meet this requirement we assume that each series is the sum of a non stationary level component D_{jt} , describing level changes and/or long term and/or semi-periodic behaviour, and a residual stationary stochastic component p_{jt} , formally $\log P_{jt} = D_{jt} + p_{jt}$.

In the present work, the D_{jt} component has been estimated once for all by using a nonparametric technique based on the nearest neighbors method, also known as Friedman supersmoother (Friedman, 1984). The resulting series $p_{jt} = \log P_{jt} - D_{jt}$ are clearly stationary as can be seen in the right panel of Figure 1 and confirmed by both the ADF test and the KPSS test (see Table 1). In the following they will be referred as adjusted series.

Moreover, since here we are mainly interested in the relative predictive performance among a set of models and their combinations, we will focus on the prediction of

Table 1: Unit root tests for $log P_{jt}$ and p_{jt} . Symbols *, ** mean that the null hypothesis is rejected at 1% and 5% significance level respectively. In the ADF test, lag lengths are chosen following Ng and Perron (1995) method.

	$\log I$	j_t	p_{jt}	<u>,</u>
Load Period	ADF	KPSS	ADF	KPSS
6 (02:30-03:00am)	-1.981	0.958*	-7.795*	0.015
18 (08:30-09:00am)	-2.973	0.829^{*}	-6.917^*	0.017
28 (13:30-14:00pm)	-3.537**	0.417^{*}	-6.372*	0.015
38 (18:30-19:00pm)	-2.442	1.002*	-7.309*	0.014
44 (21:30-22:00pm)	-2.455	0.914*	-7.555*	0.016

 p_{jt} , whereas the D_{jt} component is fixed and equal for all models and combinations.

3 Individual forecasts

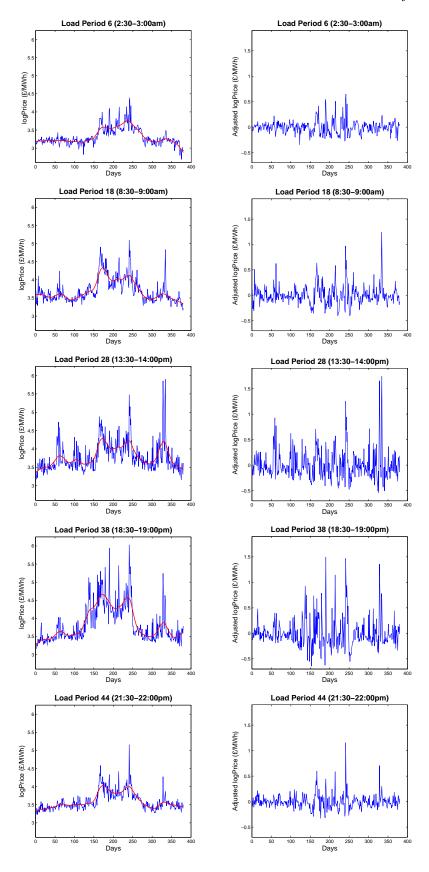
The individual models involved in this study are chosen because each of them is, potentially, very suitable to describe some specific features of the price dynamics. All models are based on a set of explanatory variables (in the log scale) that are strongly linked with the price evolution (see, Karakatsani and Bunn, 2008a among others), namely:

- the *Demand Forecast*, the national day-ahead demand forecast published by the system operator for each load period at time t-1;
- the *Indicated Margin*, the available capacity margin, defined as the difference between the sum of the maximum export limits nominated by each generator prior to each trading period, as its maximum available output capacity, and the demand forecast:
- the Gas Price, the daily UK natural gas one-day forward price, from the main National Balancing Point (NBP) hub. This is included because of its strong relation with power prices, especially during winter spikes. In particular, the series of deviations of gas prices from its deterministic component was considered;
- Past Prices, in particular, lags 1 and 5, corresponding to the previous day price and to the previous week price;
- Volatility, an indicator of instability and risk for both the electricity price series and for the demand forecast series. It is defined as the coefficient of variation computed on a rolling windows of the last 5 days.

The values at time t-1 of the first three variables represent forecasts for the next day. To face possible non linear relations between price and demand, and price and margin, quadratic polynomials of demand and margin were introduced. The individual forecasting models used in this study are:

• an ARMAX(p, q, r) model, where p and q are respectively the orders of the autoregressive and moving average parts, r is the order of the exogenous variable.

Figure 1: Left panel: log-price time series, $logP_{jt}$, with superimposed D_{jt} for the period April 2005 - September 2006. Right panel: the adjusted series p_{jt} .



In particular, for our dataset the identified model is the ARMAX(1,1,1).

$$p_{jt} = \phi_j p_{j(t-1)} + \varepsilon_{jt} + \theta_j \varepsilon_{j(t-1)} + \beta_j z_{j(t-1)}, \quad \varepsilon_{jt} \sim WN(0, \sigma_j^2), \quad (1)$$

where $z_{j(t-1)}$ is the indicated margin representing the exogenous variable, ε_{jt} is the error term and $\phi_j, \theta_j, \beta_j$ are constant coefficients. This model captures gradual adaptation through the the serial correlation in the adjusted log price series and immediate shocks in pricing caused by scarcity. It was estimated through maximum likelihood methods.

 a conventional constant parameter regression model (LR), which accounts for relations between prices and the various price drivers. The model is specified as:

$$p_{jt} = \boldsymbol{\beta}_{j}' \mathbf{X}_{jt} + \varepsilon_{jt}, \quad \varepsilon_{jt} \sim WN(0, \sigma_{j}^{2})$$
 (2)

where β_j is a $k \times 1$ vector of constant coefficients, \mathbf{X}_{jt} is the $k \times 1$ vector of regressors and ε_{jt} is an error term. The regressors are selected with stepwise backward techniques (AIC criterion) among the variables described above. The estimation was performed through maximum likelihood methods.

• a time-varying parameter regression model (TVR), with random walk parameters, allowing for price driver effects that continuously evolve:

$$p_{jt} = \beta'_{jt} \mathbf{X}_{jt} + \varepsilon_{jt}, \quad \varepsilon_{jt} \sim WN(0, \sigma_{\varepsilon_j}^2),$$
 (3)

$$\boldsymbol{\beta}_{j(t+1)} = \boldsymbol{\beta}_{jt} + \boldsymbol{\nu}_{jt}, \quad \boldsymbol{\nu}_{jt} \sim WN_k(0, \mathbf{H}_j),$$
 (4)

where β_{jt} is a vector of time-varying coefficients, \mathbf{X}_{jt} is the vector of regressors, ε_{jt} is the error term of the measurement equation and $\boldsymbol{\nu}_{jt}$ is the error term vector of the transition equation. It is assumed that $\mathbf{E}(\varepsilon_{jt}\boldsymbol{\nu}_{jt})=0$ and $\mathbf{H}_j=\mathrm{diag}\{\sigma_{\nu_{jk}}^2\}$. For this model parameters were estimated using state space methods and the Kalman filter (Hamilton, 1994 and Durbin and Koopman, 2001).

 a Markov regime switching model (MS) which should capture spikes and discontinuities in price series, distinguishing between normal and high-price regimes. It is defined as:

$$p_{jt} = \beta'_{jS_t} \mathbf{X}_{jt} + \varepsilon_{jt}, \quad \varepsilon_{jt} \sim WN(0, \sigma_{jS_t}^2),$$
 (5)

$$\Pr(S_t = i | S_{t-1} = h) = \pi_{ih}, \quad \forall i, h \in S$$

where S_t is the latent regime at time t, $S = \{1, 2\}$ the set of possible states (say, base and peak), $\boldsymbol{\beta}_{jS_t}$ is the vector of coefficients in regime S_t , \mathbf{X}_{jt} is the vector of regressors, $\sigma_{jS_t}^2$ the error variance in regime S_t and π_{ih} the transition probability between states i and h.

Maximum likelihood estimates of β_{jS_t} and $\sigma_{jS_t}^2$ are performed using the EM algorithm while for smoothed inferences of regimes, Kim's algorithm was used (Hamilton, 1994; Kim, 1994). The estimation procedure was applied referring both to the expanding dataset case (MS) and to the 6 month rolling windows

case (MS6). Once a MS model has been estimated, price forecasts are calculated as the linear combination of predicted prices across regimes weighted by predicted regime probabilities.

The regressors that were significant, at the 5% level, in the five different load periods are listed in Table 2. As can be seen, different periods have different significant specifications.

	Period 6	Period 18	Period 28	Period 38	Period 44
intercept	√	√	√		
p_{t-1}	\checkmark			\checkmark	\checkmark
$demF_{t-1}$				\checkmark	_
$dem F_{t-1}^2$			_	\checkmark	_
$margin_{t-1}$	\checkmark		$\sqrt{}$	\checkmark	\checkmark
$margin_{t-1}^2$	\checkmark			\checkmark	_
$gasF.res_{t-1}$	\checkmark		_	_	\checkmark
$demVol_t$	\checkmark			_	_
$priceVol_{\pm}$	_		_		1/

Table 2: Final sets of regressors obtained with stepwise backward techniques.

4 Combining forecasts

In general, a forecast combination based upon a set of K competing spot price predictors producing forecasts $\hat{P}_t^{(1)}, ..., \hat{P}_t^{(K)}$ of P_t , based on the information available up to time t-1, is given by:

$$\hat{P}_{t}^{C} = f\left(\hat{P}_{t}^{(1)}, ..., \hat{P}_{t}^{(K)}; \boldsymbol{\theta}\right) \tag{7}$$

with f a generic function, possibly nonlinear, and θ a parameter vector. Using linear functions, expression (7) becomes

$$\hat{P}_t^C = \sum_{k=1}^K \theta_k \hat{P}_t^{(k)}.$$
 (8)

where the vector $\boldsymbol{\theta}$ optimizes some criterion. Several studies have shown that, due to the effect of finite-sample error in estimating the combining weights, an equally weighted mean is often the best choice (Makridakis and Winkler, 1983; Clemen, 1989; Stock and Watson, 2001, 2004; Smith and Wallis, 2009). We follow this conclusion and in the rest of the paper we assume $\theta_k = 1/K$.

In our case, the forecasts derive from the models described in the previous section¹, and thus, for each trading period there are five forecasts of the same spot

¹Here we consider as different predictive models, the Markov switching models based on the expanding dataset (MS) and the 6 months rolling windows (MS6)

price, P_{jt} that can be considered singularly or combined. Although the final price predictions would be given by

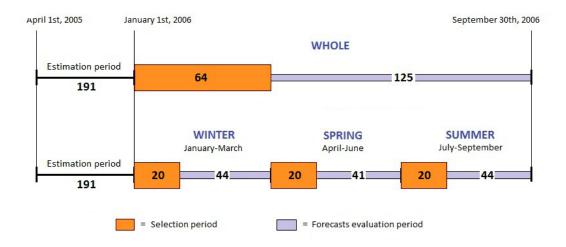
$$\hat{P}_{it} = \exp(D_{it} + \hat{p}_{it}) \tag{9}$$

with \hat{p}_{jt} the prediction of p_{jt} , when we refer to out-of-sample predictions we mean that we are considering out-of-sample forecasts of p_{jt} . Note that, although this is not a real out-of-sample prediction of P_{jt} because D_{jt} has been estimated with a smoother and not predicted, in our context this approach does not affect relative conclusions because all models are equally favoured or penalized by D_{jt} .

The whole dataset (April 1st, 2005 - September 30th, 2006) was divided into three parts. The first part, covering the period April 1st, 2005 - December 31th, 2005, is used only for individual model estimation. The remaining period (January 1st, 2006 - September 30th, 2006, 189 data) has been divided in further two parts: 1/3 is used to calibrate combined forecasts, i.e. to select the constituents of the combination, and 2/3 to out-of-sample forecasts evaluation (see Figure 2). Moreover, to compare the relative forecasting performances between individual models and combinations of the forecasts, 4 forecasting (sub-)periods were considered: the first three are associated with the different seasons (January-March, 44 data; April-June, 41 data; and July-September, 44 data) while the fourth includes the three seasons (January 1st, 2006 - September 30th, 2006, 125 data). The reason is to detect how much the forecasting accuracy of the predictions is influenced by the period of the year as well as by the considered trading period.

In our analyses comparisons are made on two levels: firstly we considered the

Figure 2: The framework of the prediction experiment (numbers in bold are sample sizes).



forecasting performance with respect to the following four statistics

MSE =
$$\frac{1}{m} \sum_{t=1}^{m} (P_{jt} - \hat{P}_{jt})^2$$
 MSPE = $\frac{1}{m} \sum_{t=1}^{m} \left(100 \times \frac{P_{jt} - \hat{P}_{jt}}{P_{jt}} \right)^2$
MAE = $\frac{1}{m} \sum_{t=1}^{m} \left| P_{jt} - \hat{P}_{jt} \right|$ MAPE = $\frac{1}{m} \sum_{t=1}^{m} \left| 100 \times \frac{P_{jt} - \hat{P}_{jt}}{P_{jt}} \right|$

with m the length of the forecasting period. We considered the significance of the difference in forecasting accuracy by means various tests, i.e. the Diebold and Mariano test (Diebold and Mariano, 1995), whose null hypothesis is that of no difference in the accuracy of two competing forecasters; a test based on the MCS (Model Confidence Set) procedure of Hansen et al. (2003, 2005) that, for two models, is similar to the Diebold and Mariano test but it estimates the distribution of the test statistic by a bootstrap procedure; and a test of forecast encompassing, whose null hypothesis is that predictions based on a model (for example CC) do not contain additional information with respect to those based on a second model (for example CI; in this case we say that CI encompasses CC). In the research literature, several formulations of encompassing test have been suggested (Newbold and Harvey, 2004; Clements and Harvey, 2007); here we adopted the specification given by Harvey et al. (1998), i.e. the modified Diebold and Mariano test statistic with demeaned forecasting errors. In the first two tests the equivalence between predictors is assessed with respect to some specified loss functions: here we considered mean square error (MSE) and mean absolute error (MAE). All tests were reported at the 5% significance level.

5 Comparing individual model forecasts and combinations of forecasts

Forecasting performances of the individual models and combinations are evaluated distinguishing among the 5 load periods (j = 6, 18, 28, 38, 44) referring to the trading hour of the day, 4 forecasting 'seasons' (3 'seasons' and the whole period) 4 prediction error statistics (MSE, MSPE, MAE, MAPE) and, when the Diebold and Mariano and/or the MCS tests are involved 2 loss functions (squared errors and absolute errors).

According to the approach followed by Hibon and Evgeniou (2005), all comparisons are performed from two different perspectives. Firstly we compare ex post the predictive performance of the best individual model (BI) with that of the best combination (BC). Since the evaluation is made ex post, this is not an out-of-sample prediction and it only allows us to check if there exists a combination giving better predictive performance than individual forecasts. Obviously, results are related to the specific models we considered.

In a second step, the comparisons are made considering models that have been selected in-sample and, thus, they account for possible misspecifications and/or estimation errors. We denote by CI the chosen individual model and by CC the chosen combination. In this case, out-of-sample predictions are involved.

The model selection is performed minimizing, in the validation period, one of the prediction error statistics described above and thus the models selected with respect to different indicators are not necessarily the same and, indeed, usually differ. When the descriptive indicators are involved, our study involves 80 cases (5 load periods \times 4 'seasons' \times 4 indicators). The number of cases scales consequently if some element (load period, 'season' or indicator) is kept fixed.

The results are graphically summarized, for the whole period case, in Figures 3-4. For example, the panel in position (1,1) of Figure 3 shows for the load period 6 and the MSE indicator the predictive performances in the out-of-sample forecasting period. The five points on the left represent the values of MSE corresponding to our five models, while the 26 points on the right relate to the MSE associated to the 26 possible combinations of 2, 3, 4 or 5 individual forecasts. The best/worst ex post individual model and combination, corresponding to the minimum/maximum value of the indicator, are reported in the figure. In this case the best performance is obtained with the forecasts combination of three models TVR, MS and ARMAX, which outperforms the best individual model MS. The arrows denote the MSE associated with the model/combination chosen in-sample. Note that, although there are 26 possible combinations and only 5 models, the comparison is fair because, in both categories, we consider only the model selected in-sample. The range of the MSE values can be interpreted as a measure of selection risk among individual forecasts or among combinations.

Detailed results are given, for all cases, in Tables 3-7, where we list the exact prediction error indicators and the p-values i) of the one-sided Diebold and Mariano test for the null hypothesis that best (chosen) individual forecasts have the same accuracy of the best (chosen) combined forecasts; ii) of the MCS test for the same hypothesis and iii) of the forecast encompassing for the null hypothesis that individual model predictions contain all the information contained in the combined predictions. Diebold and Mariano and MCS tests are performed with respect to loss functions based both on squared (rows MSE) and absolute errors (row MAE). This implies that the total number of comparisons is 160. Since the chosen models are different for different indicators, we have different p-values corresponding to different indicators. Table 8 lists a summary of the comparisons.

Table 9 contains the differences of performances of individual and combined forecasts with respect to the best possible performance (B), that is the minimum value of the prediction error statistics chosen ex post among all individual and combined forecasts. In particular, it lists the difference of performance, with respect to the best case, of the worst and of the chosen individual and combined forecasts. This gives us information about the riskiness of the two approaches.

5.1 Ex post analyses

In this first battery of analyses we compare, ex post, the best individual forecasts, among our five models, and the best combination of the predictions based on these models. The findings (see Figures 3-4 and Tables 3-7) highlight that, in general, combined models show better prediction ability in terms of prediction error statis-

tics. If we consider all the 80 comparisons², in 76% of them, the best possible forecasting model, obtained among all the individual models and all the combinations for each measure, is a combination (see also Table 8). Moreover, the worst performance - among all individual and combined forecasts - is always given by an individual model, so that selecting among combinations seems to be less risky than among individual models.

However, when we analyze the significance of the forecasting performance by means of tests (DM, MCS, encompassing), the predictive accuracy of the best combination is significantly better than that of the best individual model in only 8.75% of the 160 comparisons³, according to the DM test and in 3.75% according to MCS test. On the contrary, however, for both tests the individual model accuracy never significantly outperforms that of the best combination (see also Table 8).

In general, our analyses indicate that the best performances are obtained combining predictions of only two or three models. For example, considering the MAPE indicator in Figure 4, the best performing combination for the least volatile load period 6 and for the peak load period 38 is obtained with the models TVR, MS and ARMAX. This agrees with previous research: it has been argued that, rather than combining the full set of forecasts, it is often advantageous to discard the models with the worst performance (see, for instance, Aiolfi and Favero, 2005; Granger and Jeon, 2004; Marcellino, 2004; Stock and Watson, 2001, 2004). However, in our study some exceptions emerge when the worst predictive model is the TVR. In 7 cases, for the whole forecasting period (load periods 6, 18 and 44), and in 2 cases, during summer (load period 6), the best combination contains this (the worst performing) model.

5.2 Ex ante analyses

We focus now on the forecasting comparison of models chosen ex ante, as it might happen in practice. Thus, when models have to be selected, there is the risk that the chosen model is much worse than the best possible choice in terms of out-ofsample accuracy. For each period, the ex ante selection process considers individual methods and combinations.

For these analyses the series have been divided into three parts (see also Figure 2): an estimation period, coinciding with the in-sample period for the ex post analysis; a validation period, of length 1/3 of the remaining data⁴, used to enable the selection of the best individual model and combination ex ante and a forecasting period given by the last 2/3 of data⁵, used for out-of-sample comparisons among models.

With respect to the indicators, the results are similar to those of the expost case: the selected combined predictions produce forecasting error statistics lower than the selected individual model predictions in about 79% of cases (for detailed results see Tables 3-8).

However, the situation is quite different from the corresponding ex post case when

 $^{^2}$ 5 load periods \times 4 'seasons' \times 4 indicators

 $^{^35}$ load periods \times 4 'seasons' \times 4 indicators \times 2 loss functions

⁴64 data for the whole period and 20 data for the subperiods

 $^{^5125}$ data for the whole period and 44 or 41 data for the subperiods

we consider the statistical significance of the difference in out-of-sample forecasting accuracy. Indeed, combined predictions are significantly more accurate than individual model predictions in 33.13% of cases for D-M test and 18.13% for MCS test. The contrary is true only in 1.25% of cases for DM test and only in 0.63% of cases for MCS test (for detailed results see Tables 3-8). This points out the benefit in choosing among combinations in ex ante situations: our findings indicate that, in general, we obtain forecasts that are more accurate than selecting among the individual models, and when they are not more accurate, they are almost always not worse. Similar conclusions can be drawn with respect to the encompassing test: globally, the hypothesis that the chosen single forecasts contain the same information as the chosen combined forecasts is rejected 1/3 of times.

5.3 Risk analysis

Our third way to compare individual forecasts and combined forecasts is through the analysis of risks. In this regard, two interpretations of risk were considered. The first one refers to the risk of an incorrect individual model or combination selection, that is the risk of choosing a model or a combination that is not the best. We call this selection risk. The second kind of risk is that related to the probability of incurring in large prediction error and we call it prediction risk.

With respect to the selection risk, Table 9 shows that - in terms of performance indicators - the distance from the globally best predictor (that is, the best predictor among combinations and individual models, B) is generally smaller for the combination (compare column "CC-B" of Table 9 with respect to column "CI-B"). This suggests that combining forecasts is less risky.

As a measure of prediction risk the so-called Expected Shortfall (ES), the average forecasting error exceeding a specified quantile of the forecasting error distribution, was considered. To have reliable results, this kind of analysis was performed only for the whole period and for the quantiles, 95% and 97.5%. Moreover, in order to compare the Expected Shortfalls a simple rule was adopted: we say that the forecast combination is better than individual forecasts if the reduction in the ES is at least 5% (and viceversa). Interpreting our results, although in most of cases the differences are smaller than 5%, the combination led to improvements which are larger than 5% in about 35% of cases, while improvements larger than 5% for individual models occur only in about 7.5% of case.

6 Summary and conclusions

We have compared the relative forecasting performances of five individual models and simple average combinations. The summary findings are as follows:

- in ex post comparisons, although the combined forecasts perform better than individual forecasts in 76% of cases, only in a few cases they are also significantly more accurate at the 5% level;
- in ex ante comparisons, when out-of-sample predictions are involved, the general indications are not very different but quite different in terms of the signifi-

cance of the improvements. Indeed, when the analyses are based on individual and combined forecasts obtained through in-sample selection, the latter is significantly more accurate than individual forecasts in about 33% of cases. On the contrary, individual forecasts are more accurate in only 1% of cases. Thus, within the limit of our data and of the considered models, we can conclude that in about 99% of cases, seeking a combination of forecasts leads to predictions more accurate than or equivalent to those obtained through seeking to identify the individually best forecasts:

- our study stresses also that choosing an individual model out of a set of models is more risky than choosing among combinations of their forecasts and that combining is effective under value at risk criteria as well as for average accuracy.

In terms of the sensitivity of these results, it is worth noting that very similar results were obtained by considering adaptive weights, following Bates and Granger (1969), rather than simple averaging. Interestingly, similar results can be obtained by using all five methods in the combination rather than a chosen subset, but only if the adaptive weights are used instead of simple averaging. It is intuitive that if the task of optimising a subset is avoided, there is a compensating need to use optimal weights.

Finally, these analyses provide further indications of the specification difficulties in modelling electricity prices. The fact that a simple combination of a subset of quite sophisticated methods such as Markov regime switching and time varying regressions, as well as ARMAX and linear regression, provides a more accurate forecasting procedure, points to the inadequacies in each of these methods and/or the ability to select the best performing one reliably.

Figure 3: Forecasting performances of the individual models (I, on the left inside each figure) and of all the combinations (C, on the in-sample. Results refer to the whole out-of-sample period (125 data). right). The arrows indicate the value of the indicator (MSE in the first row and MSPE in the second row) for the models chosen

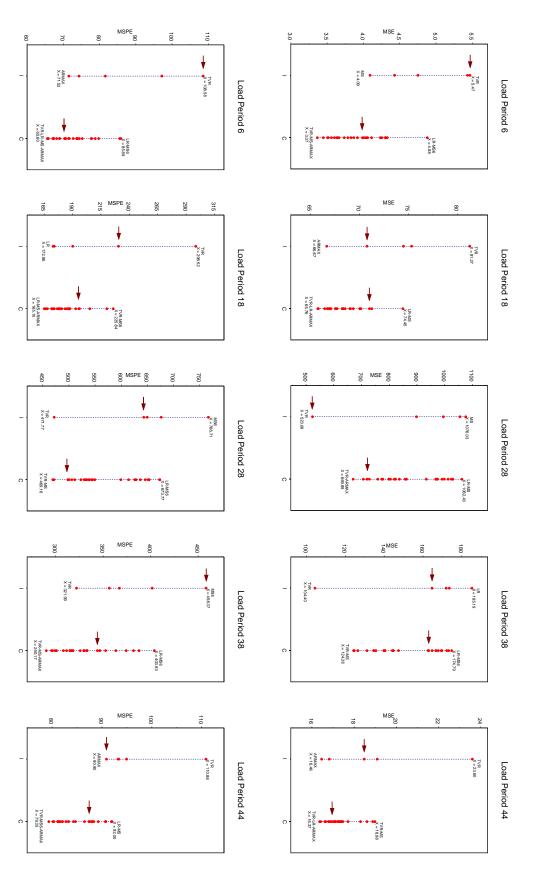


Figure 4: Forecasting performances of the individual models (I, on the left inside each figure) and of all the combinations (C, on the right). The arrows indicate the value of the indicator (MAE in the first row and MAPE in the second row) for the models chosen

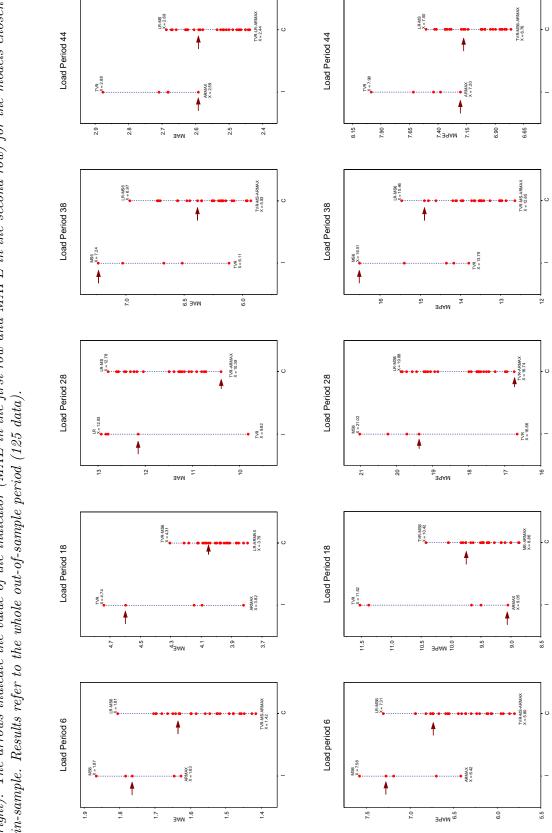


Table 3: Load period 6. Prediction error statistics values and p-values for the Diebold-Mariano, MCS and encompassing tests. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

		Wł	nole		Winter					
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models			Predict	tion error s	tatistics v	alues				
BI	4.092	71.521	1.627	6.419	56.454	266.751	5.291	12.089		
BC	3.366	65.598	1.415	5.803	56.140	236.093	5.222	11.944		
CI	5.466	108.583	1.764	7.278	69.946	368.523	5.972	14.267		
CC	3.987	70.496	1.632	6.735	68.598	318.663	5.599	12.736		
	BI vs. BC									
Loss Function				D-M test p						
MSE	0.014	0.051	0.034	0.034	0.480	0.408	0.480	0.480		
MAE	< 0.001	0.057	0.019	0.019	0.435	0.321	0.435	0.435		
				MCS test I	o-values					
MSE	0.025	0.108	0.072	0.083	0.961	0.785	0.962	0.963		
MAE	0.001	0.111	0.044	0.041	0.866	0.650	0.865	0.856		
				CI vs.	\mathbf{CC}					
Loss Function	0.000	. 0 224	0.015	D-M test p		0.435	0.755	0.755		
MSE	0.006	< 0.001	0.018	0.018	0.341	0.438	0.155	0.155		
MAE	0.015	< 0.001	0.078	0.078	0.386	0.458	0.104	0.104		
				MCS test p						
MSE	0.008	0.001	0.034	0.032	0.702	0.777	0.257	0.248		
MAE	0.031	0.003	0.173	0.179	0.780	0.918	0.236	0.228		
\mathbf{H}_0	0.001	. 0 001		ompassing t	-		0.00=	0.00=		
CI encompasses CC	0.001	< 0.001	0.002	0.002	0.419	0.479	0.097	0.097		
					Summer					
		Spr	ring			Sum	mer			
	MSE	MSPE	MAE MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models	MSE		MAE	MAPE		MSPE		MAPE		
Models BI	MSE 2.401		MAE			MSPE		MAPE 7.128		
		MSPE	MAE	tion error s	tatistics v	MSPE	MAE			
BI	2.401	MSPE 37.200	MAE Predict	tion error s	tatistics v	MSPE alues 94.443	MAE 1.549	7.128		
BI BC	2.401 2.419	MSPE 37.200 40.024	MAE Predict 1.170 1.280	tion error s 4.724 5.280	tatistics v 4.054 3.755	MSPE alues 94.443 94.321	MAE 1.549 1.391	7.128 6.558		
BI BC CI	2.401 2.419 6.163	MSPE 37.200 40.024 107.967	MAE Predict 1.170 1.280 2.153	tion error s 4.724 5.280 8.949	4.054 3.755 4.363 4.099	MSPE alues 94.443 94.321 104.202	MAE 1.549 1.391 1.681	7.128 6.558 7.707		
BI BC CI	2.401 2.419 6.163	MSPE 37.200 40.024 107.967	MAE Predict 1.170 1.280 2.153 1.662	4.724 5.280 8.949 6.956	tatistics v. 4.054 3.755 4.363 4.099 BC	MSPE alues 94.443 94.321 104.202	MAE 1.549 1.391 1.681	7.128 6.558 7.707		
BI BC CI CC	2.401 2.419 6.163	MSPE 37.200 40.024 107.967	MAE Predict 1.170 1.280 2.153 1.662	tion error s 4.724 5.280 8.949 6.956 BI vs.	4.054 3.755 4.363 4.099	MSPE alues 94.443 94.321 104.202	MAE 1.549 1.391 1.681	7.128 6.558 7.707		
BI BC CI CC	2.401 2.419 6.163 3.813	37.200 40.024 107.967 68.011	MAE Predict 1.170 1.280 2.153 1.662	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p	4.054 3.755 4.363 4.099 BC	MSPE alues 94.443 94.321 104.202 101.553	1.549 1.391 1.681 1.391	7.128 6.558 7.707 6.558		
BI BC CI CC Loss Function MSE	2.401 2.419 6.163 3.813	MSPE 37.200 40.024 107.967 68.011	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463	4.054 3.755 4.363 4.099 BC o-values 0.121 0.039	MSPE alues 94.443 94.321 104.202 101.553	MAE 1.549 1.391 1.681 1.391 0.301	7.128 6.558 7.707 6.558 0.301 0.037		
BI BC CI CC Loss Function MSE	2.401 2.419 6.163 3.813	MSPE 37.200 40.024 107.967 68.011	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058	tion error s' 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058	4.054 3.755 4.363 4.099 BC o-values 0.121 0.039	MSPE alues 94.443 94.321 104.202 101.553	MAE 1.549 1.391 1.681 1.391 0.301	7.128 6.558 7.707 6.558		
BI BC CI CC Loss Function MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058	MSPE 37.200 40.024 107.967 68.011 0.463 0.058	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058	tion error s' 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p	4.054 3.755 4.363 4.099 BC o-values 0.121 0.039 o-values	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229	1.549 1.391 1.681 1.391 0.301 0.037	7.128 6.558 7.707 6.558 0.301 0.037		
BI BC CI CC Loss Function MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058	tion error s' 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924	### 4.054 ### 3.755 ### 4.363 ### 4.099 ### BC ### D-values ### 0.121 ### 0.039 ### 0.204 ### 0.108	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465	MAE 1.549 1.391 1.681 1.391 0.301 0.037 0.578	7.128 6.558 7.707 6.558 0.301 0.037		
BI BC CI CC Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219	tion error s' 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924 0.219 CI vs. D-M test p	### Automatic Au	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067		
BI BC CI CC Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924 0.219 CI vs. D-M test p	### Acceptance	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067		
BI BC CI CC Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219 < 0.001 < 0.001	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924 0.219 CI vs. D-M test p < 0.001 < 0.001	### Automatic Au	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215 < 0.001 < 0.001	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219 < 0.001 < 0.001	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924 0.219 CI vs. D-M test p < 0.001 < 0.001 MCS test p	### Automatic ### Automatic	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421 0.065 < 0.001	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226 < 0.001 < 0.001	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215 < 0.001 < 0.001	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219 < 0.001 < 0.001 < 0.001	### display of the control of the co	### Acceptable of the control of the	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421 0.065 < 0.001 0.101	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067 0.149 0.002		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215 < 0.001 < 0.001	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219 < 0.001 < 0.001	tion error s 4.724 5.280 8.949 6.956 BI vs. D-M test p 0.463 0.058 MCS test p 0.924 0.219 CI vs. D-M test p < 0.001 < 0.001 MCS test p	### Automatic ### Automatic	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421 0.065 < 0.001	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	2.401 2.419 6.163 3.813 0.463 0.058 0.920 0.226 < 0.001 < 0.001	MSPE 37.200 40.024 107.967 68.011 0.463 0.058 0.921 0.215 < 0.001 < 0.001	MAE Predict 1.170 1.280 2.153 1.662 0.463 0.058 0.923 0.219 < 0.001 < 0.001 < 0.001 < 0.001	### display of the control of the co	### A.054 ### A.054 ### A.054 ### A.054 ### A.054 ### A.063 ### A.	MSPE alues 94.443 94.321 104.202 101.553 0.234 0.229 0.465 0.421 0.065 < 0.001 0.101 0.001	1.549 1.391 1.681 1.391 0.301 0.037 0.578 0.078	7.128 6.558 7.707 6.558 0.301 0.037 0.576 0.067 0.149 0.002		

Table 4: Load period 18. Prediction error statistics values and p-values for the Diebold-Mariano, MCS and encompassing tests. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

		Wh	ole		Winter				
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE	
Models			Predic	tion error	statistics v	alues			
BI	66.670	172.855	3.822	9.050	280.442	330.798	8.908	13.517	
BC	65.758	165.096	3.795	8.863	276.851	313.603	9.099	13.237	
CI	70.780	230.445	4.597	9.050	355.069	378.061	10.476	14.738	
CC	71.037	195.548	4.054	9.753	321.389	321.217	9.369	13.530	
				BI vs.	BC				
Loss Function				D-M test	p-values				
MSE	0.182	0.119	0.392	0.343	0.377	0.284	0.495	0.181	
MAE	0.312	0.005	0.437	0.499	0.236	0.305	0.355	0.323	
				MCS test	p-values				
MSE	0.609	0.159	0.711	0.540	0.756	0.520	0.991	0.277	
MAE	0.668	0.007	0.853	0.998	0.400	0.587	0.671	0.619	
				CI vs.	\mathbf{CC}				
Loss Function				D-M test	•				
MSE	0.482	0.011	0.011	0.449	0.070	0.081	0.081	0.081	
MAE	< 0.001	< 0.001	< 0.001	0.021	0.070	0.071	0.071	0.071	
				MCS test	p-values				
MSE	0.954	0.028	0.030	0.893	0.089	0.091	0.091	0.086	
MAE	< 0.001	< 0.001	< 0.001	0.039	0.152	0.092	0.097	0.092	
\mathbf{H}_0				ompassing	_				
CI encompasses CC	0.740	0.003	0.003	0.479	0.034	0.097	0.097	0.097	
		C	·		Summer				
		Spr	ing			Sum	illei		
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE	
Models	MSE		MAE	MAPE		MSPE		MAPE	
Models BI	MSE 11.382		MAE			MSPE		MAPE 6.817	
		MSPE	MAE	tion error	statistics v	MSPE	MAE		
BI	11.382	MSPE 91.653	MAE Predic 2.509	tion error	statistics v	MSPE alues 93.710	MAE 2.136	6.817	
BI BC	11.382 11.396	MSPE 91.653 83.109	MAE Predict 2.509 2.543	7.453 7.439	statistics v 9.407 9.740	MSPE alues 93.710 95.559	MAE 2.136 2.031	6.817 6.499	
BI BC CI	11.382 11.396 17.814	MSPE 91.653 83.109 91.653	MAE Predic 2.509 2.543 2.509	7.453 7.439 7.453	statistics v 9.407 9.740 14.503 15.219	MSPE alues 93.710 95.559 101.057	MAE 2.136 2.031 2.136	6.817 6.499 6.817	
BI BC CI	11.382 11.396 17.814	MSPE 91.653 83.109 91.653	MAE Predic 2.509 2.543 2.509	7.453 7.439 7.453 7.598	statistics v 9.407 9.740 14.503 15.219 BC	MSPE alues 93.710 95.559 101.057	MAE 2.136 2.031 2.136	6.817 6.499 6.817	
BI BC CI CC	11.382 11.396 17.814	MSPE 91.653 83.109 91.653	MAE Predic 2.509 2.543 2.509	7.453 7.439 7.453 7.598 BI vs.	statistics v 9.407 9.740 14.503 15.219 BC	MSPE alues 93.710 95.559 101.057	MAE 2.136 2.031 2.136	6.817 6.499 6.817	
BI BC CI CC	11.382 11.396 17.814 13.169	MSPE 91.653 83.109 91.653 92.395	MAE Predic 2.509 2.543 2.509 2.578	7.453 7.439 7.453 7.598 BI vs.	9.407 9.740 14.503 15.219 BC p-values	MSPE alues 93.710 95.559 101.057 95.797	MAE 2.136 2.031 2.136 2.146	6.817 6.499 6.817 6.874	
BI BC CI CC Loss Function MSE	11.382 11.396 17.814 13.169	MSPE 91.653 83.109 91.653 92.395	MAE Predic 2.509 2.543 2.509 2.578 0.497	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264	MSPE alues 93.710 95.559 101.057 95.797	MAE 2.136 2.031 2.136 2.146	6.817 6.499 6.817 6.874	
BI BC CI CC Loss Function	11.382 11.396 17.814 13.169	MSPE 91.653 83.109 91.653 92.395	MAE Predic 2.509 2.543 2.509 2.578 0.497	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264	MSPE alues 93.710 95.559 101.057 95.797	MAE 2.136 2.031 2.136 2.146	6.817 6.499 6.817 6.874	
BI BC CI CC Loss Function MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433	91.653 83.109 91.653 92.395 0.482 0.423	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395	MAE 2.136 2.031 2.136 2.146 0.300 0.239	6.817 6.499 6.817 6.874 0.300 0.239	
BI BC CI CC Loss Function MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345	MAE 2.136 2.031 2.136 2.146 0.300 0.239 0.601	6.817 6.499 6.817 6.874 0.300 0.239	
BI BC CI CC Loss Function MSE MAE MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747	0.300 0.239 0.601 0.191	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC Loss Function MSE MAE MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836 0.314 0.365	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868 0.314 0.365	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365 MCS test	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454 p-values	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747 0.191 0.442	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC CC Loss Function MSE MAE Loss Function MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868 0.314 0.365 0.664	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365 MCS test 0.673	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454 p-values 0.608	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747 0.191 0.442 0.415	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	MSPE 91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836 0.314 0.365	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868 0.314 0.365	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365 MCS test	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454 p-values	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747 0.191 0.442	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE HO	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868 0.314 0.365 0.664 0.708 Enc	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365 MCS test 0.673 0.722 ompassing	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454 p-values 0.608 0.897 test p-values	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747 0.191 0.442 0.415 0.879	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	11.382 11.396 17.814 13.169 0.497 0.433 0.993 0.863	91.653 83.109 91.653 92.395 0.482 0.423 0.965 0.836	MAE Predic 2.509 2.543 2.509 2.578 0.497 0.433 0.995 0.868 0.314 0.365 0.664 0.708	7.453 7.439 7.453 7.598 BI vs. D-M test 0.497 0.433 MCS test 0.995 0.855 CI vs. D-M test 0.314 0.365 MCS test 0.673 0.722	9.407 9.740 14.503 15.219 BC p-values 0.335 0.264 p-values 0.456 0.480 CC p-values 0.301 0.454 p-values 0.608 0.897	MSPE alues 93.710 95.559 101.057 95.797 0.172 0.395 0.345 0.747 0.191 0.442 0.415 0.879	0.300 0.239 0.601 0.415	6.817 6.499 6.817 6.874 0.300 0.239 0.598 0.411	

Table 5: Load period 28. Prediction error statistics values and p-values for the Diebold-Mariano, MCS and encompassing tests. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

		Wh	ole		Winter				
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE	
Models			Predic	ction error	statistics	values			
BI	523.078	471.771	9.816	16.658	924.282	590.634	15.881	19.254	
BC	669.886	469.162	10.392	16.740	913.736	617.322	15.842	19.328	
CI	523.078	643.093	12.145	19.377	934.600	590.634	15.881	19.254	
CC	719.774	497.826	10.392	16.740	936.435	621.086	16.690	20.626	
		s. BC							
Loss Function				D-M test	t p-values				
MSE	0.095	0.095	0.095	0.095	0.432	0.386	0.424	0.424	
MAE	0.190	0.141	0.190	0.190	0.455	0.291	0.466	0.466	
					t p-values				
MSE	0.259	0.268	0.264	0.266	0.843	0.731	0.839	0.835	
MAE	0.378	0.218	0.370	0.388	0.907	0.593	0.918	0.925	
				CI vs	s. CC				
Loss Function				D-M test	t p-values				
MSE	0.101	0.082	0.082	0.082	0.434	0.424	0.157	0.157	
MAE	0.152	0.010	0.010	0.010	0.130	0.466	0.074	0.074	
				MCS tes	t p-values				
MSE	0.282	0.133	0.127	0.121	0.896	0.839	0.395	0.410	
MAE	0.235	0.028	0.032	0.029	0.424	0.928	0.135	0.139	
\mathbf{H}_0			Enc	compassing	g test p-val	ues			
CI encompasses CC	0.228	0.151	0.151	0.151	0.990	0.765	0.449	0.449	
		en.	ina		Summer				
		Spri	ing			Sum	illei		
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE	
Models	MSE		MAE		MSE	MSPE		MAPE	
Models BI	MSE 68.973		MAE			MSPE	MAE	MAPE 14.849	
BI	68.973	MSPE 433.676	MAE Prediction 6.382	ction error	statistics	MSPE values 382.361	MAE 5.513	14.849	
BI BC	68.973 73.274	MSPE 433.676 406.469	MAE Predic 6.382 6.140	ction error 16.075 15.318	statistics 60.680 55.241	MSPE values 382.361 369.110	MAE 5.513 5.279	14.849 14.363	
BI	68.973	MSPE 433.676	MAE Prediction 6.382	ction error	statistics	MSPE values 382.361	MAE 5.513	14.849	
BI BC CI	68.973 73.274 88.021	MSPE 433.676 406.469 448.339	MAE Predic 6.382 6.140 6.382	16.075 15.318 16.509 15.318	* statistics * 60.680	MSPE values 382.361 369.110 545.883	5.513 5.279 6.561	14.849 14.363 17.682	
BI BC CI	68.973 73.274 88.021	MSPE 433.676 406.469 448.339	MAE Predic 6.382 6.140 6.382	etion error 16.075 15.318 16.509 15.318 BI vs	* statistics 60.680 55.241 81.937 79.430	MSPE values 382.361 369.110 545.883	5.513 5.279 6.561	14.849 14.363 17.682	
BI BC CI CC	68.973 73.274 88.021 73.274	MSPE 433.676 406.469 448.339 408.630	Predic 6.382 6.140 6.382 6.140	tion error 16.075 15.318 16.509 15.318 BI vs	60.680 55.241 81.937 79.430 s. BC t p-values	MSPE values 382.361 369.110 545.883 433.093	5.513 5.279 6.561 6.318	14.849 14.363 17.682 16.971	
BI BC CI CC	68.973 73.274 88.021	MSPE 433.676 406.469 448.339	MAE Predic 6.382 6.140 6.382	etion error 16.075 15.318 16.509 15.318 BI vs	60.680 55.241 81.937 79.430 s. BC	MSPE values 382.361 369.110 545.883	5.513 5.279 6.561	14.849 14.363 17.682	
BI BC CI CC Loss Function	68.973 73.274 88.021 73.274	MSPE 433.676 406.469 448.339 408.630	MAE Predic 6.382 6.140 6.382 6.140 0.207	16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030	60.680 55.241 81.937 79.430 s. BC t p-values 0.256	MSPE values 382.361 369.110 545.883 433.093	5.513 5.279 6.561 6.318	14.849 14.363 17.682 16.971	
BI BC CI CC Loss Function	68.973 73.274 88.021 73.274	MSPE 433.676 406.469 448.339 408.630	MAE Predic 6.382 6.140 6.382 6.140 0.207	16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139	MSPE values 382.361 369.110 545.883 433.093	5.513 5.279 6.561 6.318 0.297 0.266	14.849 14.363 17.682 16.971	
BI BC CI CC Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139	MSPE 433.676 406.469 448.339 408.630 0.191 0.411	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139	16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030 MCS tes	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266	5.513 5.279 6.561 6.318	14.849 14.363 17.682 16.971 0.385 0.281	
BI BC CI CC Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541	16.075 15.318 16.509 15.318 BI v: D-M test 0.005 0.030 MCS tes 0.050 0.151	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584	MAE 5.513 5.279 6.561 6.318 0.297 0.266 0.571	14.849 14.363 17.682 16.971 0.385 0.281	
BI BC CI CC Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541	Etion error 16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030 MCS tes 0.050 0.151 CI vs	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584	MAE 5.513 5.279 6.561 6.318 0.297 0.266 0.571	14.849 14.363 17.682 16.971 0.385 0.281	
BI BC CI CC Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541	Etion error 16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030 MCS tes 0.050 0.151 CI vs	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584	MAE 5.513 5.279 6.561 6.318 0.297 0.266 0.571	14.849 14.363 17.682 16.971 0.385 0.281	
BI BC CI CC Loss Function MSE MAE MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417	Etion error 16.075 15.318 16.509 15.318 BI vs D-M test 0.005 0.030 MCS tes 0.050 0.151 CI vs	s. BC t p-values 0.422 0.354 c. CC t p-values	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417	D-M test 0.050 0.151 CI vs 0.207 0.139	* statistics * 60.680	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417	D-M test 0.050 0.151 CI vs 0.207 0.139	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354 s. CC t p-values	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855 0.207 0.139	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417 0.207 0.139	D-M test 0.050 0.151 CI vs 0.207 0.139 MCS tes	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354 s. CC t p-values 0.256 0.139	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491 0.099 0.063	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	
BI BC CI CC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE Ho	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855 0.207 0.139 0.543	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417 0.207 0.139 0.544 0.418	D-M test 0.207 0.139 MCS tes 0.207 0.139 MCS tes 0.207 0.139 MCS tes 0.539 0.416	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354 s. CC t p-values 0.256 0.139 t p-values 0.221 t p-values	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491 0.099 0.063 0.032 0.101	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	
BI BC CI CC CI CC Loss Function MSE MAE Loss Function MSE MAE	68.973 73.274 88.021 73.274 0.207 0.139 0.558 0.417	MSPE 433.676 406.469 448.339 408.630 0.191 0.411 0.449 0.855 0.207 0.139 0.543	MAE Predic 6.382 6.140 6.382 6.140 0.207 0.139 0.541 0.417 0.207 0.139 0.544 0.418	D-M test 0.207 0.139 MCS tes 0.207 0.139 MCS tes 0.207 0.139 MCS tes 0.539 0.416	60.680 55.241 81.937 79.430 s. BC t p-values 0.256 0.139 t p-values 0.422 0.354 s. CC t p-values 0.221 t p-values 0.221 t p-values	MSPE values 382.361 369.110 545.883 433.093 0.297 0.266 0.584 0.491 0.099 0.063 0.032 0.101	5.513 5.279 6.561 6.318 0.297 0.266 0.571 0.487	14.849 14.363 17.682 16.971 0.385 0.281 0.746 0.580	

Table 6: Load period 38. Prediction error statistics values and p-values for the Diebold-Mariano, MCS and encompassing tests. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

		Wl	Winter							
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models			Predi	ction error	statistics va	lues				
BI	104.403	321.991	6.114	13.793	2373.833	622.140	23.497	19.307		
BC	124.260	290.172	5.927	12.646	2316.932	614.194	23.339	19.126		
CI	164.629	458.370	7.238	16.509	2795.410	903.622	26.675	22.443		
\overline{CC}	162.906	343.986	6.385	14.896	2431.601	696.829	24.507	20.160		
	BI vs. BC									
Loss Function				D-M test	p-values					
MSE	0.170	0.173	0.173	0.173	0.403	0.460	0.460	0.460		
MAE	0.282	0.282	0.282	0.282	0.130	0.444	0.444	0.444		
				MCS test	p-values					
MSE	0.452	0.551	0.560	0.560	0.783	0.920	0.923	0.924		
MAE	0.596	0.606	0.597	0.600	0.207	0.896	0.893	0.895		
				CI vs.	CC					
Loss Function				D-M test	p-values					
MSE	0.377	0.002	0.002	< 0.001	0.014	0.027	0.424	0.424		
MAE	0.256	< 0.001	< 0.001	0.001	0.004	0.021	0.035	0.035		
				MCS test	p-values					
MSE	0.744	0.070	0.075	0.030	0.017	0.035	0.841	0.841		
MAE	0.515	0.004	0.003	0.010	0.007	0.042	0.035	0.035		
\mathbf{H}_0			Enc	compassing	g test p-values					
CI encompasses CC	0.131	< 0.001	< 0.001	< 0.001	0.012	0.012	0.598	0.598		
	Spring Summer									
		Spi	rıng			Sumr	ner			
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models	MSE		MAE	MAPE		MSPE		MAPE		
Models BI	MSE 39.878		MAE			MSPE		MAPE 12.019		
		MSPE	MAE Predic	ction error	statistics va	MSPE	MAE			
BI	39.878	MSPE 236.531	MAE Prediction 4.298	ction error	statistics va	MSPE alues 254.507	MAE 4.023	12.019		
BI BC	39.878 39.751	MSPE 236.531 216.672	MAE Predict 4.298 4.063	ction error 11.162 10.533	statistics va 29.902 25.076	MSPE alues 254.507 216.955	MAE 4.023 3.760	12.019 11.092		
BI BC CI	39.878 39.751 55.925	MSPE 236.531 216.672 314.892	MAE Predic 4.298 4.063 4.872	ction error 11.162 10.533 12.845	statistics va 29.902 25.076 36.825 32.603	MSPE alues 254.507 216.955 292.681	MAE 4.023 3.760 4.673	12.019 11.092 13.588		
BI BC CI	39.878 39.751 55.925	MSPE 236.531 216.672 314.892	MAE Predic 4.298 4.063 4.872	tion error 11.162 10.533 12.845 10.643	statistics va 29.902 25.076 36.825 32.603	MSPE alues 254.507 216.955 292.681	MAE 4.023 3.760 4.673	12.019 11.092 13.588		
BI BC CI CC	39.878 39.751 55.925	MSPE 236.531 216.672 314.892	MAE Predic 4.298 4.063 4.872	tion error 11.162 10.533 12.845 10.643 BI vs.	statistics va 29.902 25.076 36.825 32.603	MSPE alues 254.507 216.955 292.681	MAE 4.023 3.760 4.673	12.019 11.092 13.588		
BI BC CI CC	39.878 39.751 55.925 39.751	MSPE 236.531 216.672 314.892 216.672	MAE Predic 4.298 4.063 4.872 4.063	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test	statistics va 29.902 25.076 36.825 32.603 BC p-values	MSPE 254.507 216.955 292.681 292.619	MAE 4.023 3.760 4.673 4.465	12.019 11.092 13.588 13.387		
BI BC CI CC Loss Function MSE	39.878 39.751 55.925 39.751	MSPE 236.531 216.672 314.892 216.672	MAE Predic 4.298 4.063 4.872 4.063	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053	29.902 25.076 36.825 32.603 BC p-values 0.101 0.076	MSPE 254.507 216.955 292.681 292.619	MAE 4.023 3.760 4.673 4.465	12.019 11.092 13.588 13.387		
BI BC CI CC Loss Function MSE	39.878 39.751 55.925 39.751	MSPE 236.531 216.672 314.892 216.672	MAE Predic 4.298 4.063 4.872 4.063	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107	29.902 25.076 36.825 32.603 BC p-values 0.101 0.076	MSPE 254.507 216.955 292.681 292.619	MAE 4.023 3.760 4.673 4.465	12.019 11.092 13.588 13.387		
BI BC CI CC Loss Function MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178	MSPE 236.531 216.672 314.892 216.672 0.032 0.154	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test	statistics va 29.902 25.076 36.825 32.603 BC p-values 0.101 0.076 p-values	MSPE 254.507 216.955 292.681 292.619 0.167 0.055	MAE 4.023 3.760 4.673 4.465 0.101 0.076	12.019 11.092 13.588 13.387 0.101 0.076		
BI BC CI CC Loss Function MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test 0.244	29.902 25.076 36.825 32.603 BC p-values 0.101 0.076 p-values 0.130 0.315	MSPE 254.507 216.955 292.681 292.619 0.167 0.055	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118	12.019 11.092 13.588 13.387 0.101 0.076		
BI BC CI CC Loss Function MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test 0.244 0.233	### statistics va	MSPE 254.507 216.955 292.681 292.619 0.167 0.055	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118	12.019 11.092 13.588 13.387 0.101 0.076		
BI BC CI CC Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test 0.244 0.233 CI vs. D-M test 0.031	### statistics va	MSPE 254.507 216.955 292.681 292.619 0.167 0.055	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118	12.019 11.092 13.588 13.387 0.101 0.076		
BI BC CI CC Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test 0.244 0.233 CI vs. D-M test	statistics va 29.902 25.076 36.825 32.603 BC p-values 0.101 0.076 p-values 0.130 0.315 CC p-values	MSPE 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310		
BI BC CI CC Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031	tion error 11.162 10.533 12.845 10.643 BI vs. D-M test 0.053 0.107 MCS test 0.244 0.233 CI vs. D-M test 0.031	statistics va 29.902 25.076 36.825 32.603 BC p-values 0.101 0.076 p-values 0.130 0.315 CC p-values 0.269 0.327	MSPE alues 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310		
BI BC CI CC Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031	D-M test 0.233 CI vs. D-M test 0.043 CI vs. D-M test 0.053 0.107	statistics va 29.902 25.076 36.825 32.603 BC p-values 0.101 0.076 p-values 0.130 0.315 CC p-values 0.269 0.327	MSPE alues 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294 0.031 0.047	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031 0.047	D-M test 0.244 0.233 CI vs. D-M test 0.047 MCS test	### statistics va	MSPE 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071 0.269 0.327	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322 0.269 0.327	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310 0.231 0.379		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300 0.031 0.047 0.038	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294 0.031 0.047 0.039	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031 0.047 0.043 0.070	D-M test 0.244 0.233 CI vs. D-M test 0.047 MCS test 0.047 MCS test 0.044	### statistics va	MSPE alues 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071 0.269 0.327 0.452 0.601	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322 0.269 0.327 0.452	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310 0.231 0.379 0.400		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	39.878 39.751 55.925 39.751 0.480 0.178 0.963 0.300 0.031 0.047 0.038	MSPE 236.531 216.672 314.892 216.672 0.032 0.154 0.091 0.294 0.031 0.047 0.039	MAE Predic 4.298 4.063 4.872 4.063 0.032 0.154 0.105 0.300 0.031 0.047 0.043 0.070	D-M test 0.024 0.233 CI vs. D-M test 0.047 MCS test 0.047 MCS test 0.044 0.076	### statistics va	MSPE alues 254.507 216.955 292.681 292.619 0.167 0.055 0.250 0.071 0.269 0.327 0.452 0.601	MAE 4.023 3.760 4.673 4.465 0.101 0.076 0.118 0.322 0.269 0.327 0.452	12.019 11.092 13.588 13.387 0.101 0.076 0.126 0.310 0.231 0.379 0.400		

Table 7: Load period 44. Prediction error statistics values and p-values for the Diebold-Mariano, MCS and encompassing tests. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

		Wh	ole			Winter				
	MSE	MSPE	MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models Prediction error statistics values										
BI	16.462	90.904	2.592	7.203	309.909	276.057	7.840	11.983		
BC	16.366	79.345	2.438	6.762	329.600	266.004	7.609	11.472		
CI	18.478	90.904	2.592	7.203	360.028	284.415	8.885	12.126		
CC	16.944	87.873	2.590	7.177	355.264	287.700	8.026	12.159		
BI vs. BC										
Loss Function				D-M t	est p-values					
MSE	0.480	0.417	0.480	0.417	0.183	0.183	0.183	0.183		
MAE	0.130	0.170	0.130	0.170	0.152	0.152	0.152	0.152		
				MCS t	test p-values					
MSE	0.960	0.803	0.956	0.813	0.564	0.569	0.571	0.569		
MAE	0.320	0.343	0.320	0.361	0.424	0.420	0.418	0.422		
				CI	vs. CC					
Loss Function					est p-values					
MSE	0.148	0.356	0.356	0.356	0.270	0.270	0.090	0.270		
MAE	0.127	0.494	0.494	0.494	0.417	0.417	0.017	0.417		
					test p-values					
MSE	0.198	0.669	0.677	0.682	0.490	0.482	0.245	0.489		
MAE	0.199	0.986	0.985	0.987	0.820	0.819	0.020	0.816		
\mathbf{H}_0			\mathbf{E}	ncompass	sing test p-va	alues				
CI encompasses CC	0.188	0.964	0.964	0.964	0.304	0.304	0.090	0.304		
	Spring Summer									
		Spr	ing			Sum	mer			
	MSE	Spr	MAE	MAPE	MSE	MSPE	MAE	MAPE		
Models	MSE		MAE		MSE ror statistics	MSPE		MAPE		
Models BI	MSE 5.238		MAE			MSPE		MAPE 5.186		
		MSPE	MAE Pred	diction er	ror statistics	MSPE s values	MAE			
BI	5.238	MSPE 54.940	MAE Prec 1.842	diction er	ror statistics	MSPE s values 46.259	MAE 1.710	5.186		
BI BC	5.238 5.136	MSPE 54.940 52.830	MAE Pred 1.842 1.905	diction er 5.963 6.170	ror statistics 5.103 5.072	MSPE s values 46.259 45.764	MAE 1.710 1.684	5.186 5.089		
BI BC CI	5.238 5.136 6.137	MSPE 54.940 52.830 65.836	MAE Pred 1.842 1.905 2.169	5.963 6.170 7.102 6.682	ror statistics 5.103 5.072 5.256	MSPE s values 46.259 45.764 47.856	1.710 1.684 2.034	5.186 5.089 6.201		
BI BC CI	5.238 5.136 6.137	MSPE 54.940 52.830 65.836	MAE Pred 1.842 1.905 2.169	5.963 6.170 7.102 6.682	5.103 5.072 5.256 5.072	MSPE s values 46.259 45.764 47.856 49.075	1.710 1.684 2.034	5.186 5.089 6.201		
BI BC CI CC Loss Function MSE	5.238 5.136 6.137 6.144	MSPE 54.940 52.830 65.836 64.316	MAE Pred 1.842 1.905 2.169 2.064	diction errors 5.963 6.170 7.102 6.682 BI D-M t 0.413	ror statistics	MSPE s values 46.259 45.764 47.856 49.075	1.710 1.684 2.034 1.845	5.186 5.089 6.201 5.817		
BI BC CI CC	5.238 5.136 6.137 6.144	MSPE 54.940 52.830 65.836 64.316	Pred 1.842 1.905 2.169 2.064	diction er 5.963 6.170 7.102 6.682 BI D-M t	ror statistics	MSPE s values 46.259 45.764 47.856 49.075	1.710 1.684 2.034 1.845	5.186 5.089 6.201 5.817		
BI BC CI CC Loss Function MSE	5.238 5.136 6.137 6.144	MSPE 54.940 52.830 65.836 64.316	MAE Pred 1.842 1.905 2.169 2.064	diction err 5.963 6.170 7.102 6.682 BI D-M t 0.413 0.229	ror statistics	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320	1.710 1.684 2.034 1.845	5.186 5.089 6.201 5.817		
BI BC CI CC Loss Function MSE	5.238 5.136 6.137 6.144	MSPE 54.940 52.830 65.836 64.316	MAE Pred 1.842 1.905 2.169 2.064	diction errors 5.963 6.170 7.102 6.682 BI D-M t 0.413 0.229 MCS t 0.822	ror statistics 5.103 5.072 5.256 5.072 I vs. BC est p-values 0.431 0.337	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320	1.710 1.684 2.034 1.845	5.186 5.089 6.201 5.817		
BI BC CI CC Loss Function MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229	MSPE 54.940 52.830 65.836 64.316 0.413 0.229	Pred 1.842 1.905 2.169 2.064 0.413 0.229	diction err 5.963 6.170 7.102 6.682 BI D-M t 0.413 0.229 MCS t	ror statistics 5.103 5.072 5.256 5.072 I vs. BC est p-values 0.431 0.337 test p-values	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320	1.710 1.684 2.034 1.845 0.424 0.320	5.186 5.089 6.201 5.817 0.424 0.320		
BI BC CI CC Loss Function MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822	D-M t 0.413 0.229 MCS t 0.822 0.479	ror statistics 5.103 5.072 5.256 5.072 4 vs. BC est p-values 0.431 0.337 test p-values 0.777	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861	1.710 1.684 2.034 1.845 0.424 0.320	5.186 5.089 6.201 5.817 0.424 0.320		
BI BC CI CC Loss Function MSE MAE MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493	BI D-M t 0.413 0.229 MCS t 0.822 0.479 CI D-M t	ror statistics	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644	1.710 1.684 2.034 1.845 0.424 0.320 0.863 0.647	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493	BI D-M t 0.413 0.229 MCS t 0.822 0.479 CI D-M t 0.496	ror statistics	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644	1.710 1.684 2.034 1.845 0.424 0.320 0.863 0.647	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651		
BI BC CI CC Loss Function MSE MAE MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493	BI D-M t 0.822 0.479 CI D-M t 0.496 0.231	ror statistics 5.103 5.072 5.256 5.072 I vs. BC est p-values 0.431 0.337 test p-values 0.777 0.709 I vs. CC est p-values 0.154 0.061	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644 0.292 0.040	1.710 1.684 2.034 1.845 0.424 0.320 0.863 0.647	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487 0.496 0.231	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493 0.496 0.231	BI D-M t 0.822 0.479 CI D-M t 0.496 0.231 MCS t	ror statistics 5.103 5.072 5.256 5.072 Evs. BC Lest p-values 0.431 0.337 Lest p-values 0.777 0.709 Evs. CC Lest p-values 0.154 0.061 Lest p-values test p-values	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644 0.292 0.040	0.424 0.320 0.863 0.647 0.009 0.009	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488 0.496 0.231	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487 0.496 0.231 0.992	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493 0.496 0.231 0.994	BI D-M t 0.413 0.229 MCS t 0.822 0.479 CI D-M t 0.496 0.231 MCS t 0.991	ror statistics 5.103 5.072 5.256 5.072 4 vs. BC est p-values 0.431 0.337 test p-values 0.777 0.709 4 vs. CC est p-values 0.154 0.061 test p-values 0.136	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644 0.292 0.040 0.581	0.424 0.320 0.863 0.647 0.009 0.001	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651 0.112 0.032		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487 0.496 0.231	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493 0.496 0.231	BI D-M t 0.822 0.479 CI D-M t 0.496 0.231 MCS t	ror statistics 5.103 5.072 5.256 5.072 Evs. BC Lest p-values 0.431 0.337 Lest p-values 0.777 0.709 Evs. CC Lest p-values 0.154 0.061 Lest p-values test p-values	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644 0.292 0.040	0.424 0.320 0.863 0.647 0.009 0.009	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651		
BI BC CI CC Loss Function MSE MAE MSE MAE Loss Function MSE MAE MSE MAE	5.238 5.136 6.137 6.144 0.413 0.229 0.826 0.488 0.496 0.231	MSPE 54.940 52.830 65.836 64.316 0.413 0.229 0.827 0.487 0.496 0.231 0.992	MAE Pred 1.842 1.905 2.169 2.064 0.413 0.229 0.822 0.493 0.496 0.231 0.994 0.465	D-M t 0.496 0.231 MCS t 0.991 0.467	ror statistics 5.103 5.072 5.256 5.072 4 vs. BC est p-values 0.431 0.337 test p-values 0.777 0.709 4 vs. CC est p-values 0.154 0.061 test p-values 0.136	MSPE s values 46.259 45.764 47.856 49.075 0.424 0.320 0.861 0.644 0.292 0.040 4.0.581 0.105	0.424 0.320 0.863 0.647 0.009 0.001	5.186 5.089 6.201 5.817 0.424 0.320 0.860 0.651 0.112 0.032		

Table 8: Summary of comparisons on the whole: percentage and, in brackets, number of cases. BI = best individual model (ex post); BC = best combination (ex post); CI = chosen (ex ante) individual model; CC = chosen (ex ante) combination.

Prediction error statistics values									
	Whole	Winter	Spring	Summer	Totals				
BC better than BI	80.00% (20)	80.00% (20)	55.00% (20)	90.00% (20)	76.25% (80)				
BI better than BC	20.00% (20)	20.00% (20)	45.00% (20)	10.00% (20)	23.75% (80)				
CC better than CI	85.00% (20)	70.00% (20)	80.00% (20)	80.00% (20)	78.75% (80)				
CI better than CC	15.00% (20)	30.00% (20)	20.00% (20)	20.00% (20)	21.25% (80)				
Significance of	of differences	with D-M te	st (MSE and	MAE loss fu	nctions)				
	Whole	Winter	Spring	Summer	Totals				
BC better than BI	17.50% (40)	0.00% (40)	10.00% (40)	7.50% (40)	8.75% (160)				
BI better than BC	0.00% (40)	0.00% (40)	0.00% (40)	0.00% (40)	0.00% (160)				
CC better than CI	50.00% (40)	17.50% (40)	50.00% (40)	15.00% (40)	33.13% (160)				
CI better than CC	2.50% (40)	0.00% (40)	0.00% (40)	2.50% (40)	1.25% (160)				
Significance of	of differences	with MCS te	st (MSE and	MAE loss fu	nctions)				
	Whole	Winter	Spring	Summer	Totals				
BC better than BI	12.50% (40)	0.00% (40)	2.50% (40)	0.00% (40)	3.75% (160)				
BI better than BC	0.00% (40)	0.00% (40)	0.00% (40)	0.00% (40)	0.00% (160)				
CC better than CI	47.50% (40)	15.00% (40)	37.50% (40)	12.50% (40)	28.13% (160)				
CI better than CC	2.50% (40)	0.00% (40)	0.00% (40)	0.00% (40)	0.63%~(160)				
		Encompassi	ng test						
	Whole	Winter	Spring	Summer	Totals				
CI encompasses CC	55.00% (20)	85.00% (20)	50.00% (20)	85.50% (20)	67.50% (80)				

chosen combination. $worst\ value\ obtained\ among\ the\ combinations,\ CI=\ value\ obtained\ with\ the\ chosen\ individual\ model,\ CC=\ value\ obtained\ with\ the$ $value\ obtained\ among\ all\ individual\ models\ and\ all\ combinations,\ WI=\ worst\ value\ obtained\ among\ the\ individual\ models,\ WC=$ **Table 9:** Differences of prediction error statistics values. Out-of-sample periods (125, 44, 41 and 44 data). $B = best \ possible \ statistics$

MSE MSPE MAE MAPE		MSE MSPE MAE MAPE		MSE MSPE MAE MAPE		MSE MSPE MAE MAPE		MSE MSPE MAE MAPE		Statistics	
7.234 31.520 0.438 1.222		80.792 168.198 1.311 3.863		552.949 297.548 3.115 4.363		15.514 133.427 0.945 2.659		$ \begin{array}{c} 2.101 \\ 42.985 \\ 0.450 \\ 1.779 \end{array} $		WI-B	
2.616 12.654 0.249 0.742		70.391 113.762 1.040 2.814		539.349 204.611 2.968 3.218		8.691 60.748 0.511 1.555		1.513 20.289 0.390 1.504		WC-B	Whole
2.112 11.559 0.153 0.442		60.226 168.198 1.311 3.863		0.000 173.932 2.329 2.719		5.022 65.349 0.802 0.187		$2.101 \\ 42.985 \\ 0.349 \\ 1.475$		CI-B	ole
0.578 8.527 0.152 0.416		58.504 53.813 0.458 2.250		196.696 28.665 0.576 0.082		5.279 30.452 0.259 0.890		0.621 4.897 0.217 0.932		СС-В	
167.503 348.45 2.779 4.550		552.739 578.899 6.358 7.606		162.911 169.797 2.062 3.998		78.218 64.458 1.568 1.735		26.101 132.430 1.338 2.810		WI-B	
88.346 133.603 1.515 2.409		282.417 211.887 3.167 3.277		114.464 158.353 1.941 3.768		46.751 31.624 1.060 1.174		$15.655 \\ 118.312 \\ 1.023 \\ 2.465$		WC-B	Wi
50.119 18.411 1.276 0.654		478.478 289.429 3.336 3.317		20.864 0.000 0.039 0.000		78.218 64.458 1.568 1.500		13.806 132.430 0.750 2.323		CI-B	Winter
45.355 21.695 0.417 0.688	Load Period 44	114.669 82.635 1.168 1.035	Load Period 38	22.699 30.452 0.848 1.373	Load Period 28	44.538 7.614 0.461 0.293	Load Period 18	12.458 82.570 0.377 0.792	Load Period 6	СС-В	
3.313 35.261 0.544 1.758	iod 44	27.375 192.962 1.691 4.937	iod 38	61.415 561.288 2.615 8.348	iod 28	8.462 103.256 1.051 3.640	iod 18	3.762 70.767 0.983 4.224	riod 6	WI-B	
1.493 17.380 0.381 1.276		20.026 120.513 1.166 3.256		34.114 274.211 1.439 4.365		5.035 63.95 0.581 2.044		3.012 58.402 0.820 3.571		WC-B	Spring
1.001 13.006 0.327 1.139		16.174 98.22 0.808 2.311		19.047 41.869 0.241 1.190		6.432 8.544 0.000 0.014		3.762 70.767 0.983 4.224		CI-B	ng
1.007 11.486 0.222 0.719		0.000 0.000 0.000 0.110		4.300 2.160 0.000 0.000		1.787 9.285 0.069 0.159		1.412 30.812 0.491 2.232		CC-B	
1.023 10.173 0.350 1.112		15.855 179.707 1.253 3.831		34.930 235.200 1.639 4.153		20.543 174.625 0.924 2.823		1.935 74.579 0.299 1.276		WI-B	
0.576 5.026 0.230 0.728		$11.770 \\ 139.799 \\ 0.798 \\ 2.693$		24.189 162.703 1.039 2.608		11.211 94.032 0.449 1.360		0.467 25.749 0.266 1.035		WC-B	Summer
0.184 2.093 0.350 1.112		11.749 75.726 0.913 2.496		26.696 176.773 1.282 3.319		5.096 7.348 0.106 0.318		0.608 9.881 0.290 1.149		CI-B	ner
0.000 3.311 0.161 0.728		7.527 75.664 0.705 2.294		24.189 63.983 1.039 2.608		5.812 2.087 0.115 0.375		0.344 7.232 0.000 0.000		CC-B	

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