

The ALPINE-ALMA [CII] survey

Obscured star formation rate density and main sequence of star-forming galaxies at $z > 4$

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ABSTRACT

Star formation rate (SFR) measurements at $z > 4$ have relied mostly on the rest-frame far-ultraviolet (FUV) observations. The corrections for dust attenuation based on the IRX- β relation are highly uncertain and are still debated in the literature. Hence, rest-frame far-infrared (FIR) observations are necessary to constrain the dust-obscured component of the SFR. In this paper, we exploit the rest-frame FIR continuum observations collected by the ALMA Large Program to INvestigate [CII] at Early times (ALPINE) to directly constrain the obscured SFR in galaxies at $4.4 < z < 5.9$. We used stacks of continuum images to measure average infrared luminosities taking both detected and undetected sources into account. Based on these measurements, we measured the position of the main sequence of star-forming galaxies and the specific SFR (sSFR) at $z \sim 4.5$ and $z \sim 5.5$. We find that the main sequence and sSFR do not significantly evolve between $z \sim 4.5$ and $z \sim 5.5$, as opposed to lower redshifts. We developed a method to derive the obscured SFR density (SFRD) using the stellar masses or FUV-magnitudes as a proxy of FIR fluxes measured on the stacks and combining them with the galaxy stellar mass functions and FUV luminosity functions from the literature. We obtain consistent results independent of the chosen proxy. We find that the obscured fraction of SFRD is decreasing with increasing redshift, but even at $z \sim 5.5$ it constitutes around 61% of the total SFRD.

Key words. galaxies: high-redshift – galaxies: evolution – galaxies: star formation – submillimeter: galaxies

1. Introduction

The evolution of the star formation rate density (SFRD) is one of the fundamental elements for properly describing the history of the Universe. This measure provides both information about the in situ growth of galaxies and an inference for the number of ionizing photons produced by galaxies, helping to place constraints on the history of reionization (e.g., Madau & Dickinson 2014; Bouwens et al. 2015a; Robertson et al. 2015; Dayal & Ferrara 2018).

The SFRD is generally measured by converting the dust-corrected far-ultraviolet (FUV) luminosity density of galaxies (see e.g., Madau & Dickinson 2014). Since a fraction of the FUV light emitted by massive short-lived stars can be absorbed by dust, when present, the total SFRD consists of two components: the $\text{SFRD}_{\text{FUV,uncorr}}$ measured from the rest-frame FUV luminosity density and the dust-hidden component SFRD_{IR} measured from the rest-frame infrared (IR) luminosity density.

The ratio between these two components changes with time and, hence, redshift. The obscured fraction, SFRD_{IR} , dominates at low redshifts; it is three to ten times higher than $\text{SFRD}_{\text{FUV,uncorr}}$ at $z < 3$ (e.g., Sanders et al. 2003; Takeuchi et al. 2003; Magnelli et al. 2011, 2013; Burgarella et al. 2013). At a higher redshift, the SFRD_{IR} is poorly constrained. However, since metals are produced by stars, the first galaxies should have very low dust content that is slightly enriched by only Popula-

tion III stars. Therefore, in these galaxies, $\text{SFRD}_{\text{FUV,uncorr}}$ should be well in excess of the dust-hidden fraction SFRD_{IR} . As star formation continues, stars internal to the galaxy begin to generate more dust. While the survival of dust grains is regulated by a series of constructive and destructive processes (Calura et al. 2017), the net result is an increase in the SFRD_{IR} in respect to the $\text{SFRD}_{\text{FUV,uncorr}}$. However, it is still unknown how fast the SFRD_{IR} increases at early times and when it overcomes $\text{SFRD}_{\text{FUV,uncorr}}$, mainly due to the lack of large, statistically-representative galaxy populations observed and selected both in the FUV and far-infrared (FIR) at high redshift (Dayal & Ferrara 2018).

Only a few attempts to constrain the SFRD_{IR} at high redshifts exist in literature and their results remain inconclusive. Gruppioni et al. (2013) measured SFRD_{IR} up to $z \sim 4$ using *Herschel* selected galaxies and found that the SFRD_{IR} decreases rapidly at $z > 3$. Wang et al. (2019a) extended these results to higher redshifts using the de-blended *Herschel*-SPIRE catalog. Their results show that the dust-obscured SFRD is comparable to estimates from the rest-frame UV at $z \sim 4$ –6. Rowan-Robinson et al. (2016) used the 500 μm sources from *Herschel* and found that the SFRD_{IR} at $z = 3$ –6 is even higher than the estimates from the rest-frame UV, although these results still have significant uncertainty. The measurements of Koprowski et al. (2017) using SCUBA-2 data at a redshift up to $z \sim 5$, on the other hand, suggest a very steep decrease in SFRD_{IR} (see discussion in Gruppioni & Pozzi 2019), so that SFRD_{IR}

[†] Deceased.

at $z > 4$ is even lower than $\text{SFRD}_{\text{FUV,uncorr}}$. This may be difficult to reconcile with the estimates of Rowan-Robinson et al. (2016) as well as with individual detections of very dusty galaxies at redshifts $z \approx 7$ (Strandet et al. 2017; Bowler et al. 2018), $z = 8.312$ (Tamura et al. 2019), and $z = 8.38$ (Laporte et al. 2017), where the IR contribution should be extremely low if the SFRD_{IR} continues to decrease rapidly with an increasing redshift. As the discoveries of individual, highly dust-obscured objects are not from volume-complete samples, it is difficult to determine whether such objects are common in the early Universe. However, the recent study using a volume-complete sample from the CO Luminosity Density at High Redshift (COLDz) survey by Riechers et al. (2020) resulted in the detection of three massive dusty starburst galaxies over $\sim 200\,000\text{ Mpc}^3$, indicating a high space density of such dusty objects at $z > 5$. Since this study was limited to luminous starburst galaxies, this is only a lower limit and less luminous galaxies can contribute even more to SFRD_{IR} . Previously mentioned studies based on measured IR luminosity functions (Gruppioni et al. 2013; Wang et al. 2019a; Rowan-Robinson et al. 2016; Koprowski et al. 2017) take this contribution into account; however, the observations at $z > 3.0$ rely on complex completeness corrections and difficult redshift identifications. In addition, they do not probe low luminosities, resulting in a poorly constrained faint end of the IR luminosity function. As such, conclusions related to the relative contribution of unobscured and obscured star formation at these epochs must be taken with caution and require confirmation through independent methods.

To overcome the difficulty of computing IR luminosity functions at $z > 4$, the measurements of the cosmic infrared background (CIB) produced by dusty galaxies can be used together with the modeling of dusty galaxy clustering, from which the SFRD_{IR} can then be derived. Maniyar et al. (2018) did this analysis using the CIB anisotropy measurements and their cross-correlation with cosmic microwave background lensing (see also Planck Collaboration XXX 2014). The results are consistent with a shallower evolution of the SFRD_{IR} at high redshifts compared to the results by Gruppioni et al. (2013) and Koprowski et al. (2017). At $z > 4$, the SFRD_{IR} does not drop below $\text{SFRD}_{\text{FUV,uncorr}}$ but approaches it up to $z \sim 6$.

Due to the difficulty in constraining the SFRD_{IR} at redshifts $z > 4$, the measurements of the total SFRD rely mostly on the rest-frame FUV part of the spectrum. To account for the obscured fraction, the relation between the IR excess (IRX) and the UV spectral slope (β) is often used (Meurer et al. 1999). However, stacking analysis (Fudamoto et al. 2017), as well as individual observations of high redshift galaxies with Atacama Large Millimeter/submillimeter Array (ALMA), reveal significant scatter of dust properties. Most galaxies show a deficit of FIR flux compared to local galaxies with the same β slopes (Capak et al. 2015; Bouwens et al. 2016; Fudamoto et al. 2020), which can be partially explained by higher dust temperatures (Faisst et al. 2017). The measurements of dust temperatures are scarce at high redshifts but they show that dust temperatures are, indeed, higher than in local galaxies (30–43 K at $z \sim 5$, Faisst et al. 2020). Since measurements of the SFRs at high redshifts are based on dust corrections coming from the IRX- β relation, the scatter in the relation induces uncertainties on these measurements. For this reason, observing rest-frame FIR continuum coming from galaxies selected in UV is important to independently constrain the IR luminosity density produced by these galaxies.

It is well established in the literature that star-forming galaxies form a so-called main sequence, a relationship between the amount of stellar mass in situ (M_*) and the star formation rate (SFR, Noeske et al. 2007; Daddi et al. 2007; Whitaker et al.

2012; Speagle et al. 2014; Salmon et al. 2015; Tasca et al. 2015; Schreiber et al. 2015; Tomczak et al. 2016; Santini et al. 2017; Pearson et al. 2018; Khusanova et al. 2020). However, the measurements of the SFRs of individual galaxies at $z > 4$ suffer from the uncertainty of the IRX- β relation and/or the dust temperature of the galaxies. Hence, a lower number of galaxies is detected in the rest-frame FIR than expected assuming local IRX- β relation (e.g., Capak et al. 2015; Bouwens et al. 2016). Besides, getting a wide volume in the rest-frame FIR at $z > 4$ is expensive observationally. Therefore, the constraints on the main sequence of galaxies are limited and are mostly based on the rest-frame FUV data.

Only a few attempts have been made to constrain the main sequence using submillimeter observations, mainly using data from *Herschel* (Schreiber et al. 2015; Pearson et al. 2018). At $z > 4$, however, the measurements are limited by confusion noise (Nguyen et al. 2010), which makes it difficult to observe individual sources without careful and well-informed de-blending schemes. Therefore, these works primarily are limited to only the high mass end of the main sequence ($\log(M_*/M_\odot) > 10.5$). Star-forming galaxies with such high masses are rather rare, and it remains unclear if the slope of the main sequence remains the same over the whole range of masses.

The main sequence evolution with redshift is linked to the sSFR evolution defined as SFR/M_* , although the sSFR evolution can vary depending on the mass if the slope of the main sequence is not unity, as claimed in several studies (e.g., Salmon et al. 2015; Schreiber et al. 2015; Tasca et al. 2015; Khusanova et al. 2020). In that case, the measurements from UV selected samples, which probe galaxies with lower stellar masses ($\log(M_*/M_\odot) \lesssim 10$) are not comparable with FIR samples probing higher stellar masses (Schreiber et al. 2015). The sSFR constraints at high redshifts are inconclusive: while many studies find a shallower evolution at high redshifts (Bouwens et al. 2012; González et al. 2014; Tasca et al. 2015; Faisst et al. 2016; Santini et al. 2017), some find higher sSFR, consistent with steeper evolution, as at lower redshifts (Stark et al. 2013; de Barros et al. 2014).

The ALMA Large Program to INvestigate [CII] at Early times (ALPINE) was designed with a goal of measuring the dust-hidden SFR in galaxies at $z > 4$ from a representative UV selected sample (B  thermin et al. 2020; Le F  vre et al. 2020; Faisst et al. 2020). In this paper, we use a large sample of 118 galaxies observed in the rest-frame FIR with ALMA to determine the SFRD_{IR} at $z > 4$ from ALPINE. We also determine their average and individual SFRs and constrain the main sequence over the stellar mass range $9 \leq \log(M_*/M_\odot) \leq 11$. Our goal is to estimate SFRs and SFRD without relying on the IRX- β relation and by directly measuring the total IR luminosities. We present the ALPINE data in Sect. 2. In Sect. 3, we describe the stacking code and the methods to measure the SFRD. In Sect. 4, we present and discuss our SFRD measurements. Section 5 is dedicated to a discussion about the main sequence and the sSFR evolution with redshift. In Sect. 6 we summarize our results.

Throughout the paper, we use a Λ CDM cosmology with $\Omega_\Lambda = 0.70$, $\Omega_m = 0.30$ and $h = 0.7$. All magnitudes are given in the AB system. We assume a Chabrier (2003) initial mass function (IMF) to convert luminosities to SFRs. We refer to absolute magnitude at 1600 \AA by M_{FUV} and total luminosity between 8 and $1000\text{ }\mu\text{m}$ by L_{IR} .

2. Data

We use the data from ALPINE, a survey designed to observe [CII] emission and the rest-frame FIR continuum of a

representative sample of star-forming galaxies in the redshift range $4.4 < z < 5.8$ with a gap at redshifts $4.65 < z < 5.05$, where the [CII] 158 μm emission line falls into a window of low atmospheric transmission (Le Fèvre et al. 2020). The galaxies are selected by the following criteria: UV-luminosity is above $0.6L^*$ or $M_{\text{FUV}} < -20.2$ (it is important to note that this selection is missing faint UV sources, the consequences of that are discussed below and in Sect. 4.3.3) and have secure spectroscopic redshifts from the rest-frame UV spectra. The secure spectroscopic redshift ensures that [CII], if present, falls within the relatively narrow observed ALMA bandpass. The redshifts are taken from two large spectroscopic surveys: VIMOS Ultra-Deep Survey (VUDS, Le Fèvre et al. 2015; Tasca et al. 2017) and DEep Imaging Multi-Object Spectrograph (DEIMOS, Faber et al. 2003) 10 K Spectroscopic Survey (Hasinger et al. 2018). The targets for these spectroscopic surveys are selected based on their broad and narrow band photometry. More on the selection can be read in Le Fèvre et al. (2020).

The advantage of the ALPINE selection is that it covers a wide range of stellar masses ($9 \lesssim \log(M_*/M_\odot) \lesssim 11$) and SFRs derived from the rest-frame FUV with Spectral Energy Distribution (SED) fitting ($1 \lesssim \log(\text{SFR}[M_\odot \text{ yr}^{-1}]) \lesssim 3$, Faisst et al. 2020). The targets are “normal” star-forming galaxies and, based on observations in the rest-frame FUV, populate the main sequence. We use stacking of both detections and nondetections to derive the average properties of the sample (see Sect. 3). In this way, we avoid bias toward rare, bright starburst galaxies, compared to other observations of samples selected in the rest-frame FIR at these redshifts. Since the targets are selected from well-studied fields, they are imaged with both space and ground-based instruments (Grogin et al. 2011; Koekemoer et al. 2011; Laigle et al. 2016; Skelton et al. 2014).

However, the ALPINE selection of targets has two caveats. First of all, since the selection is based on UV-properties of galaxies, the objects which are faint in UV are missed. Hence, their contribution is not taken into account by our SFRD measurements and blind surveys are still necessary to make a proper estimate of contribution from such objects. This caveat is discussed in more detail in Sect. 4.3.3. The second caveat is the bias toward higher UV-luminosities in the low mass bins. In Sect. 3.2.2, we discuss how we deal with this caveat in deriving the SFRD.

In total, 118 galaxies were observed in the period from May 2018 to January 2019 (see Béthermin et al. 2020). The ALMA data were calibrated with the standard ALMA pipeline. The Common Astronomy Software Applications (CASA) software was used for the data reduction (McMullin et al. 2007). To produce continuum maps, we excluded all the channels that correspond to the position of the [CII] line. In case of nondetections of the [CII] emission, we used spectroscopic redshifts from VUDS or DEIMOS 10K and excluded data within 500 km s^{-1} around the expected position of [CII] line. For galaxies with detected [CII] emission, we manually defined the window around the detected emission line. We then produced continuum maps, using the task `tclean`. We used natural weighting to maximize the signal-to-noise (S/N). More detail on data reduction can be found in Béthermin et al. (2020).

The survey was optimized to detect [CII] line emission. Therefore, the expected S/N for the rest-frame FIR continuum varies in the range from 0.5 to 3 for most targets based on the SED models of Béthermin et al. (2017). We reached a sensitivity of $50 \mu\text{Jy beam}^{-1}$ at $4.4 < z < 4.6$ and $28 \mu\text{Jy beam}^{-1}$ at $5.1 < z < 5.8$. We found that 95% purity is reached with a $S/N = 3.5$ cut for targeted galaxies. Only 23 out of 118 (19%) of the ALPINE targets are detected with such significance.

Table 1. Model parameters for SED fitting.

Input parameters	
IMF	Chabrier (2003)
SFH	Exponentially declining ($\tau = 0.1, 0.3, 1.0, 3.0 \text{ Gyr}$) Delayed exponential ($\tau = 0.1, 0.5, 1.0, 3.0 \text{ Gyr}$) Constant
Attenuation law	Calzetti starburst
$E(B - V)_s$	0, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35, 0.4, 0.45, 0.5
Metallicities	$0.2 Z_\odot$ and $1.0 Z_\odot$

However, given the known positions of the targets, we can extract the average continuum flux of nondetected galaxies using stacking, as described in Sect. 3.1.

The galaxies in ALPINE were chosen in the two well-studied fields, Cosmic Evolution Survey (COSMOS, 89% of targets, Scoville et al. 2007) and Extended *Chandra* Deep Field-South Survey (ECDFS, 11% of targets, Giacomoni et al. 2002) that is covered by CANDELS (Koekemoer et al. 2011; Grogin et al. 2011). The photometry from the public COSMOS catalog (Laigle et al. 2016) was used for targets in the COSMOS field, and the 3D-HST catalog (Skelton et al. 2014) was used for the ECDFS. Faisst et al. (2020) analyzed the multiwavelength ancillary data in both fields and derived the physical properties of galaxies using SED fitting at fixed spectroscopic redshift (stellar masses, SFRs, rest-frame FUV luminosities, etc.).

The SED fitting was performed with the LePhare package (Arnouts et al. 1999; Ilbert et al. 2006) as well as a modified version of the HyperZ code (Bolzonella et al. 2000), using Bruzual & Charlot (2003) models. The model parameters are outlined in Table 1. The fitting was performed in flux density space and emission lines were included. The two different codes were used to analyze the systematic uncertainties introduced by the χ^2 minimization algorithms and the treatment of emission lines (see Faisst et al. 2020). The absolute UV magnitudes from the two codes agree, while the stellar masses and SFRs have systematic uncertainties of ~ 0.3 dex. Only four galaxies were found to have significantly different (larger than systematic uncertainties) stellar masses and SFRs due to contaminated *Spitzer* photometry. The derived physical parameters were compared to previous results for the galaxies in COSMOS field derived with photometric redshifts and we found that they agree. Here and in other ALPINE papers, we use the parameters derived by the SED fitting derived with LePhare. More details about the SED fitting of ALPINE galaxies and ancillary data can be found in Faisst et al. (2020).

3. Methods

3.1. Stacking of the rest-frame FIR continuum images

As mentioned above, for $\sim 81\%$ of the ALPINE targets, the observed continuum flux cannot be measured since it falls below the 3.5σ limits. Therefore, we use stacking to measure the average flux of galaxies with similar physical properties. We use all the targeted galaxies including both detections and nondetections, since our goal is to get the average flux of the whole population of galaxies in each bin.

Here we use the mean stacks of continuum images. We only use the targeted galaxies and their UV-positions for alignment. Since the targets are not perfectly aligned on stacks due to uncertainties in astrometry or real physical offsets, the flux is

measured using an aperture of 3 arcsec diameter. Béthermin et al. (2020) has tested three other methods of continuum flux measurements in addition to aperture photometry: Gaussian fitting on a continuum map and on the *UV* plane, and peak flux. They all were proven to be consistent with each other, except for the peak flux. This is because the sources are not point-like. However, on stacks only aperture photometry can be used, since we cannot align the nondetected sources and their sizes can vary from target to target. Therefore, their mean profile is not Gaussian. The aperture photometry, on the other hand, makes it possible to measure the flux without any assumption on the profile shape. Since the beam sizes in ALPINE do not exceed 1.6 arcsec, the 3 arcsec aperture is large enough to include all the flux from the targets even if the sources are significantly extended. Fujimoto et al. (2020) examined the radial surface brightness profiles of ALPINE targets and found that the sources are compact in the rest-frame FIR.

We use bootstrapping analysis to ensure the robustness of the measurements of the flux and to estimate the uncertainties coming from both the noise and the sample variance. Each stack is produced from a set of continuum images. To measure the average flux and its uncertainty, we randomly draw a new sample of images without withdrawal from the initial set and produce a new stack image, from which the continuum flux is remeasured. We repeat the procedure 1000 times and find the average and standard deviation of the measurement – σ_{boot} .

We also measure the flux in the field with the same aperture at each step. We mask the positions of the serendipitously detected objects and the center beforehand, to ensure that the flux measured in the field is not contaminated. The apertures are then placed at random positions, away from serendipitous sources. The variance of the field flux is an estimate of the photometric noise on the stacked image and is on average $\sigma_{\text{phot}} = 50 \mu\text{Jy}$ for the typical number of stacked images (eight). The average flux in the field is compatible with zero as expected ($F_{\text{field}} = 0.1 \pm 50.0 \mu\text{Jy}$).

As discussed in Béthermin et al. (2012), the bootstrap uncertainty σ_{boot} and the photometric noise σ_{phot} are related as:

$$\sigma_{\text{boot}} = \frac{\sqrt{\sigma_{\text{phot}}^2 + \sigma_{\text{pop}}^2}}{\sqrt{N_{\text{stack}}}}, \quad (1)$$

where N_{stack} is the number of images in the stack and σ_{pop} is the intrinsic population variance. The uncertainties derived using the bootstrap method are thus including both the photometric noise and the sample variance coming from the finite size and the possible large heterogeneity of the stacked samples.

In order to test reliability of the flux measurement on the stacks, we generated a number of fake sources on the images avoiding the center with fluxes drawn from a Gaussian distribution with a known mean F_{in} and variance σ_{in} . The sources are Gaussian and their FWHM were allowed to vary from 0.8 to 1.6 arcsec (as the beam sizes in ALPINE, Béthermin et al. 2020). We used the procedure described above to stack images with the fake sources, but in order to simulate position uncertainties of real targets, we added random offsets sampled from a Gaussian with $\sigma = 0.12$ arcsec (as the average astrometric offset of ALPINE targets, Faisst et al. 2020). Then we measured the average flux F_{out} and the bootstrap uncertainty σ_{out} . We performed the procedure 250 times, varying the F_{in} flux value in the range 10–180 μJy or ~ 0.25 – $3.5\sigma_{\text{phot}}$ and the number of images from six to 13 (as we used later for the stacks).

Figure 1 shows the distribution of $\Delta F/\sigma_{\text{out}} = (F_{\text{out}} - F_{\text{in}})/\sigma_{\text{out}}$. The mean of the distribution is -0.03 and the

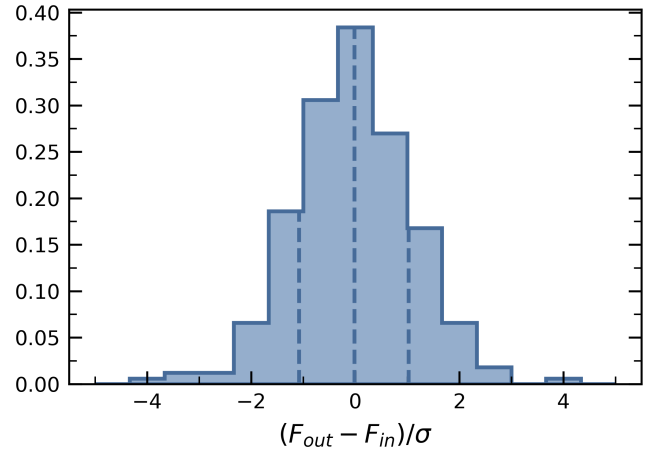


Fig. 1. Comparison of injected and recovered fluxes from stacking. The vertical dashed lines correspond to 16th, 50th and 84th percentiles of the distribution (-1.08 , -0.02 , 1.03).

standard deviation is 1.13. The mean is compatible with zero. The standard deviation of the distribution can be reduced to ~ 1 , if we limit the analysis to stacks with a high number of images (>20), however, this is not feasible given the number of objects in the sample. We, therefore, divide the sample in smaller bins and make stacks with the number of objects in range from six to 13 to be able to constrain the $L_{\text{IR}} - M_*$ or $L_{\text{IR}} - M_{\text{FUV}}$ relation.

We cannot assess the real shape of the L_{IR} distribution but the population variance can tell us how well the average L_{IR} of a given selection is constrained. For instance, if the distribution is bimodal, our bootstrap procedure will measure a high population variance. These uncertainties taking into account both the population variance and the noise are propagated to the other derived quantities.

In conclusion, the average fluxes on stacks are well recovered within the error bars if the sources are not significantly extended or offset. This is the case for the detected targets (Béthermin et al. 2020). Therefore, stacking can be safely used to recover the average continuum fluxes.

3.2. SFRD measurement: Method description

The total SFRD can be defined as (see e.g., Madau & Dickinson 2014):

$$\text{SFRD} = \text{SFRD}_{\text{FUV,uncorr}} + \text{SFRD}_{\text{IR}} = \kappa_{\text{FUV}}\rho_{\text{FUV}} + \kappa_{\text{IR}}\rho_{\text{IR}}, \quad (2)$$

where $\text{SFRD}_{\text{FUV,uncorr}}$ is derived from the FUV luminosity density (ρ_{FUV}) not corrected for dust attenuation, and SFRD_{IR} is derived from the IR luminosity density (ρ_{IR}). The conversion factors are $\kappa_{\text{FUV}} = 1.5 * 10^{-10} M_{\odot} \text{yr}^{-1} L_{\odot}^{-1}$ and $\kappa_{\text{IR}} = 10^{-10} M_{\odot} \text{yr}^{-1} L_{\odot}^{-1}$ for Chabrier (2003) IMF (Kennicutt 1998).

3.2.1. Measuring IR luminosity density

Since ALPINE is not a volume-limited sample, it is rather difficult to determine the IR luminosity function from the target sample (see Gruppioni et al. 2020, for IR luminosity function measurement based on nontarget galaxies found in ALPINE). We use, therefore, a different approach to obtain the IR luminosity density, which can then be converted to the SFRD_{IR} . The method is based on using some physical property as a proxy of

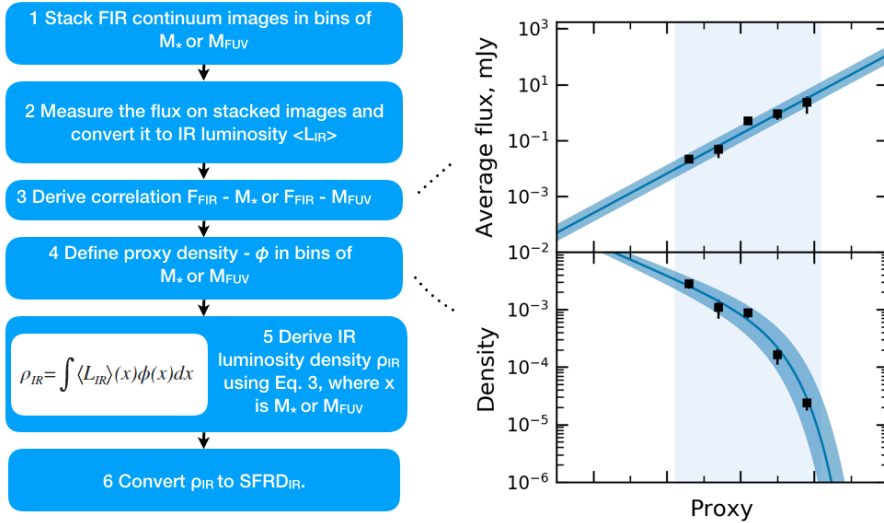


Fig. 2. Illustration of the method used to determine the SFRD_{IR} . *Left panel:* steps performed. *Right panel:* arbitrary proxy density function (UVLF or GSMF) and a power law relation between the property used as a proxy and the FIR flux. The black squares represent measured values and the solid line the fit with uncertainties represented by a shaded region. The vertical shaded regions show the proxy range, in which the data is available for both the power law relation derived from ALPINE and the proxy density function.

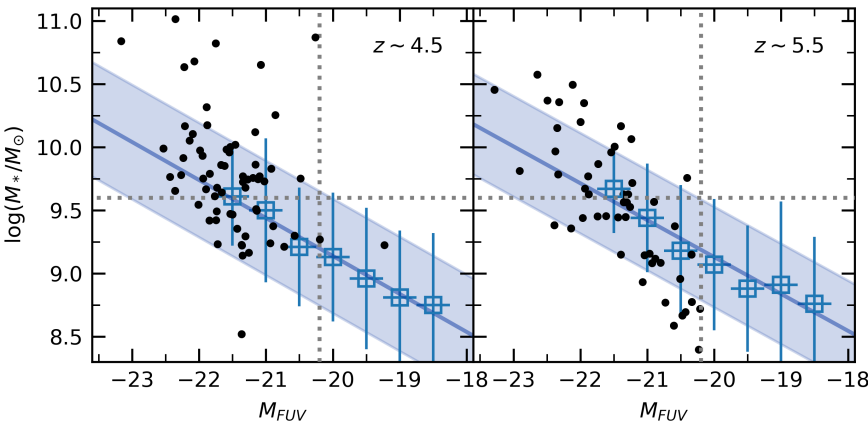


Fig. 3. Stellar mass versus FUV magnitude. The black circles are ALPINE targets as measured by Faisst et al. (2020). The open squares are measurements from Salmon et al. (2015). The solid blue line is the fit to the measurements by Salmon et al. (2015) and the shaded areas are 1σ uncertainties. The vertical dotted line shows the FUV luminosity cut used in selecting galaxies. The vertical dotted lines show the mass limits below which the flux measurements are considered to be upper limits. *Left panel:* $z \sim 4.5$ redshift bin and *right panel:* $z \sim 5.5$ bin.

the IR luminosity – L_{IR} and convolving the volume density distribution of this proxy with the mean LIR-proxy relation as:

$$\rho_{\text{IR}} = \int \langle L_{\text{IR}} \rangle(x) \phi(x) dx, \quad (3)$$

where x is a proxy (M_{FUV} or M_* , see Sect. 3.2.2), $\langle L_{\text{IR}} \rangle$ is the total IR luminosity and $\phi(x)$ is either the FUV luminosity function (UVLF) or the galaxy stellar mass function (GSMF). The total IR luminosity is derived from the SED templates scaled to the $158\mu\text{m}$ flux measured on stacks and then integrated from 8 to $1000\mu\text{m}$. We use average conversion factors $\langle f_{\text{temp}, z \sim 4.5} \rangle = 0.13 \pm 0.02$ and $\langle f_{\text{temp}, z \sim 5.5} \rangle = 0.12 \pm 0.03$ derived from a set of templates from the literature, which are consistent with the stacked *Herschel* data (see Appendix A for more detail on the templates and conversion factors). The volume density distribution can be derived from the literature measurements of the proxy density functions (UVLF or GSMF in our case). A summary of the method is presented in Fig. 2.

3.2.2. The choice of proxy

The method described above relies on the assumption that there is a relation between the proxy and the IR luminosity. To first order, this is true for stellar masses (M_* , we refer to “stellar mass” as “mass” hereafter) of star-forming galaxies, which sit on the main sequence. Their SFR increases with the mass (Whitaker et al. 2012, 2014; Tasca et al. 2015; Salmon et al. 2015; Santini

et al. 2017; Pearson et al. 2018; Khusanova et al. 2020). While it is still unclear what fraction of SFR is hidden by dust, we expect that there is a relation between the masses and the IR dust emission (this is further discussed in Sect. 5 dedicated to the main sequence). Also the FUV-magnitudes are linked to SFR to first order. If we assume that more star-forming galaxies have higher IR luminosities, the FUV-magnitudes should correlate with the L_{IR} . Each proxy, however, has its own sources of uncertainty, which are discussed below. Therefore, we use both of them and compare the results.

The accuracy of the mass is limited, since it is derived from SED fitting and it is, therefore, model-dependent. The caveat in using the mass as a proxy is the fact that the sample of galaxies in ALPINE is selected to have FUV luminosities above $0.6L^*$. Hence, the galaxies selected at lower masses are not representative of typical galaxies at these masses, since they are biased toward higher UV luminosities at fixed mass. We show in Fig. 3 the median values of the $M_* - M_{\text{FUV}}$ relation from Salmon et al. (2015) and the fit of this relation. This relation agrees well with the M_* and M_{FUV} measurements for ALPINE targets. We find the mass at which the 1σ envelope around the best fit crosses the FUV luminosity selection limit, where σ is the scatter around the fit. As shown in Fig. 3, the mass limit is $\log M_{\text{lim}}/M_{\odot} = 9.6$ at both redshifts. Below this limit we are likely to miss galaxies with faint FUV magnitudes, biasing SFR toward higher values.

The FUV magnitudes are not affected by this bias. Since the spectroscopic redshifts are known, they are not model-dependent and can be derived with high accuracy given well-measured

photometry (Faisst et al. 2020). We do not correct the derived FUV magnitudes for dust attenuation in order to keep them model-independent. However, the more dust is in the galaxy, the more FUV radiation is absorbed for a given SFR/IMF combination. Therefore, even if majority of faint in FUV galaxies have low dust content, some dust rich galaxies can contaminate FUV faint bins. In that case, the population will be heterogeneous in each bin and the relation may have larger scatter. This will make it more difficult to constrain the relation between FUV magnitude and IR luminosity. We determine the population variance with the bootstrapping procedure described in Sect. 3.1 (see Eq. (1)). The impact of the population variance is then propagated to the uncertainties on the SFRD. However, if the population variance is intrinsically too large, the use of FUV magnitudes as a proxy can be challenging to analyze small samples.

3.2.3. Integration limits

ALPINE probes only a range of masses ($9 \lesssim \log(M_*/M_\odot) \lesssim 11$) or FUV-magnitudes ($-19 \lesssim \log(M_*/M_\odot) \lesssim -23$), used as a proxy (this range is schematically shown as shaded region in Fig. 2). In this range, we have measurements of the rest-frame FIR flux directly from the stacks of ALPINE images. The proxy density is known from observations. The SFRD_{IR} measured from integration in this range is, hence, the most robust lower limit of the dust-hidden fraction of SFRD. However, more IR luminosity can be contained in FUV faint or low mass galaxies. While these galaxies are expected to have low dust content, they can still affect the results due to their high density in the Universe. Galaxies with high masses or bright in FUV are rare, but they also contribute to the total SFRD budget. Therefore, we need to extrapolate the observed L_{IR} -proxy relation and the proxy density functions to obtain the estimate of the total SFRD_{IR}.

We determine, first, the lower limit (SFRD_{IR,min}) by integrating the Eq. (3) within the observed in ALPINE mass or FUV-magnitude range. Then, for the extrapolation, we use the integration limits corresponding to $0.03L^*$ ¹ and $100L^*$. These are $M_{\text{FUV}} = -17$ and $M_{\text{FUV}} = -26$, respectively. In order to define integration limits for masses, we convert these limits to SFRs. Then we use the relation between SFR and mass from the main sequence fit in Khusanova et al. (2020) to find the corresponding masses: $\log(M_*/M_\odot) = 6.0$ for the lower limit and $\log(M_*/M_\odot) = 12.4$ for the upper limit. With these limits, we can make a meaningful comparison between the SFRD_{FUV,uncorr} derived in the literature from UVLFs and the SFRD_{IR} measured here. We note that even after extrapolation, we are missing galaxies with high IR luminosity, because some of them are too faint in the rest-frame FUV to be detected in current photometric surveys (e.g., Caputi et al. 2014; Franco et al. 2018; Williams et al. 2019; Wang et al. 2019b; Gruppioni et al. 2020). Their contribution is discussed in the Sect. 4.3.3.

4. SFRD measurement results

4.1. Proxy number density

First, we need to define the proxy number density: UVLF or GSMF. Their measurements are widely available in the literature (e.g., Bouwens et al. 2015b; Finkelstein et al. 2015; Ono et al. 2018; Pelló et al. 2018; Khusanova et al. 2020; Song et al. 2016; Davidzon et al. 2017; Wright et al. 2018) but are still affected

¹ This is a commonly used value in the literature (e.g., Bouwens et al. 2015b; Madau & Dickinson 2014; Khusanova et al. 2020).

by many uncertainties. In particular, the faint and low mass end slopes are still not well constrained. Another uncertainty is the shape of the UVLF. While most authors assume the Schechter function form, some recent works find that at high redshift the double power law (DPL) is preferable form (Bowler et al. 2015; Ono et al. 2018; Khusanova et al. 2020). We do not favor any particular UVLF or GSMF, but use several of them to show how the uncertainties on their parameters and functional form propagate into our SFRD estimates.

For the UVLF, we use the Bouwens et al. (2015b); Finkelstein et al. (2015), Ono et al. (2018), Pelló et al. (2018) and Khusanova et al. (2020) results. The Bouwens et al. (2015b), Finkelstein et al. (2015) and Pelló et al. (2018) UVLFs are based on large samples with photometric redshifts. The UVLF is represented with a Schechter function. Ono et al. (2018) uses a dropout selection partially confirmed by spectroscopic redshifts and Khusanova et al. (2020) uses the sample with spectroscopic redshifts. These studies probe the bright end of the UVLF and find a DPL form of UVLF.

We use Song et al. (2016), Davidzon et al. (2017) and Wright et al. (2018) measurements of GSMFs. Song et al. (2016) GSMFs are based on samples selected from CANDELS-GOODS field. Davidzon et al. (2017) uses photometric selection of galaxies in COSMOS field, and Wright et al. (2018) uses a joint analysis of GAMA, COSMOS, and 3D-HST data. We note that the physical parameters derived for ALPINE galaxies in COSMOS field were compared with the COSMOS15 catalog and are consistent (see Faisst et al. 2020). Therefore, the uncertainties of mass measurements, which are more affected by the choice of the IMF and star formation history (SFH) in SED fitting compared to FUV magnitudes, should not have impact on our results, when we combine the COSMOS-based GSMF with L_{IR} -mass relation from ALPINE.

4.2. Infrared luminosity as a function of proxy

As discussed in Sect. 3.2.2, we used two proxies in this work: masses and FUV magnitudes derived using the SED fitting as described in detail in Faisst et al. (2020). The bin sizes were chosen to be small enough to reduce the heterogeneity of the underlying population but to include enough galaxies (6-13) in the bin to have robust average flux measurements. As was discussed in Sect. 3.1, even faint fluxes on the stacks give us information on the average flux of the underlying population of galaxies. Therefore, we use $3.5\sigma_{\text{phot}}$ upper limits only when the measured fluxes of the stack have negative values. In such cases, we use conservative upper limits $0+3.5\sigma_{\text{phot}}$. In all the remaining cases, we use the average flux measured with bootstrapping (the S/N in these cases is $>0.5\sigma_{\text{phot}}$). When stacking by mass bins, we consider the results as upper limits in bins below $\log M_{\text{lim}}/M_\odot = 9.6$, for the reasons discussed in Sect. 3.2.2 (bias toward higher SFR because of the FUV selection of ALPINE). The upper limits in those cases are the sum of the flux measured on stacks and 3σ .

We converted the average rest-frame $158\mu\text{m}$ fluxes to $\langle L_{\text{IR}} \rangle$ and found the $\langle L_{\text{IR}} \rangle$ -proxy relation. We show the resulting relations in Fig. 4. The $\langle L_{\text{IR}} \rangle$ is clearly well correlated with both proxies. We fit this relation with a power law using the MCMC method with emcee package in python and checking at each step that the fit does not go above upper limits. The results are shown in Fig. 4. The slope is well constrained, and the normalization lies within the error bars. We use the MCMC chains later when deriving the SFRD_{IR}. This allows us to derive the uncertainty of the SFRD_{IR} measurements, which relies on the precision of our $\langle L_{\text{IR}} \rangle$ -proxy relation.

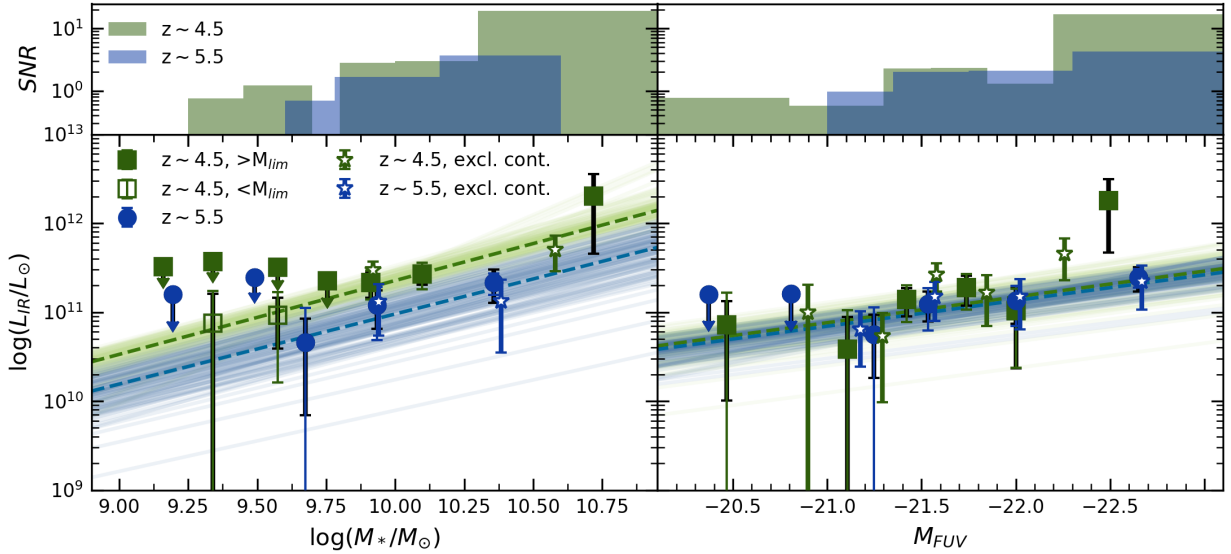


Fig. 4. Average infrared luminosity versus proxy (stellar mass as a proxy on the *left panel* and FUV magnitude on the *right*). The green squares and blue circles are the average IR luminosities on the stacks at $z \sim 4.5$ and $z \sim 5.5$, respectively. The black error bars show the population variance (σ_{pop}), the colored error bars show the photometric noise (σ_{phot} , see Eq. (1), Sect. 3.1). The open squares are the flux measurements on stacks below mass limit M_{lim} . The stars are the results on stacks excluding the galaxies with signs of possible contamination by a close companion. The green and blue dashed lines are the best fits of the relation and the thin lines of corresponding color are the MCMC chain realizations of the fit. *Top panels*: S/N on each stack.

Faisst et al. (2020) identified galaxies with signs of possible contamination of photometry by close companions (based on optical HST and ground-based images). Excluding them lowers the number of galaxies which can be used for stacking, but does not affect the resulting power law relation between the proxy and $\langle L_{\text{IR}} \rangle$. We show the results obtained from the stacks after excluding the galaxies with signs of contamination in Fig. 4. Since this new sample contains less objects, we had to adjust the bins, but the data points agree with the power-law relation found for the full sample.

In Fig. 4, we show the photometric errors and population variance computed as described in Sect. 3 (see Eq. (1)) and S/N in each stack. The population variance at $z \sim 4.5$ is ~ 0.91 dex on average. At $z \sim 5.5$, it is ~ 0.47 dex, almost two times lower. As discussed in Sect. 3.2.2, if the underlying population is heterogeneous, the scatter of its FIR properties will be large. This is what we observe at $z \sim 4.5$. This makes the $L_{\text{IR}} - M_{\text{FUV}}$ relation particularly difficult to constrain at $z \sim 4.5$.

We note that the two points below M_{lim} , which were excluded from the fit due to a possible bias (see Sect. 3.2.2), are in a very good agreement with the power law fit to the points above M_{lim} . Therefore, we trust these two points and use them later, when we derive the main sequence.

Interestingly, we observe a stronger evolution with redshift of the $L_{\text{IR}} - M_*$ relation than the $L_{\text{IR}} - M_{\text{FUV}}$ relation. As the redshift decreases, the L_{IR} on average increases for galaxies with the same mass, which means the dust attenuation increases in these galaxies.

4.3. Infrared contribution to SFRD

We present the results of our measurements of SFRD_{IR} in Figs. 5 and 6 for redshifts $z \sim 4.5$ and $z \sim 5.5$ respectively, and in Table 2. Although the results depend on the choice of the proxy density parameters, in most cases they agree with each other within the error bars. The choice of the proxy plays a role in the constraining power of our method. At redshift $z \sim 4.5$, the

population variance in FUV bins is larger as we noted before. Hence, although we find a fit to the measured points, these constraints should be interpreted with caution. At $z \sim 5.5$, on the contrary, we have weaker constraints when using the mass as a proxy. Due to the bias toward higher FUV magnitudes in low mass bins, we had to exclude them from the fitting of the $L_{\text{IR}} - M_*$ relation. The remaining points have larger uncertainties at $z \sim 5.5$. Hence, the fit of the $L_{\text{IR}} - M_*$ relation has larger uncertainties, which propagate into uncertainties of the SFRD estimates.

The measurements obtained with FUV as well as M_* as a proxy agree well with each other within the errors in both redshift bins. The fact that the measurements obtained with different proxies are consistent with each other gives us certainty on robustness of our constraints of the IR contribution to the SFRD. In the next section, we discuss our measurements in the context of the SFRD evolution.

4.3.1. Lower limit of the obscured SFRD

First, we obtained the lower limit on SFRD_{IR} . For that, we integrated the $\langle L_{\text{IR}} \rangle$ -proxy relation with the proxy density function in the range where both of them are known from the observations. Hence, this estimate is free from the uncertainties induced by extrapolations. The integration limits are $8.35 \leq \log(M_*/M_{\odot}) \leq 10.5$ for masses and $-23.3 \leq M_{\text{FUV}} \leq -20.0$ for FUV magnitudes.

As described in Sect. 4.1 and 4.2, each power law function describing L_{IR} -proxy relation is fit with the MCMC (see Eq. (3)). To derive the SFRD_{IR} and its uncertainty, we use the MCMC chains of fit parameters to produce a resulting SFRD_{IR} chain. In this way, we obtain a probability distribution function (PDF) of SFRD_{IR} , which is a normalized distribution of individual SFRD_{IR} measurements at each step. These PDFs are shown in the left panel of Figs. 5 and 6 for both proxies. Depending on the choice of the proxy density function, the PDFs differ but remain consistent within the error bars for each proxy. In Fig. 7,

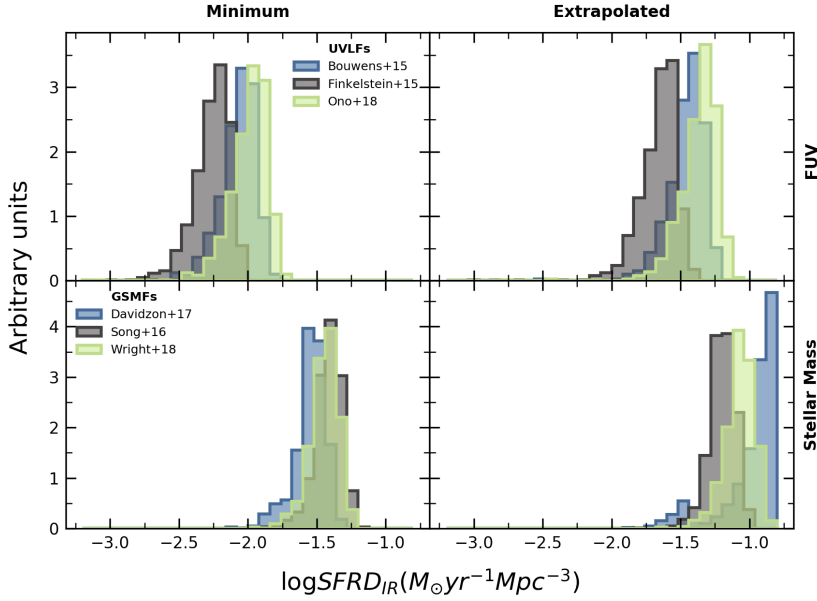


Fig. 5. Probability distribution of the SFRD_{IR} at redshift $z \sim 4.5$. All distributions are derived with the same relations between the stellar mass (*bottom panels*) and FUV magnitudes (*top panels*). The minimum is derived in the observed by ALPINE range of stellar masses and FUV magnitudes and is shown on the *left panels*. The SFRDs from extrapolated relation are shown on the *right panels*. Different colors correspond to different GSMFs and UVLFs (Bouwens et al. 2015b; Finkelstein et al. 2015; Ono et al. 2018; Davidzon et al. 2017; Song et al. 2016; Wright et al. 2018).

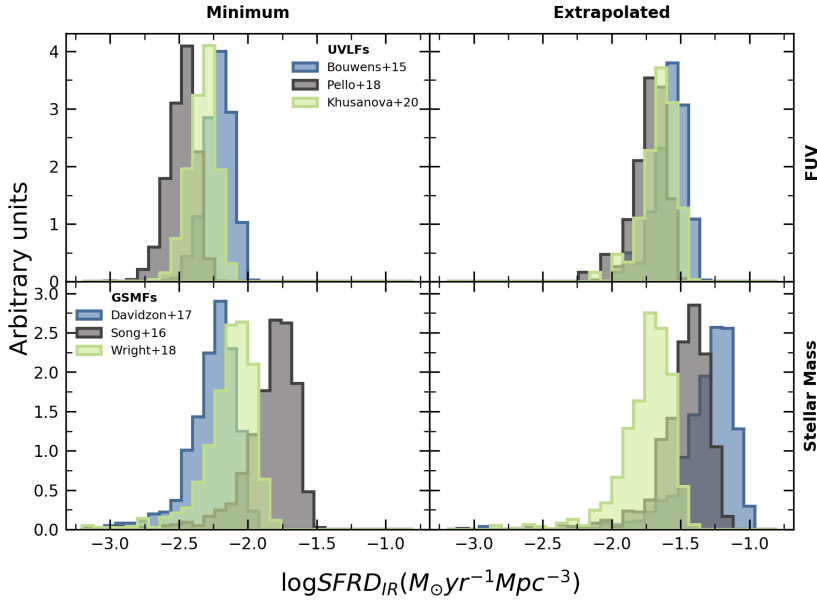


Fig. 6. Same as Fig. 5, but at redshift $z \sim 5.5$. The UVLFs and GSMF are taken from Bouwens et al. (2015b), Pelló et al. (2018), Khusanova et al. (2020), Davidzon et al. (2017), Song et al. (2016), Wright et al. (2018).

we show the lowest value minus 1σ as our lower limits for the IR contribution to SFRD. These are the most robust lower limits of the SFRD_{IR} as they are obtained with a large and representative sample of galaxies at $4.4 < z < 5.8$ and only using the proxy range, where actual observations are available.

Given this lower limit, the IR contribution to the total SFRD is already at least 8–13% at $z > 4$ as compared to the total SFRD from the Madau & Dickinson (2014) curve. While this is seemingly a small amount, these results are in severe disagreement with the results by Koprowski et al. (2017). They fit the evolution of SFRD_{IR} with redshift by the Gaussian function. The extrapolation of this curve gives $\log(\text{SFRD}_{\text{IR}} M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}) = -3.95$ at $z \sim 5.5$, which is much lower than the ALPINE lower limit at this redshift $\log(\text{SFRD}_{\text{IR}} M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}) = -2.67$. Although, the agreement between ALPINE lower limits and SFRD_{IR} measurements by Koprowski et al. (2017) could be reached by a shallower function at $z > 4$, we note that we only considered a small range of masses or FUV magnitudes for computing the lower limit of SFRD_{IR} and our sample is UV-selected.

Hence, the real values at both redshifts are even higher and in even stronger tension with Koprowski et al. (2017). Due to the fact that the work of Koprowski et al. (2017) is based on the IR luminosity functions, the observations in the high redshift bins barely cover the faint end slope of the IR luminosity function, whose uncertainty could be one of the sources of this discrepancy.

4.3.2. Extrapolated infrared star formation rate density

The total SFRD_{IR} is higher than the lower limit derived above. To derive the total SFRD_{IR} , we assume that the $\langle L_{\text{IR}} \rangle$ -proxy relation is the same at all FUV-magnitudes and masses and extrapolate the $\langle L_{\text{IR}} \rangle$ -proxy relation as well as the proxy number density function to the integration limits, corresponding to $0.03L_*$ and $100L_*$ or $\log(M_*/M_{\odot}) = 6.0$ and $\log(M_*/M_{\odot}) = 12.4$ for masses, as mentioned in Sect. 3.2. We obtain the PDFs in the same way as above and show the results on the right panels in Figs. 5 and 6. To place the results in the context of the SFRD evolution, we

Table 2. Infrared SFRD ($\log \text{SFRD}_{\text{IR}} M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}$):

$z \sim 4.5$	GSMF	Lower limit	Extrapolated
	Davidzon+17	$-1.53^{+0.16}_{-0.17}$	$-0.87^{+0.18}_{-0.25}$
	Song+16	$-1.41^{+0.16}_{-0.16}$	$-1.19^{+0.17}_{-0.15}$
	Wright+18	$-1.43^{+0.16}_{-0.17}$	$-1.06^{+0.17}_{-0.18}$
	Combined	-1.64	$-1.07^{+0.28}_{-0.23}$
	UVLF		
	Bouwens+15	$-2.05^{+0.18}_{-0.20}$	$-1.44^{+0.17}_{-0.21}$
	Finkelstein+15	$-2.24^{+0.18}_{-0.20}$	$-1.64^{+0.17}_{-0.21}$
	Ono+18	$-1.97^{+0.18}_{-0.20}$	$-1.34^{+0.17}_{-0.21}$
	Combined	-2.44	$-1.48^{+0.24}_{-0.25}$
$z \sim 5.5$	GSMF		
	Davidzon+17	$-2.24^{+0.26}_{-0.31}$	$-1.27^{+0.26}_{-0.32}$
	Song+16	$-1.81^{+0.26}_{-0.31}$	$-1.45^{+0.26}_{-0.29}$
	Wright+18	$-2.11^{+0.26}_{-0.31}$	$-1.72^{+0.26}_{-0.30}$
	Combined	-2.54	$-1.50^{+0.38}_{-0.39}$
	UVLF		
	Bouwens+15	$-2.20^{+0.21}_{-0.20}$	$-1.56^{+0.22}_{-0.23}$
	Pello+18	$-2.47^{+0.21}_{-0.20}$	$-1.80^{+0.22}_{-0.23}$
	Khusanova+20	$-2.32^{+0.21}_{-0.20}$	$-1.73^{+0.22}_{-0.23}$
	Combined	-2.67	$-1.64^{+0.23}_{-0.24}$
$z \sim 4.5$	UVLF+GSMF	-2.44	$-1.28^{+0.38}_{-0.36}$
$z \sim 5.5$	UVLF+GSMF	-2.67	$-1.60^{+0.36}_{-0.28}$

Notes. Results obtained with various UVLFs and GSMFs from the literature.

combine the PDFs obtained with different proxy density functions from the literature. Since the lengths are the same for all chains, combining them does not favor any particular proxy density function. We obtain an average estimate of the SFRD and our uncertainties naturally include the systematics coming from the GSMF and UVLF.

Figure 8 illustrates the evolution with redshift of SFRD_{IR} and the uncorrected for dust estimate from FUV luminosity density – $\text{SFRD}_{\text{FUV,uncorr}}$. We observe a gradual decrease in the SFRD_{IR} , which only starts to intersect with the $\text{SFRD}_{\text{FUV,uncorr}}$ at $z > 5$. Even at such high redshifts, the $\text{SFRD}_{\text{FUV,uncorr}}$ does not overcome the SFRD_{IR} . It remains an open question, however, at which redshift the $\text{SFRD}_{\text{FUV,uncorr}}$ overcomes the SFRD_{IR} , since at $z > 4$ the SFRD_{IR} is only gradually approaching the $\text{SFRD}_{\text{FUV,uncorr}}$. If the evolution is flatter at higher redshifts, then the dust contribution becomes negligible compared to $\text{SFRD}_{\text{FUV,uncorr}}$ only at very high redshifts. This trend is consistent with the extrapolation of the Maniyar et al. (2018) model of SFRD_{IR} evolution, which is based on CIB anisotropies. Our results agree well with this model at both redshifts. However, if the contribution from ultra-dusty objects, which are missing from the optical and near-infrared (NIR) catalogs is significant, the SFRD_{IR} evolution can be even flatter.

Such objects, indeed, exist. For example, an ultra-dusty merging galaxy was discovered at $z = 5.185$ (Neri et al. 2014), and at even at higher redshift, $z = 6.34$ (Riechers et al. 2013). However, the individual detections do not allow us to derive their contribution to the total infrared SFRD budget. This can only be done from blind search for galaxies observed in the rest-frame FIR and missed by rest-frame UV-surveys. Recently, Gruppioni et al. (2020) determined the SFRD_{IR} using the

nontarget ALPINE sources, which includes galaxies not seen in the rest-frame UV. Our results are in good agreement with the results by Gruppioni et al. (2020) within error bars. Nevertheless, the fiducial value in Gruppioni et al. (2020) is higher than results in this paper. This is not surprising, since by design the nontarget sample does not miss ultra-dusty galaxies. However, given the large uncertainties in both Gruppioni et al. (2020) and in this paper, it is not possible to determine whether this difference is due to the contribution from ultra-dusty galaxies or not. We can only conclude that their contribution is less significant than the uncertainty on the SFRD_{IR} .

4.3.3. Total star formation rate density

We now define the total SFRD at $z \sim 4.5$ and $z \sim 5.5$ by summing the $\text{SFRD}_{\text{UV,uncorr}}$ with the SFRD_{IR} from ALPINE. We plot our results in Fig. 7. The results are in agreement with the FUV based estimates corrected for dust attenuation from the literature within the error bars at both redshifts. They are also in agreement with the majority of measurements based on IR luminosity function, including the measurement from nontarget sources from ALPINE (Gruppioni et al. 2020) and the measurements based on *Herschel* data (Rowan-Robinson et al. 2016; Wang et al. 2019b).

Besides summing the UV and IR contribution, the total SFRD can be estimated using other tracers of SFR. Schaerer et al. (2020) and Béthermin et al. (2020) find that [CII]-SFR relation holds at redshifts $z > 4$. The [CII] luminosity function was determined using both targeted galaxies in ALPINE (Yan et al. 2020) and serendipitous detections (Loiacono et al. 2021). Both [CII] luminosity functions are consistent with each other and SFRD derived using [CII] luminosity density agrees with our measurements. The total SFRD measured using gamma-ray bursts at $z > 4$ (Kistler et al. 2009) also agrees with results of this paper. The good agreement between these independent measurements of the total SFRD shows that even using UV-selected sample, we can trace the major part of the total SFRD. Hence, the contribution of ultra-dusty objects is likely small compared to the contribution of faint but numerous galaxies.

Our results obtained by a combination of two proxies (see Table 2) are 0.5 dex and 0.3 dex higher than the fit of SFRD evolution by Madau & Dickinson (2014) or in 1.4σ and 1.2σ tension at $z \sim 4.5$ and $z \sim 5.5$ respectively. Although, given the uncertainty on the SFRD_{IR} measurement, it is not possible to reach firm conclusions, the evolution of the total SFRD at $z > 4$ is possibly shallower than the best fit in Madau & Dickinson (2014). This is supported by independent tracers of SFRD discussed above (Kistler et al. 2009; Loiacono et al. 2021) as well as with other IR based estimates (Gruppioni et al. 2020; Rowan-Robinson et al. 2016), which are also in tension with dust corrected estimated based on UV luminosity functions.

In Fig. 9, we show the evolution of the dust obscured fraction of SFRD with redshift. We used all the measurements from the literature together with our measurements shown in Figs. 8 and 7 to calculate the average SFRD_{IR} and $\text{SFRD}_{\text{UV,uncorr}}$ in each redshift bin and the ratio of SFRD_{IR} to the total SFRD. We find the IR contribution to the total SFRD equal to $68^{+18}_{-25}\%$ and $61^{+20}_{-25}\%$ at $z \sim 4.5$ and $z \sim 5.5$ respectively. Although significant uncertainties remain, our results show that the dust obscured fraction of SFRD is significant even at $z > 4$. Our results are consistent with semi-analytical model by Cousin et al. (2019), which predict that $\sim 70\%$ of UV radiation is absorbed by dust at $z = 5$, and with the best fit model by Zavala et al. (2018), which predicts $35\%–85\%$ at $z \sim 4–5$.

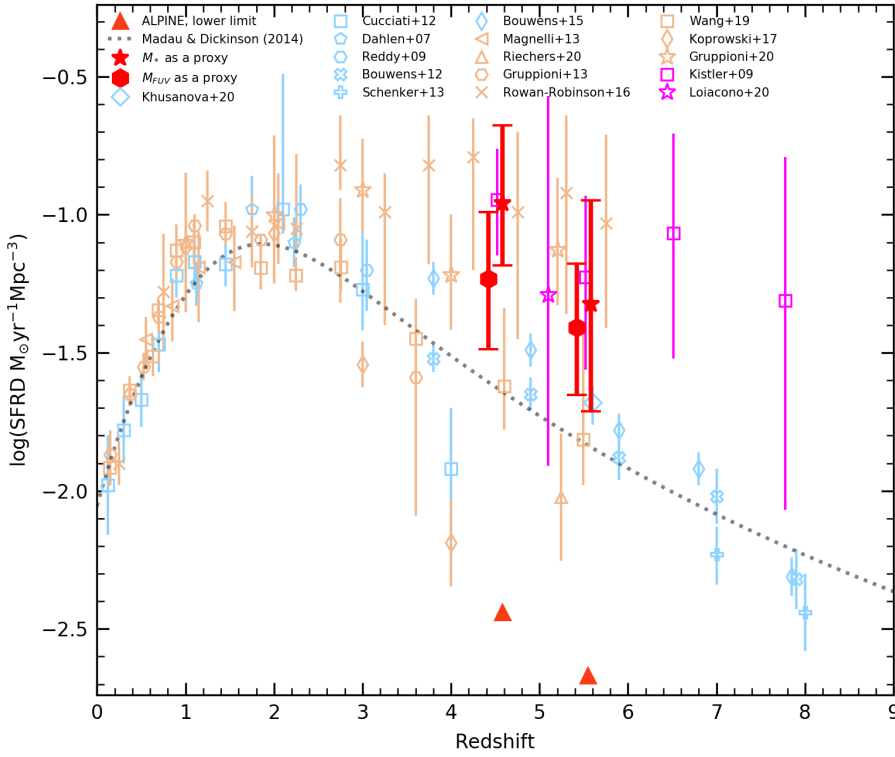


Fig. 7. Evolution of the total SFRD (Eq. (2)) with redshift. The red symbols are the total SFRDs, derived in this paper. Small offsets of ± 0.08 are applied to their redshift for clarity. The triangles are the lower limits for SFRD_{IR} derived in Sect. 4.3.1. The blue symbols are dust-corrected SFRD derived from the FUV data (Cucciati et al. 2012; Dahlen et al. 2007; Reddy & Steidel 2009; Bouwens et al. 2012, 2015b; Schenker et al. 2013; Pelló et al. 2018; Khusanova et al. 2020), orange symbols are derived from reradiated dust emission from forming stars as measured from the IR (Magnelli et al. 2013; Gruppioni et al. 2013, 2020; Rowan-Robinson et al. 2016; Koprowski et al. 2017; Wang et al. 2019a; Riechers et al. 2020). The magenta points are from other SFR tracers: [CII] luminosity function based on the ALPINE field sample of Loiacono et al. (2021) and number counts of γ -ray bursts (Kistler et al. 2009). The dotted line is the fit of SFRD evolution from Madau & Dickinson (2014).

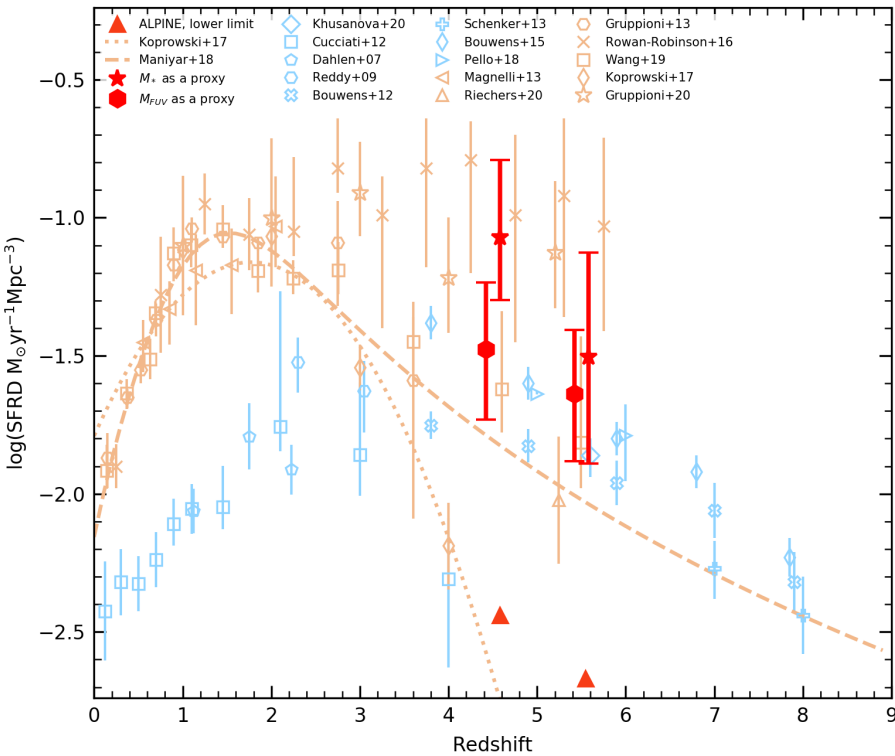


Fig. 8. Evolution of SFRD_{IR} and $\text{SFRD}_{\text{FUV,uncorr}}$ with redshift. The red symbols are the SFRD_{IR} , derived in this paper. Small offsets of ± 0.08 are applied to their redshift for clarity. The triangles are the lower limits for SFRD_{IR} derived in Sect. 4.3.1. The blue symbols are $\text{SFRD}_{\text{FUV,uncorr}}$ derived from the FUV data (Cucciati et al. 2012; Dahlen et al. 2007; Reddy & Steidel 2009; Bouwens et al. 2012, 2015b; Schenker et al. 2013; Pelló et al. 2018; Khusanova et al. 2020), orange symbols are SFRD_{IR} from Magnelli et al. (2013), Gruppioni et al. (2013, 2020), Rowan-Robinson et al. (2016), Koprowski et al. (2017), Wang et al. (2019a) and Riechers et al. (2020). Orange lines are the fits of SFRD_{IR} evolution from Koprowski et al. (2017) and Maniyar et al. (2018).

Since we used a sample of galaxies detected in FUV, we did not take into account the contribution from highly obscured and purely IR galaxies, which remains unknown at these redshifts, mainly due to the difficulties in detecting such galaxies. The low number counts of the most massive galaxies makes it difficult to make a statistical census. No sources with $z > 5$ were found by the deep ALMA observations of the *Hubble* Ultra-Deep Field (HUDF; Aravena et al. 2016; Dunlop et al. 2017; González-

López et al. 2019). Only recently, a few sources with no optical or NIR counterparts were discovered with ALMA at $z \sim 4$ and $z \sim 5$ (Franco et al. 2018; Williams et al. 2019) and even $z \sim 6.9$ (Strandet et al. 2017; Marrone et al. 2018). The largest sample up to date is assembled by Wang et al. (2019b). It contains 39 *H*-band dropouts at $z > 3$ observed with ALMA. Given their results, such galaxies could have an additional contribution of $\sim 11\%$ to the total SFRD at $z > 4$. Since their sample is restricted

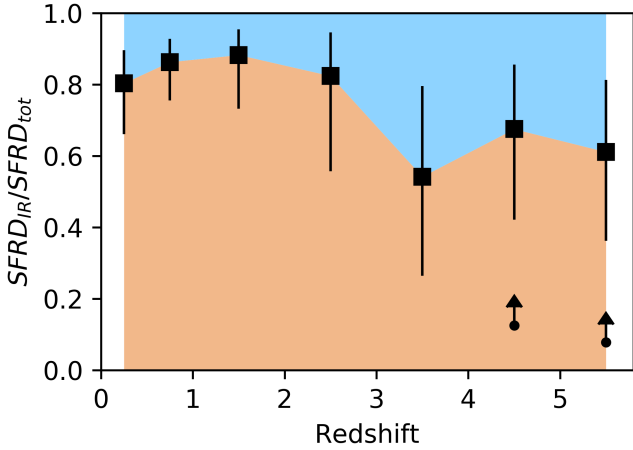


Fig. 9. Evolution of the fraction of the dust obscured $SFRD_{IR}$ as a function of redshift. The arrows show the lower limits obtained using the lower limits discussed in Sect. 4.3.1. The points at $z < 4$ are obtained using a compilation of the literature from Fig. 7. The points at $z > 4$ are obtained using the UVLF+GSMF combined measurements from Table 2.

to massive H -band dropouts, this is only a lower limit. The lower mass H -band dropouts could contribute to it significantly. Indeed, given the most recent results by Riechers et al. (2020), the dust obscured SFRD is $\log(SFRD_{IR} M_{\odot} yr^{-1} Mpc^{-3}) = -2.02$ or 22% of the total SFRD (based on the space density of two sources detected by CO ($J=2 \rightarrow 1$) and not detected in the rest-frame UV and optical).

Another uncertainty comes from the fact that the conversion from the $158 \mu m$ flux to L_{IR} in this work is based only on one point in the infrared SED. Therefore, our measurement of the total IR luminosity are dependent on the choice of the dust SED template. The infrared SED in high redshift galaxies is uncertain due to poorly constrained dust temperatures (Pavesi et al. 2016; Bouwens et al. 2016; Faisst et al. 2017, 2020). We tested a number of templates against the stacking of *Herschel* data and only used the ones, which are compatible with the *Herschel* stacks at redshift range of ALPINE (see appendix). The best fit of modified black body to these stacks gives the dust temperature $T_{dust} = 41 \pm 1$ K at $z \sim 4.5$ and $T_{dust} = 43 \pm 5$ K at $z \sim 5.5$ consistent with most recent measurements by Faisst et al. (2020; $T_{dust} = 38 \pm 8$ at $z \sim 5.5$). Although some uncertainties on the dust temperature and the rest-frame FIR part of the SED remain, we incorporate them into the uncertainty of our SFRD measurement by using an average conversion factor between the templates compatible with the stacks of *Herschel* data and taking into account the uncertainty of the conversion factor. Nevertheless, more observations are needed to better constrain the dust temperatures and SED of galaxies at $z > 4$.

5. Star-forming main sequence and sSFR evolution

The main sequence is the relation between the mass and SFR of star-forming galaxies. In Sect. 4.2, we derived the $\langle L_{IR} \rangle - M_*$ relation. Here we use this relation to derive the main sequence. In each mass bin, we derive average SFR as $\langle SFR \rangle = \kappa_{FUV} \langle L_{1600} \rangle + \kappa_{IR} \langle L_{IR} \rangle$. The average $\langle L_{1600} \rangle$ is computed from FUV absolute magnitudes, determined with the SED fitting, and the average $\langle L_{IR} \rangle$ from stacks. As discussed in Sect. 3.2.2, we consider the results from the stacks as upper limits at masses below the completeness limits.

We derived the main sequence in the two redshifts bins: $4.4 < z < 4.7$ and $5.1 < z < 5.8$. We show the results in Fig. 10. The main sequence is well-defined and is in very good agreement with previous results from the literature (Santini et al. 2017; Tasca et al. 2015; Heinis et al. 2013; Khusanova et al. 2020). We fit the relation between SFR and mass with a power law. We find a slope $\alpha = 0.99 \pm 0.08$ at $z \sim 4.5$. We find an excellent agreement with the Schreiber et al. (2015) parametrization of the main sequence evolution at $z \sim 4.5$ based on *Herschel* data, even if we measure the SFRs at lower masses compared to Schreiber et al. (2015).

At $z \sim 5.5$, we obtain a shallower slope $\alpha = 0.66 \pm 0.21$. The difference with the slope at $z \sim 4.5$ is only 1.5σ , providing no evidence for an evolution of the slope between the two redshift bins. We note that at $z \sim 5.5$, we could only provide FIR flux upper limits at lower masses due to the selection effects (see Sect. 3.2.2). Therefore, we only used three points to fit our data and the fit is subject to larger uncertainties. The slope of the main sequence found with *Herschel* data (Pearson et al. 2018) at the same redshift but at larger masses is steeper than found with ALPINE data, but still consistent with our data on stacks within the error bars.

In Fig. 10, we also plot the individual measurements for galaxies with continuum detections. As expected, most of them are above the main sequence since they represent the brightest galaxies with high SFRs. This confirms that it is necessary to use stacking to obtain unbiased measurements of the average SFR as a function of M_* and fit the main sequence.

We measured the sSFR in the mass range $9.6 < \log(M_*/M_{\odot}) < 9.8$ as in Santini et al. (2017). The average sSFR is $\log sSFR (Gyr^{-1}) = -8.4 \pm 0.18$ and $\log sSFR (Gyr^{-1}) = -8.45 \pm 0.16$ at $z \sim 4.5$ and $z \sim 5.5$, respectively. We present a comparison with results from the literature in Fig. 11. We find good agreement within the error bars with the results from Khusanova et al. (2020) at $z > 5$ and with *Herschel* data at $z \sim 4$ (Béthermin et al. 2015; Schreiber et al. 2015), although we note that the studies based on *Herschel* data probe only the high mass end ($\log(M_*/M_{\odot}) > 10.0$) at $z \sim 4$. The results are clearly against a steep increase in sSFR at $z > 4$ and even indicate a possible decrease in sSFR at high redshift. More observations at higher redshifts are necessary to explore this trend.

If the growth of galaxies is regulated mainly by gas accretion through cold streams, the sSFR evolves as $\sim (1+z)^{2.25}$ (DeKel et al. 2009; Davé et al. 2011; Sparre et al. 2015). This is not the case at high redshifts. Therefore, another mechanism may play a role in the growth of galaxies, such as major and minor mergers (see e.g., Faisst et al. 2016). Another possible explanation could be the suppression of star formation by stronger stellar feedback at high redshifts and reduced star formation efficiency (see e.g., Weinmann et al. 2011). Future studies will place constraints on the role of different mechanisms regulating star formation and the growth of galaxies at high redshifts.

6. Conclusions

In this paper, we explored the SFRD, sSFR and main sequence evolution at $z > 4$ with ALPINE. Using the stacking technique, we constrained the average properties of galaxies even with low number of individual detections.

We provide the robust lower limits for infrared SFRD at $z \sim 4.5$ and 5.5 , which indicate that the dust plays an important role at high redshift and that dust build-up happens quite rapidly during and just after epoch of reionization. Based on extrapolated the density functions, we determine the total dust-hidden

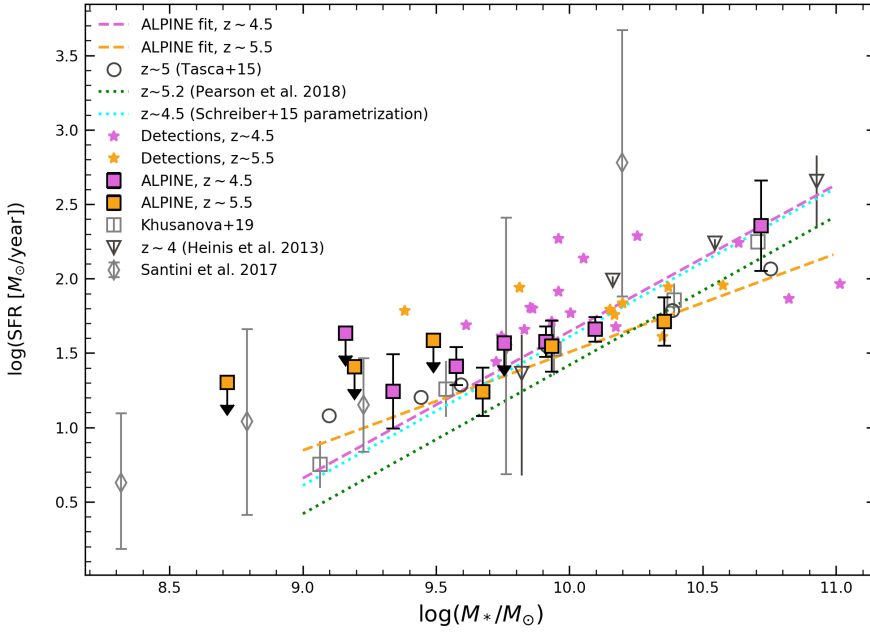


Fig. 10. Main sequence of star-forming galaxies at $z \sim 4.5$ and $z \sim 5.5$. The filled squares are the measurements of average SFR from stacks; the open symbols are results from the literature; the magenta and orange lines are the fits of the main sequence at $z \sim 4.5$ and $z \sim 5.5$ respectively; the cyan and green lines are the fits of the main sequence from the literature. The colored stars are the individual galaxies in ALPINE with FIR continuum detections at $>3\sigma$.

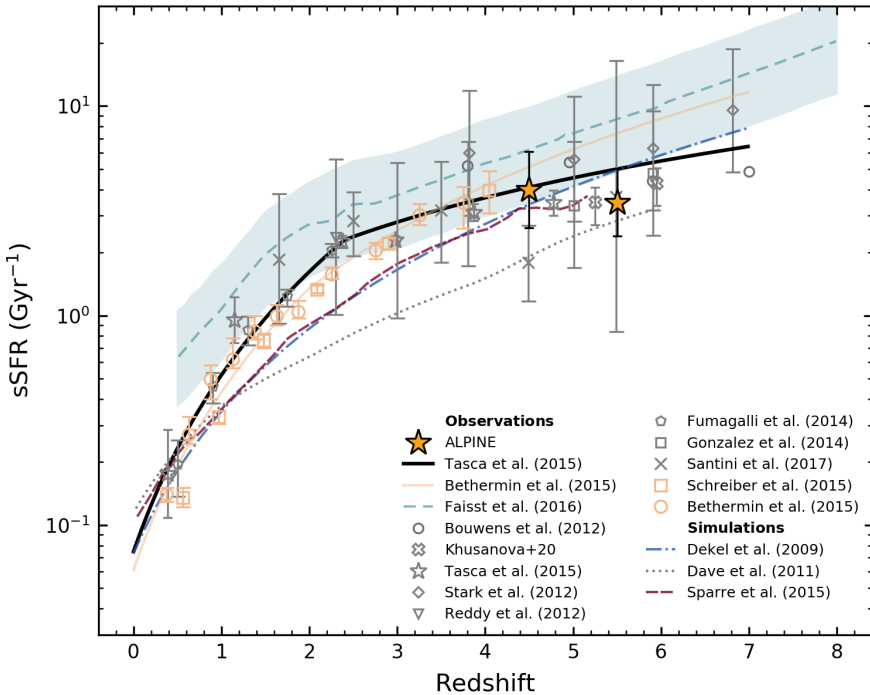


Fig. 11. SSFR evolution with redshift. Results of various observations and numerical simulations are shown (Dekel et al. 2009; Davé et al. 2011; Sparre et al. 2015). Gray symbols are based on FUV data (Bouwens et al. 2012; Khusanova et al. 2020; Tasca et al. 2015; Stark et al. 2013; Reddy et al. 2012; Fumagalli et al. 2014; González et al. 2014; Santini et al. 2017). Orange symbols are based on the rest-frame FIR data (Schreiber et al. 2015; Béthermin et al. 2015). The orange filled stars show this paper's results. The solid line shows the fit to results by Tasca et al. (2015), the shaded area and the dashed line show the results coming from the observations of EW(H α) in COSMOS (Faisst et al. 2016).

IR contribution to SFRD using either masses or FUV magnitudes as a proxy of IR luminosity. The results obtained using different proxies (see Table 2) agree with each other within the error bars. The results are $\log \text{SFRD}_{\text{IR,tot}}^{z=4} (M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}) = -1.28^{+0.38}_{-0.36}$ and $\log \text{SFRD}_{\text{IR,tot}}^{z=5} (M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}) = -1.60^{+0.36}_{-0.28}$. They correspond to $68^{+18}_{-25}\%$ and $61^{+20}_{-25}\%$ fractions of the star formation hidden by dust at $z \sim 4.5$ and $z \sim 5.5$ respectively. While at $z < 4$ the SFRD_{IR} component dominates over the $\text{SFRD}_{\text{FUV,uncorr}}$, at $z > 4$ their contributions are comparable. The SFRD_{IR} approaches and possibly crosses the $\text{SFRD}_{\text{FUV,uncorr}}$ at $z > 5$ but this is yet to be confirmed with future observations.

Although our method by design does not include the contribution from ultra-dusty galaxies, our results agree with a number of independent measurements of the total SFRD at this redshift (based on IR luminosity function, [CII] luminosity function and

gamma-ray bursts). Hence, we conclude that the major part of the SFRD can be traced by UV-selected galaxies.

The evolution of the total SFRD at redshifts higher than the peak of SFRD at $z \sim 2.5$ may be shallower than previously measured. Further observations leading to reduced uncertainties are needed to confirm this conclusion.

We also provide robust measurements of SFRs of galaxies at $z > 4$ and use them to determine the main sequence at $z \sim 4.5$ and $z \sim 5.5$. We find that the observed main sequence is in good agreement with the previous results based on the rest-frame UV and optical data, as well as the IR data for the most massive galaxies. The main sequence has a slope $\alpha = 0.99 \pm 0.08$ at $z \sim 4.5$ and $\alpha = 0.66 \pm 0.21$ at $z \sim 5.5$, and no signs of turn-over at high masses. No significant evolution is observed from $z \sim 4.5$ to $z \sim 5.5$.

We use the SFR and mass measurements to determine the average sSFR of galaxies at $z > 4$. The results support a shallower or nonexistent sSFR evolution at high redshifts than predicted from models of cold gas accretion, or no evolution. Other mechanisms should play an important role in governing the growth of galaxies.

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Appendix A: Conversion of FIR flux to IR luminosity

To convert the rest-frame $158\ \mu\text{m}$ flux to IR luminosity, we scaled our flux measurement to the dust SED template and then integrated it from 8 to $1000\ \mu\text{m}$. Since we used stacks of galaxies, which are not at the same redshift, we used the mean redshift of galaxies in stacks for that conversion. Since we only obtain a measurement of one point in SED, our conversion to IR luminosity depends on dust SED templates.

There are numerous dust SED templates available in the literature (e.g., Magdis et al. 2012; Béthermin et al. 2017; Álvarez-Márquez et al. 2016; Casey et al. 2018; Schreiber et al. 2018; De Rossi et al. 2018; Álvarez-Márquez et al. 2019). Some of them were already discussed and tested by Béthermin et al. (2020). Béthermin et al. (2020) made stacks of *Herschel* data for galaxies at $z > 4$ selected via photometric redshifts. They then compared the SED templates to these stacks. The fit with the modified black body model corresponds to the average dust temperature $T_d = 41 \pm 1\ \text{K}$ at $z \sim 4.5$ and $T_d = 43 \pm 5\ \text{K}$ at $z \sim 5.5$ for galaxies with $\text{SFR} > 10\ M_\odot\text{yr}^{-1}$. The SFR limit is defined by completeness of the sample. It is not possible to test whether the dust temperature is lower for fainter galaxies, due

to this limitation. However, the uncertainty on the choice of the template naturally includes the uncertainty on the dust temperature. When we convert the IR luminosity in each bin of M_{FUV} or M_* to SFR, we assume that we do not know the exact dust temperature typical for this M_{FUV} or M_* and that the uncertainty on the conversion factor includes the uncertainty on the dust temperature.

We defined the conversion factor f_{temp} for each template and the χ^2 from comparison to *Herschel* stacks at both redshifts (see Table A.1). The conversion factor is defined as $f_{\text{temp}} = \nu L_{\nu=158\mu\text{m}}/L_{\text{IR}}$. We discarded the templates with reduced $\chi^2 > 1.5$ in at least one of the redshift bins (see Fig. A.3). We defined the mean conversion factors from the remaining templates $\langle f_{\text{temp},z\sim 4.5} \rangle = 0.13 \pm 0.02$ and $\langle f_{\text{temp},z\sim 5.5} \rangle = 0.12 \pm 0.03$ for redshift bins $4 < z < 5$ and $5 < z < 6$ respectively. These are the values we used to convert the monochromatic flux to the IR luminosity and propagate their uncertainties into our SFRD measurements.

We note that although the De Rossi et al. (2018) template passes our χ^2 criteria, it goes above the upper limits in redshift bin $4 < z < 5$, but is perfectly consistent at $5 < z < 6$. Therefore, we used this template only for $5 < z < 6$ redshift bin.

Table A.1. Dust SED templates, conversion factors f_{temp} , and SFRD_{IR} corresponding to templates from the literature.

Reference	f_{temp}	$\text{SFRD}_{\text{IR},z=4.5}$	$\chi^2_{z=4.5}$	$\text{SFRD}_{\text{IR},z=5.5}$	$\chi^2_{z=5.5}$
Béthermin et al. (2017)	0.133	$-1.37^{+0.21}_{-0.27}$	1.61	$-1.71^{+0.21}_{-0.17}$	3.40
Álvarez-Márquez et al. (2019) L1	0.105	$-1.47^{+0.21}_{-0.27}$	1.16	$-1.81^{+0.21}_{-0.17}$	3.19
Álvarez-Márquez et al. (2019) L2	0.152	$-1.31^{+0.21}_{-0.27}$	4.69	$-1.65^{+0.21}_{-0.17}$	5.36
Álvarez-Márquez et al. (2019) L3	0.123	$-1.40^{+0.21}_{-0.27}$	1.89	$-1.74^{+0.21}_{-0.17}$	3.81
Álvarez-Márquez et al. (2019) M2	0.119	$-1.42^{+0.21}_{-0.27}$	1.04	$-1.76^{+0.21}_{-0.17}$	3.35
Álvarez-Márquez et al. (2019) M3	0.148	$-1.32^{+0.21}_{-0.27}$	1.97	$-1.66^{+0.21}_{-0.17}$	4.28
Álvarez-Márquez et al. (2019) M4	0.152	$-1.31^{+0.21}_{-0.27}$	2.20	$-1.65^{+0.21}_{-0.17}$	4.46
Álvarez-Márquez et al. (2019) M5	0.153	$-1.31^{+0.21}_{-0.27}$	2.28	$-1.65^{+0.21}_{-0.17}$	4.52
Schreiber et al. (2018), $z = 4.5$	0.093	$-1.53^{+0.21}_{-0.27}$	2.12	$-1.86^{+0.21}_{-0.17}$	–
Schreiber et al. (2018), $z = 5.5$	0.073	$-1.63^{+0.21}_{-0.27}$	–	$-1.97^{+0.21}_{-0.17}$	3.98
De Rossi et al. (2018)	0.067	$-1.67^{+0.21}_{-0.27}$	4.65	$-2.01^{+0.21}_{-0.17}$	3.76
Discarded templates					
Álvarez-Márquez et al. (2016)	0.189	$-1.22^{+0.21}_{-0.27}$	9.74	$-1.56^{+0.21}_{-0.17}$	7.05
Álvarez-Márquez et al. (2019) L4	0.229	$-1.13^{+0.21}_{-0.27}$	12.89	$-1.47^{+0.21}_{-0.17}$	8.54
Álvarez-Márquez et al. (2019) M1	0.354	$-0.94^{+0.21}_{-0.27}$	35.84	$-1.28^{+0.21}_{-0.17}$	16.14
Casey et al. (2018) A	0.244	$-1.11^{+0.21}_{-0.27}$	11.71	$-1.45^{+0.21}_{-0.17}$	9.00
Casey et al. (2018) B	0.036	$-1.94^{+0.21}_{-0.27}$	12.99	$-2.23^{+0.21}_{-0.17}$	7.74

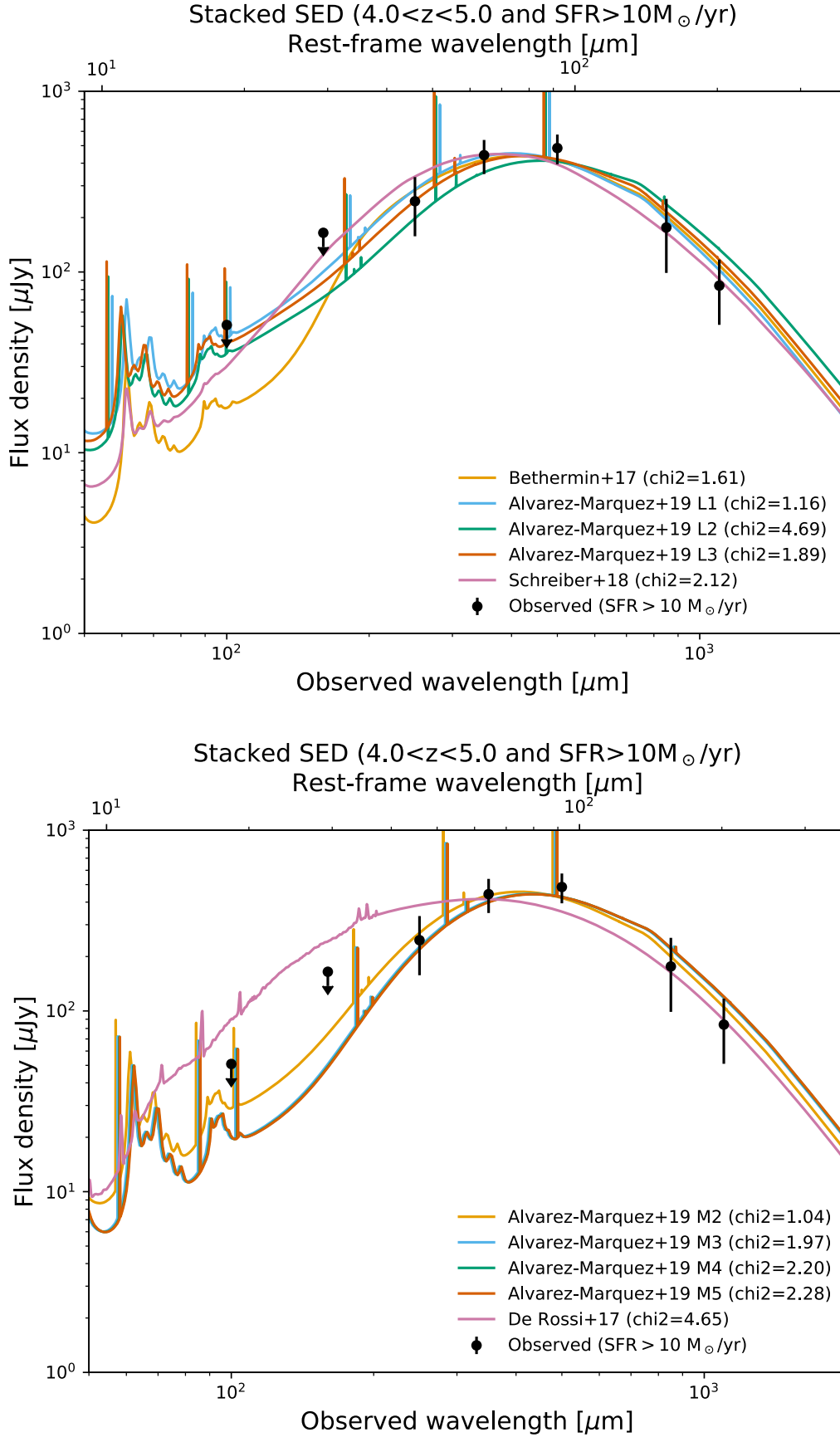


Fig. A.1. Comparison of the chosen dust SED templates with the stacks of *Herschel* data at $4 < z < 5$. The black symbols are stacked *Herschel* data and the solid lines are templates from the literature.

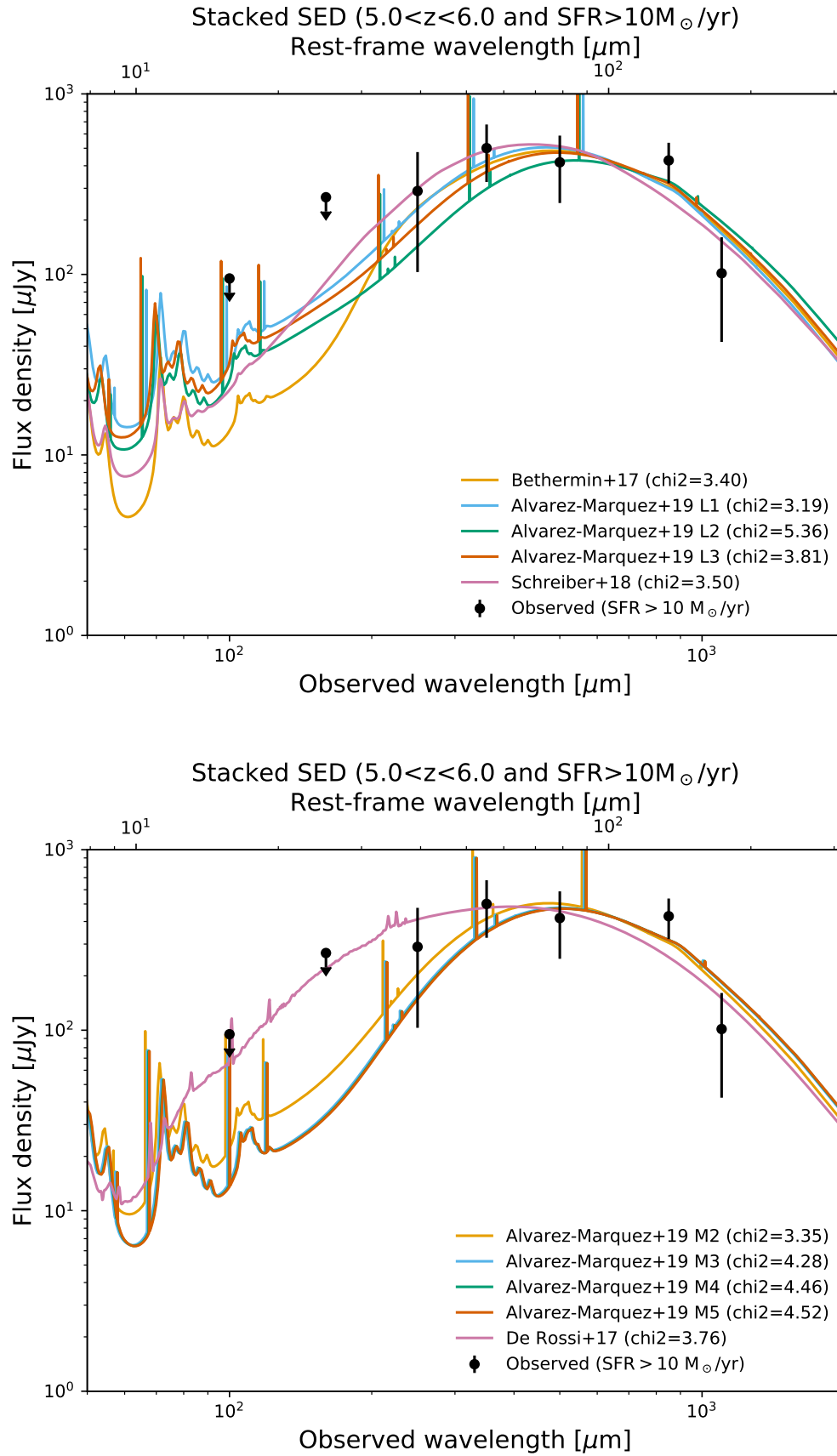


Fig. A.2. Comparison of the chosen dust SED templates with the stacks of *Herschel* data at $5 < z < 6$. The black symbols are stacked *Herschel* data and the solid lines are templates from the literature.

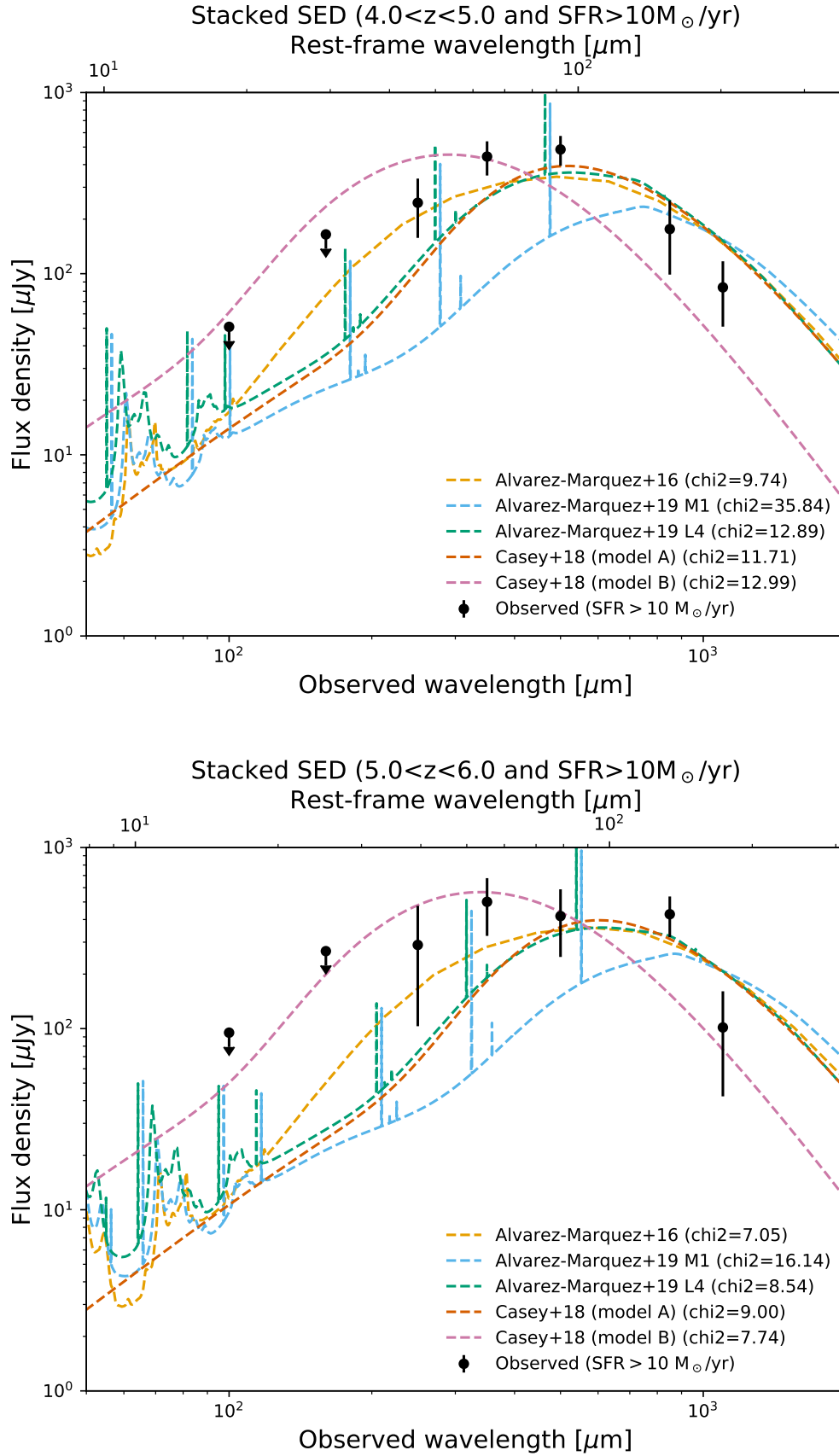


Fig. A.3. Comparison of the discarded dust SED templates with the stacks of *Herschel* data at. The black symbols are stacked *Herschel* data and the dashed lines are templates from the literature.