

Study of $e^+e^- \rightarrow h^+h^-J/\psi$ ($h = \pi, K, p$) via initial-state radiation at Belle II

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Using a data sample of 427.9 fb^{-1} collected by the Belle II detector at or near the $\Upsilon(4S)$ and $\Upsilon(10753)$ resonances, the cross sections for $e^+e^- \rightarrow h^+h^-J/\psi$ ($h = \pi/K/p$) at center-of-mass energies ranging from 3.8 GeV or the production threshold to 5.5/6.0/7.0 GeV have been measured via initial-state radiation. The cross sections for the processes $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ and $e^+e^- \rightarrow K^+K^-J/\psi$ are consistent with previously published results. The cross sections for these channels obtained by combining with previous Belle results are also given. The process $e^+e^- \rightarrow p\bar{p}J/\psi$ is investigated for the first time. The yields are small and no significant structure is observed in the cross section versus energy. Searches for vector charmoniumlike states in the h^+h^-J/ψ systems, and for associated intermediate states in the $h^\pm J/\psi$ systems, are also presented.

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I. INTRODUCTION

The traditional quark model successfully describes most charmonium states above the open-charm threshold ($D\bar{D}$ production threshold), such as $\psi(3770)$, $\psi(4040)$, and $\psi(4160)$ [1,2]. However, since 2003, many unexpected resonant states have been observed. These states exhibit exotic properties, including unusual masses and quantum numbers, which cannot be explained by the simple $c\bar{c}$ configuration within the traditional quark model [3,4]. Among these, several vector charmoniumlike states have been identified through either direct e^+e^- annihilation or initial-state radiation (ISR) processes, in which the e^+e^- system emits one or more photons, resulting in a lower c.m. energy for the annihilating e^+e^- pair [5–12]. Candidates for tetraquark and pentaquark states have also been discovered [9,13–22]. These states have unusual decay modes and are close to production thresholds for two-hadron systems. A variety of phenomenological models have been proposed to describe their structures, including the compact multiquark model [23] and the hadronic molecule model [24,25]. Notably, the first observed vector charmoniumlike state, $Y(4260)$, also known as $\psi(4230)$ [26], has been interpreted as a $D_1(2420)\bar{D}$ molecular state [27], and it has been suggested that the pentaquark candidates P_c^+ are molecular states composed of $\Lambda_c^{(*)}\bar{D}^{(*)}$ or $\Sigma_c^{(*)}\bar{D}^{(*)}$ [28–30]. However, due to the limited availability of experimental data, a comprehensive understanding of these exotic states remains elusive, and the validity of the proposed models continues to be a subject of active debate [3,26].

The $Y(4260)$ state was first discovered in the $\pi^+\pi^-J/\psi$ final state by *BABAR* in 2005 [5]. Later, this state was found by BESIII to consist of two substructures, $Y(4230)$ and $Y(4320)$ [31,32]. In addition to these findings, both Belle and BESIII observed a broad resonance in the $\pi^+\pi^-J/\psi$ system, namely $Y(4008)$ [6,9,32]. However, *BABAR* disputed the existence of this state [33]. A global coupled-channel analysis predicts a $\psi(4040)$ -like enhancement in the $\pi^+\pi^-J/\psi$ invariant mass distribution [34]. Investigations of related strange-charmonium final states have been carried out through the processes $e^+e^- \rightarrow K^+K^-J/\psi$ and $e^+e^- \rightarrow K_S^0\bar{K}_S^0J/\psi$ at BESIII. These studies have led to the observation of two novel structures, $Y(4500)$ and $Y(4710)$ [35–38]. Belle also investigated the processes $e^+e^- \rightarrow K^+K^-J/\psi$ and $e^+e^- \rightarrow K_S^0\bar{K}_S^0J/\psi$ via ISR, but did not have sufficient sensitivity to confirm these structures [39,40].

Additional measurements of the h^+h^-J/ψ cross sections are essential input for the investigation of these exotic states. The $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ cross section was measured by *BABAR* from 3.5 to 5.5 GeV and by Belle from 3.8 to 5.5 GeV using ISR production in data samples with integrated luminosities of 454 fb^{-1} [33] and 967 fb^{-1} [9], respectively. BESIII measured it from 3.77 to 4.70 GeV using an energy-scan method [31,32]. For the $e^+e^- \rightarrow K^+K^-J/\psi$ cross section, Belle measured it from the production threshold up to 6.0 GeV with a data sample of 980 fb^{-1} [40], and BESIII measured it from the production threshold to 4.95 GeV using the energy-scan method [36,37]. Recently, the authors of Ref. [41] predicted the cross section of $e^+e^- \rightarrow p\bar{p}J/\psi$ to be $\mathcal{O}(4 \text{ fb})$ around 6 GeV. Independent experimental measurements from Belle II can add to and extend these existing measurements.

We present a study of the process $e^+e^- \rightarrow h^+h^-J/\psi$ ($h = \pi/K/p$) via ISR by analyzing 427.9 fb^{-1} of data collected with the Belle II detector at or near the $\Upsilon(4S)$ and $\Upsilon(10753)$ resonances [42]. The analysis focuses

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on c.m. energies ranging from 3.8 GeV or the production threshold up to 5.5/6.0/7.0 GeV. We measure the production cross sections of $e^+e^- \rightarrow h^+h^-J/\psi$ processes in the regions of several vector charmoniumlike states. This analysis provides an independent cross check of the processes $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ and $e^+e^- \rightarrow K^+K^-J/\psi$, with precision comparable to that of Belle. We also investigate the previously unexplored final state involving baryons, $e^+e^- \rightarrow p\bar{p}J/\psi$, which may offer deeper insight into pentaquark production mechanisms. Furthermore, we explore possible intermediate states in the $h^\pm J/\psi$ systems.

II. DETECTOR AND DATASET

The Belle II experiment is located at SuperKEKB, which collides electrons and positrons at and near the $\Upsilon(4S)$ resonance [43]. The Belle II detector [44] has a cylindrical geometry and includes a two-layer silicon-pixel detector (PXD) surrounded by a four-layer double-sided silicon-strip detector [45] and a 56-layer central drift chamber (CDC). Position information from these detectors is used to reconstruct the trajectories of charged particles [46]. Only one sixth of the second layer of the PXD was installed for the data analyzed here. The symmetry axis of these detectors, defined as the z axis, is almost coincident with the direction of the electron beam. Surrounding the CDC, which also provides dE/dx energy-loss measurements, is a time-of-propagation counter (TOP) [47] in the central region and an aerogel-based ring-imaging Cherenkov counter (ARICH) in the forward region. These detectors provide charged-particle identification. Surrounding the TOP and ARICH is an electromagnetic calorimeter (ECL) based on CsI(Tl) crystals that primarily provides energy and timing measurements for photons and electrons. Outside of the ECL is a superconducting solenoid magnet. The magnet provides a 1.5 T magnetic field that is parallel to the z axis. A K_L^0 and muon detection system (KLM) is installed in the iron flux return of the solenoid.

Signal Monte Carlo (MC) samples are generated using a combination of PHOKHARA [48,49] and EvtGen [50], and are employed to guide event selection and determine detection efficiencies. The simulation of ISR events is performed with PHOKHARA at next-to-leading order accuracy in quantum electrodynamics, while meson and hadron decays are generated using EvtGen. Effects of final-state radiation (FSR) are incorporated with PHOTOS [51]. The Geant4 [52] package is employed to simulate the passage of particles through the detector and the detector response. One million signal events per channel are generated for each of $\pi^+\pi^-J/\psi$, K^+K^-J/ψ , and $p\bar{p}J/\psi$ at various center-of-mass energies ($\sqrt{s}$), with the h^+h^-J/ψ system distributed according to phase space (PHSP). For each channel, events are produced at eight different energy points to determine the detection efficiency. The dependence of efficiency on $\sqrt{s}$ is determined from a fit to the eight discrete values. These efficiencies are further weighted by the Dalitz plot

distributions obtained from data to derive the final efficiency estimates, which will be described in detail later in the text. Generic MC samples including background events from $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$), $e^+e^- \rightarrow \tau^+\tau^-$, $e^+e^- \rightarrow (\gamma)e^+e^-$ (Bhabha), $e^+e^- \rightarrow (\gamma)\mu^+\mu^-$ (dimuon), and $e^+e^- \rightarrow h^+h^-$ ($h = \pi, K, p$) via ISR, with the same integrated luminosity as the data, are utilized to study background processes in the analysis [53–55]. All data and simulated events are reconstructed and analyzed using the Belle II Analysis Software Framework [56].

III. EVENT SELECTION

Events are selected by the hardware-based level 1 triggers using signals from the CDC, ECL, or KLM. Tracks are required to be within $|d_z| < 3$ cm and $|d_r| < 1$ cm, where d_z and d_r are the distances of the closest approach to the interaction point along the z axis and in the transverse plane, respectively. Tracks are also required to have a polar angle (θ) between 17° and 150° , which is within the acceptance of the CDC. We require the total number of selected tracks in the event to be four, and the net charge to be zero. The particle identification (PID) information from various detector subsystems is combined in a likelihood $\mathcal{L}_i$ for particle species $i \in \{e, \mu, \pi, K, p, d\}$ [57]. Tracks with $\mathcal{R}_\pi = \mathcal{L}_\pi / (\mathcal{L}_\pi + \mathcal{L}_K) > 0.6 (< 0.4)$ are identified as pions (kaons). Pions (kaons) are identified with approximately 92% (95%) efficiency and approximately 6% (4%) kaon (pion) misidentification efficiency. Tracks with $\mathcal{R}_{e/\mu/p} = \mathcal{L}_{e/\mu/p} / \sum_i \mathcal{L}_i > 0.5$ are identified as electrons, muons, and protons, respectively, corresponding to approximate identification efficiencies of 90%, 85%, and 90%, respectively. For electrons and positrons, bremsstrahlung and FSR corrections are applied by incorporating the four momenta of the photons within a cone of 50 mrad around the initial direction of the electron or positron. Photons are identified from ECL energy deposits greater than 75, 100 and 50 MeV in the forward, backward and barrel regions, respectively. These regions correspond to θ ranges in the lab frame of $[12.4^\circ, 31.4^\circ]$, $[130.7^\circ, 155.1^\circ]$, and $[32.2^\circ, 128.7^\circ]$.

The J/ψ candidates are reconstructed in both e^+e^- and $\mu^+\mu^-$ decay modes. A clear J/ψ signal is observed in the data, with a purity exceeding 95% for the process $\psi(2S) \rightarrow \pi^+\pi^-J/\psi$, and approximately 80% for the process $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ in the high-mass region. The J/ψ signal regions for the two modes are defined to have $M(e^+e^-)$ in the region (3.02, 3.14) GeV/ c^2 and $M(\mu^+\mu^-)$ in the region (3.06, 3.14) GeV/ c^2 . The J/ψ mass sidebands are defined as having $M(e^+e^-)$ in either the (2.81, 2.99) GeV/ c^2 or the (3.17, 3.35) GeV/ c^2 regions, or having $M(\mu^+\mu^-)$ in either the (2.91, 3.03) GeV/ c^2 or the (3.17, 3.29) GeV/ c^2 regions. The width of each sideband region is three times the width of the corresponding signal region. A mass-constrained fit to J/ψ candidates is

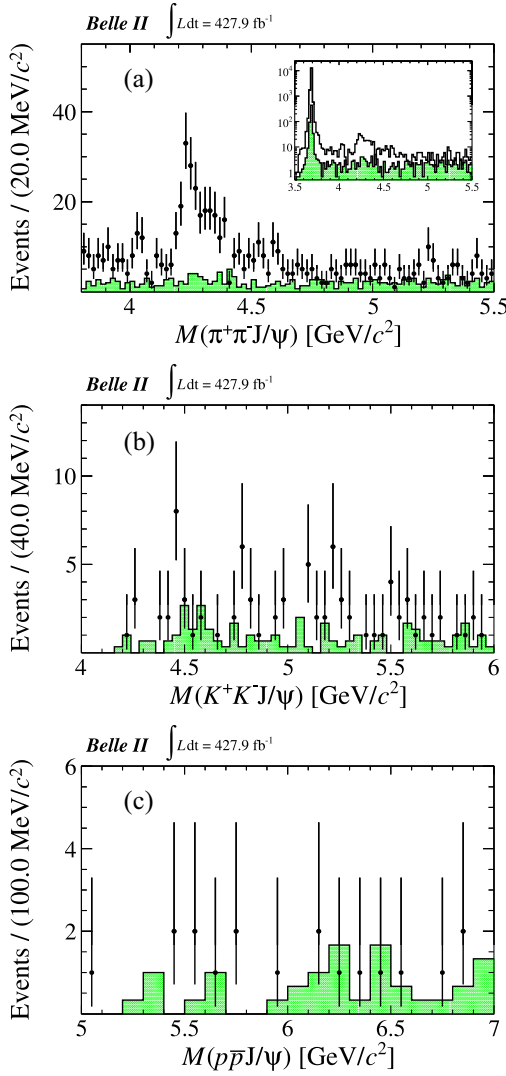


FIG. 1. Invariant mass distributions of (a) $\pi^+\pi^-J/\psi$, (b) K^+K^-J/ψ , and (c) $p\bar{p}J/\psi$. The black dots with error bars represent the selected data and the green shaded histograms are from the normalized J/ψ sidebands. The inset in (a) shows the distribution extended to lower masses on a logarithmic vertical scale, and the large peak near 3.686 GeV is from $\gamma_{\text{ISR}}\psi(2S)$.

performed to determine J/ψ -related variables and improve the resolution.

In the channel $e^+e^- \rightarrow \pi^+\pi^-J/\psi(\rightarrow e^+e^-)$, background from the process $e^+e^- \rightarrow e^+e^-\gamma$, in which photons convert to e^+e^- pairs via interaction with the detector material and the resulting pairs are misidentified as $\pi^+\pi^-$, is suppressed by requiring $\mathcal{R}_e < 0.5$ and $\mathcal{L}_e < \mathcal{L}_\pi$ for pions. These conversion background events are further reduced by requiring the invariant mass of $\pi^+\pi^-$ to be larger than 0.35 GeV/c^2 . In $e^+e^- \rightarrow K^+K^-J/\psi(\rightarrow e^+e^-)$, the invariant mass of K^+K^- is required to be larger than 1.05 GeV/c^2 to veto γ conversion events and remove the events with a $\phi(\rightarrow K^+K^-)$ meson in the final state. The ISR events are identified by the requirement

$|M_{\text{recoil}}^2| < 1 (\text{GeV}/c^2)^2$, where $M_{\text{recoil}}^2 = (p_{\text{c.m.}} - p_{h^+} - p_{h^-} - p_{e^+} - p_{e^-})^2$. Here, p_i represents the four-momentum of the corresponding particle in the e^+e^- c.m. frame, and $p_{\text{c.m.}}$ is the four-momentum of the initial e^+e^- system. After event selection, the fraction of events with multiple candidates is zero in both the signal MC and data samples.

After applying all selection criteria, the h^+h^-J/ψ invariant mass distributions for the J/ψ candidates within the signal window, together with the backgrounds estimated from the normalized J/ψ mass sidebands, are shown in Fig. 1. These background events are employed to estimate the combinatorial background arising from non- J/ψ contributions. The background contamination due to cross-feed among the three signal channels has been examined and found to be negligible using MC simulated events. The remaining background comes mostly from processes that occur through two virtual photons such as $e^+e^- \rightarrow \gamma\gamma^*\gamma^* \rightarrow \gamma VV$, for example $e^+e^- \rightarrow \gamma\rho J/\psi$ and $e^+e^- \rightarrow \gamma\phi J/\psi$; however, these contributions have been calculated to be small [58]. We investigate them using MC simulations, confirming that their contributions are insignificant and can be neglected in this study. The events with a real J/ψ and a broad pseudoscalar resonance are considered as signal.

We observe an enhancement around 4.26 GeV in the $\pi^+\pi^-J/\psi$ invariant mass distribution, consistent with the $Y(4230/4320)$ structure previously reported by Belle [6,9] and BESIII [31,32]. In addition, the observed signal events around 4.1 GeV show an excess over the expected background, which is consistent with the predicted $\psi(4040)$ -like enhancement [34]. To investigate the presence of the $\psi(4040)$, we perform an unbinned extended maximum likelihood fit, as shown in Fig. 2. The fit range is restricted to the invariant mass below 4.16 GeV/c^2 in order to

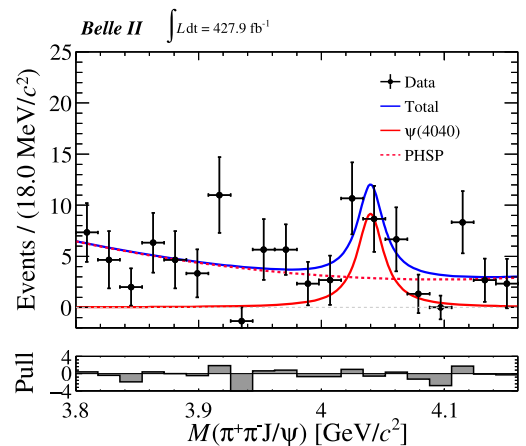


FIG. 2. Unbinned extended maximum likelihood fit to the invariant mass distribution of $\pi^+\pi^-J/\psi$ with the signal of $\psi(4040)$ state. The black dots with error bars are the $\pi^+\pi^-J/\psi$ signal candidates, obtained by subtracting the background estimated from the normalized J/ψ mass sidebands.

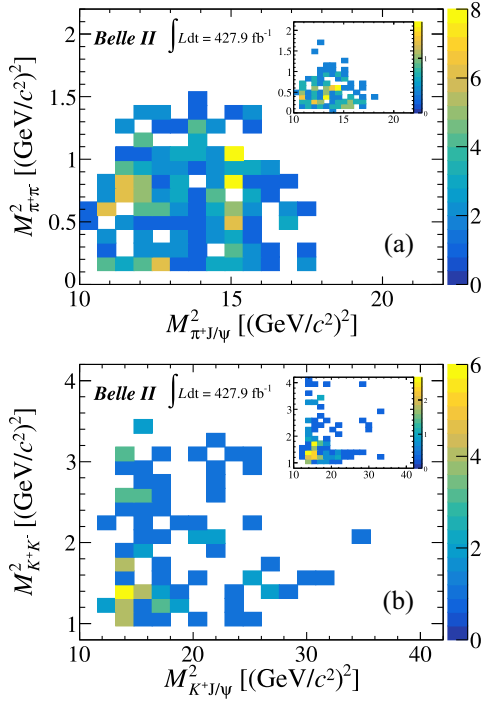


FIG. 3. Dalitz plots of (a) $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ in the $Y(4230/4320)$ region and (b) $e^+e^- \rightarrow K^+K^-J/\psi$ with $M(K^+K^-J/\psi) < 6.0 \text{ GeV}/c^2$. The insets show the background events from the normalized J/ψ mass sidebands.

suppress the effects of higher-mass resonances. The $\psi(4040)$ signal is modeled with a Breit-Wigner function, whose parameters are fixed to the world average values [26]. The background from non- J/ψ events is estimated using the normalized J/ψ mass sideband regions. A second-order Chebyshev polynomial is used to describe the PHSP $\pi^+\pi^-J/\psi$ production. The statistical significance of the $\psi(4040)$ state is found to be 2.0σ . For the K^+K^-J/ψ process, no significant structure is observed in the invariant mass distribution. No clear signal of $p\bar{p}J/\psi$ production is found.

IV. INTERMEDIATE STATE SEARCH

The presence of potential intermediate states is investigated by analyzing the projections of the Dalitz plots [59] for the selected h^+h^-J/ψ candidate events. Figure 3 presents the Dalitz plots in the J/ψ signal and sideband regions. In total 235 (43) events are obtained in the J/ψ signal (sideband) region for the process $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ in the $Y(4230/4320)$ region, defined as having $M(\pi^+\pi^-J/\psi)$ in the region $(4.15, 4.45) \text{ GeV}/c^2$, and 96 (43) events are obtained in the J/ψ signal (sideband) regions for the process $e^+e^- \rightarrow K^+K^-J/\psi$ with $M(K^+K^-J/\psi) < 6.0 \text{ GeV}/c^2$. For the $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ events in the $Y(4260)$ signal region, the $\pi^+\pi^-$ invariant mass distribution shown in Fig. 4 is similar to what was observed by Belle [6,9], where the contribution

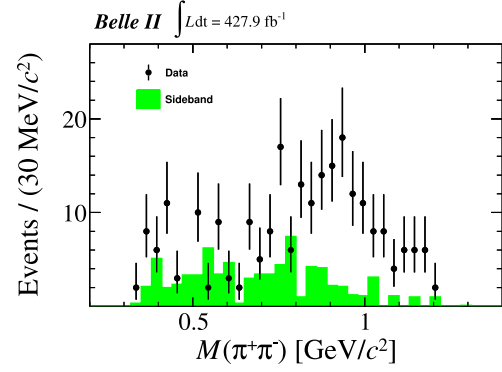


FIG. 4. Distribution of the $M(\pi^+\pi^-)$ in the $Y(4230/4320)$ region.

from the process $e^+e^- \rightarrow J/\psi f_0(980) (\rightarrow \pi^+\pi^-)$ can be seen. In addition, bandlike excesses around $M_{J/\psi\pi} = 3.9 \text{ GeV}/c^2$ are observed in the $\pi^\pm J/\psi$ system.

To investigate the bandlike excesses in the $\pi^\pm J/\psi$ system, we fit the distribution of $M_{\max}(\pi J/\psi)$, the maximum of $M(\pi^+J/\psi)$ and $M(\pi^-J/\psi)$ [9,60]. Figure 5 shows the distribution of $M_{\max}(\pi J/\psi)$ in the $Y(4230/4320)$ region. An unbinned extended maximum likelihood fit is

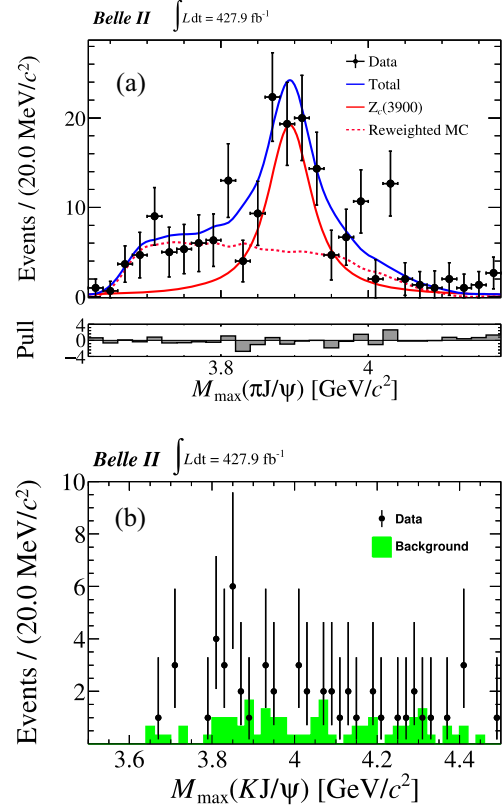


FIG. 5. (a) Unbinned extended maximum likelihood fit to the distribution of the $M_{\max}(\pi J/\psi)$ in the $Y(4230/4320)$ region. (b) The distribution of the $M_{\max}(KJ/\psi)$ with $M(K^+K^-J/\psi) < 6.0 \text{ GeV}/c^2$.

performed. The signal shape is parametrized as a Breit-Wigner function to describe $Z_c(3900)^\pm$, also known as $T_{c\bar{c}}(3900)^\pm$ [26], whose parameters are fixed using the previous result from Belle [9]. The signal shape is convolved with a Gaussian resolution function whose width is floating. The effect of cross feed from the J/ψ combined with a wrong π on the signal shape has been checked and found to be negligible. The background from fake J/ψ events is estimated using the normalized J/ψ mass sideband regions. This background is fixed in the fit but is subtracted in Fig. 5. Other contributions, such as those from PHSP $\pi^+\pi^-J/\psi$ events and processes involving intermediate states like $f_0(980)J/\psi$, are estimated using a $\pi^+\pi^-J/\psi M(\pi^+\pi^-)$ -reweighted MC shape. This MC shape is based on the measured distribution from BESIII [61] at $\sqrt{s} = 4.26$ GeV and is rescaled according to the available phase space. The fitted resolution is consistent with the MC simulation. The statistical significance is calculated by comparing the logarithmic likelihoods with and without the $Z_c(3900)^\pm$ signal, and including the change of the number of parameters in the fits [62]. The significance of the $Z_c(3900)^\pm$ state is found to be 5.6σ in the nominal fit.

We account for systematic uncertainties from the background estimation and from the signal shape in the fit results by using different fit configurations. A set of alternative fits is performed to estimate the uncertainties, including using the $Z_c(3900)^\pm$ resonant parameters measured by BESIII [15], modifying the background shape with a second-order polynomial or redefining the sideband regions, and accounting for the uncertainty associated with a floating mass resolution. We also use the $\pi^+\pi^-J/\psi$ PHSP MC samples and perform an alternative fit, to estimate the uncertainty due to possible intermediate states in the $\pi^+\pi^-$ system such as the $f_0(980)$ state. The largest contribution to the systematic uncertainties arises from the resonance parameters. In all instances, the statistical significance of the $Z_c(3900)^\pm$ state remains above 5.3σ . The Belle II detector has better resolution and higher trigger efficiency than the Belle detector, leading to higher selection efficiency for ISR events [63]. Additionally, we use prior knowledge to fix the resonance parameters in the fit [9]. As a result, our analysis reaches a significance for the $Z_c(3900)^\pm$ state comparable to Belle's, despite using a smaller data sample.

In $e^+e^- \rightarrow K^+K^-J/\psi$, the distribution of $M_{\max}(KJ/\psi)$ is presented in Fig. 5 and no obvious structure is found in the $K^\pm J/\psi$ system. The limited size of the sample impedes further extraction of information regarding the three-body dynamics.

V. CROSS SECTION MEASUREMENT

The energy-dependent cross sections of $e^+e^- \rightarrow h^+h^-J/\psi$ for $h = \pi/K/p$, from 3.8 GeV or the production

threshold to 5.5/6.0/7.0 GeV in steps of 20/40/100 MeV, are calculated using

$$\sigma_i = \frac{N_i^{\text{sig}}}{\mathcal{L}_i^{\text{eff}} \cdot \varepsilon_i \cdot \mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)}. \quad (1)$$

Here, $N_i^{\text{sig}} = \max(0, n_i^{\text{obs}} - f \times n_i^{\text{bkg}})$ [64,65], where n_i^{obs} , n_i^{bkg} , and $f = \frac{1}{3}$ are the number of observed events in J/ψ signal region in data, the number of background events determined from the J/ψ sidebands extracted from counting, and the ratio between the numbers of background events in the J/ψ signal region and sideband regions, respectively; $\mathcal{L}_i^{\text{eff}}$ is the effective ISR integrated luminosity obtained from the QED calculation [66] in the i th energy bin; $\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-) = 11.93\%$ is taken from world average value [26]. ε_i is the detection efficiency for the processes h^+h^-J/ψ corrected for PID and trigger efficiencies.

To estimate the detection efficiency, the binned efficiencies obtained from the $\pi^+\pi^-J/\psi$ PHSP signal MC samples are reweighted according to the Dalitz plot distributions measured from data in different energy regions. Specifically, the binned efficiency in each Dalitz plot bin i is defined as $\varepsilon_i = N_i^{\text{reco}}/N_i^{\text{truth}}$, where N_i^{reco} and N_i^{truth} are the reconstructed and generated signal yields in bin i , respectively. Due to the limited sample at some energy points, different binning schemes are adopted to ensure stable efficiency estimates: a 5×5 binning is used at $\sqrt{s} = 4.26$ GeV, while a 3×3 binning is used at other energies, in order to avoid negative yields after background subtraction. The data-driven detection efficiency is then calculated as $\varepsilon_{\text{data}} = \sum_i \varepsilon_i N_i^{\text{sig}}/N^{\text{sig}}$, where N_i^{sig} is the number of signal events in data in bin i , and N^{sig} is the total number of signal events after background subtraction. The background contribution is estimated using the J/ψ mass sideband. In particular, the $\pi^+\pi^-J/\psi$ MC sample at $\sqrt{s} = 3.686$ GeV uses the dynamic factor $f = (m_{\pi^+\pi^-}^2 - 4m_\pi^2)^2$ [67] for the $\pi^+\pi^-$ system to model the decay $\psi(2S) \rightarrow \pi^+\pi^-J/\psi$, by reweighting the $\pi^+\pi^-$ invariant mass distribution. The K^+K^-J/ψ signal MC samples are reweighted using the $M(K^+K^-)$ distribution from BESIII at $\sqrt{s} = 4.68$ GeV [37] and rescaled according to the variation of size of kinematic phase-space across different energy points, by assuming that the dynamics do not change with $\sqrt{s}$. For the $p\bar{p}J/\psi$ channel, the signal MC samples retain the PHSP model due to the lack of experimental measurements. The efficiency of each bin ε_i is obtained by fitting the efficiencies at eight energy points with a third-order polynomial function and then extrapolating the resulting efficiency curve for each channel. The systematic uncertainty arising from the h^+h^-J/ψ dynamics is discussed in a later section.

While the comparison of the Dalitz plot for $\psi(2S) \rightarrow \pi^+\pi^-J/\psi$ between the signal MC sample and data shows

good agreement, a significant discrepancy is observed in the $\cos\theta$ distribution of charged tracks in the control channel $e^+e^- \rightarrow \gamma_{\text{ISR}}\psi(2S)(\rightarrow \pi^+\pi^-J/\psi)$ between data and MC samples in the end-cap regions, where large discrepancies in PID efficiency between data and MC simulation are known to exist. A data-driven method utilizing the control channel of $e^+e^- \rightarrow \gamma_{\text{ISR}}\psi(2S)(\rightarrow \pi^+\pi^-J/\psi)$ is employed to reduce the data-MC discrepancy. The difference between data and MC samples is measured in different polar angle regions for electrons, muons, and pions, and the MC samples are reweighted to match the data. Since the events are well simulated in the barrel region, we scale the MC distributions by the ratio of data to MC yields in the central region ($-0.4 < \cos\theta < 0.6$ in the lab frame). Due to the limited size of the control sample, we first apply a 1D reweighting to the $\cos\theta_\ell$ ($\ell = e/\mu$) distributions. The overall reweighting factors for $\mu^+\mu^-$ and e^+e^- modes are 0.874 and 0.819. After applying the correction factor for the $\cos\theta_\ell$ distributions, we then perform a 1D reweighting on the $\cos\theta_\pi$ distributions. The second reweighting factors for $\mu^+\mu^-$ and e^+e^- modes are 0.967 and 0.961. A momentum-dependent correction is not considered due to limited statistics and weak $M(\pi^+\pi^-J/\psi)$ dependence of the track momentum distributions in the mass region of interest. After performing two 1D reweightings, we examined the $\cos\theta_\ell$, $\cos\theta_\pi$ and other kinematic distributions and found them to be consistent between data and MC simulations.

The 68.3% central confidence interval on N_i^{sig} for the h^+h^-J/ψ measurements, and the additional 90% CL upper limit on N_i^{sig} for the $p\bar{p}J/\psi$ measurement, are estimated using the TRolke method [68,69], a frequentist approach that includes systematic uncertainties (Sec. VI). Figure 6 shows the calculated cross sections and the upper limits of cross sections for $e^+e^- \rightarrow h^+h^-J/\psi$, where the error bars include both statistical and systematic uncertainties. Utilizing the combined number of signal and background events measured by Belle [9,40], along with the total luminosity and the efficiency weighted by luminosity, we calculate combined cross sections and associated uncertainties at the 68.27% CL for σ_i . Figure 6 also presents the previous results from Belle [9,40] along with the combined results.

VI. SYSTEMATIC UNCERTAINTIES

The sources of systematic uncertainty associated with the cross section measurements are listed in Table I. The uncertainty in tracking efficiency is measured to be 0.3% per track based on studies using control samples of $e^+e^- \rightarrow \tau^+\tau^-$, where one tau lepton decays leptonically ($\tau^\pm \rightarrow \ell^\pm \nu_\ell \bar{\nu}_\tau$, $\ell = e, \mu$) while the other decays hadronically into three charged pions ($\tau^\mp \rightarrow 3\pi^\mp \nu_\tau n\pi^0$, $n \geq 0$). For the four-track final states in this analysis, the total uncertainty is therefore 1.2%. The trigger efficiencies in the

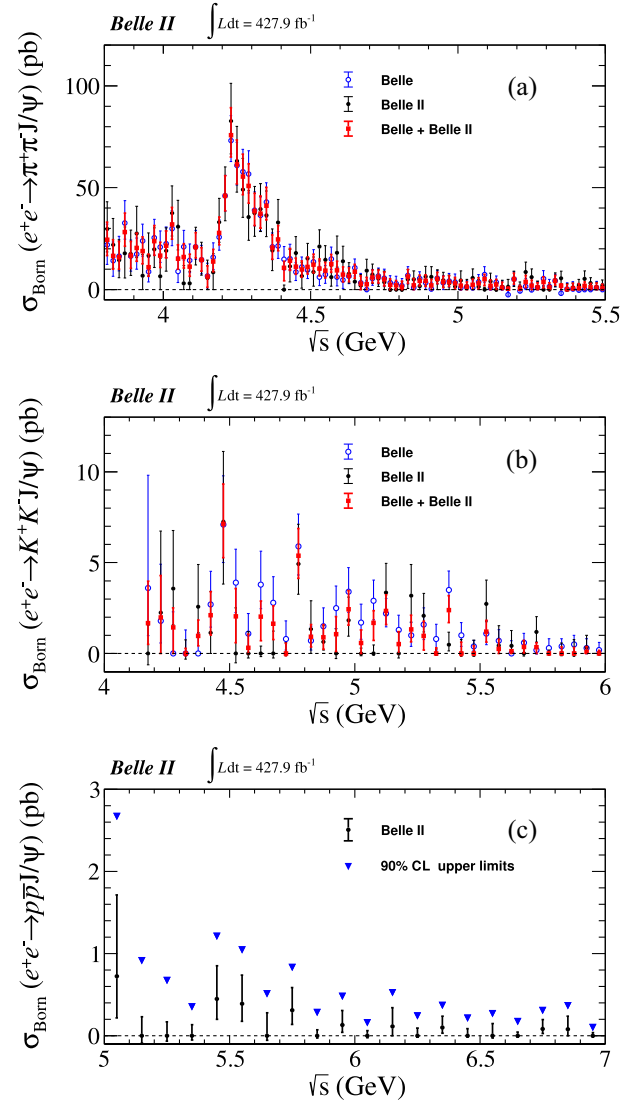


FIG. 6. Measured Born cross sections of (a) $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ for $\sqrt{s}$ between 3.8 and 5.5 GeV, (b) $e^+e^- \rightarrow K^+K^-J/\psi$ for $\sqrt{s}$ between 4.0 and 6.0 GeV, and (c) $e^+e^- \rightarrow p\bar{p}J/\psi$ for $\sqrt{s}$ between 5.0 and 7.0 GeV. The error bars include both statistical and systematic uncertainties. The blue open circles with error bars in panels (a) and (b) represent the Belle results [9,40], while the red full squares with error bars indicate the combined results. The blue inverted triangles (c) are 90% CL upper limits for the measured cross sections of $e^+e^- \rightarrow p\bar{p}J/\psi$.

CDC, ECL, and KLM are evaluated with the control samples $e^+e^- \rightarrow \gamma_{\text{ISR}}\psi(2S)$ and $e^+e^- \rightarrow \gamma\mu^+\mu^-$, with the statistical uncertainty of 0.7% for the correction factor included as the trigger uncertainty. The integrated luminosity contributes an uncertainty of 0.5% [42]. The uncertainty for $\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)$ is considered to be 0.4%, calculated by combining the errors of the world averages for the e^+e^- and $\mu^+\mu^-$ modes [26].

The statistical uncertainty of the reweighting correction factor is calculated to be 6.5%, and considered as the $\cos\theta$ -

TABLE I. Multiplicative relative systematic uncertainties in the cross section measurements of $e^+e^- \rightarrow h^+h^-J/\psi$. Uncertainties are quoted in percent and are common for all data points.

Source	$\pi^+\pi^-J/\psi$	K^+K^-J/ψ	$p\bar{p}J/\psi$
Tracking	1.2	1.2	1.2
Trigger	0.7	0.7	0.7
Luminosity	0.5	0.5	0.5
$\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)$	0.4	0.4	0.4
$\cos\theta$	6.5	6.5	6.5
PID	0.7	3.1	1.5
$M(h^+h^-)$ modeling	4.0	4.0	7.0
MC sample size	0.3	0.3	0.3
Total multiplicative	7.8	8.4	9.8

related uncertainty. The uncertainty associated with this method can be reduced by increasing the size of the control sample in the future. The systematic uncertainties of PID efficiency in the central region are estimated from data and MC samples of leptons and hadrons in $J/\psi \rightarrow \ell^+\ell^-$, $e^+e^- \rightarrow e^+e^-\ell^+\ell^-$, $e^+e^- \rightarrow \tau^\pm(\rightarrow 3\pi^\pm\nu_\tau)\tau^\mp(\rightarrow \ell^\mp\bar{\nu}_\ell\nu_\tau)$, $e^+e^- \rightarrow \mu^+\mu^-\gamma$, $K_S^0 \rightarrow \pi^+\pi^-$, $D^{*+} \rightarrow \pi^+D^0(\rightarrow K^-\pi^+)$, and $\Lambda \rightarrow p\pi^-$ [70]. The uncertainties in the total electron, muon, pion, kaon, and proton identification efficiencies are estimated to be approximately 0.7%, 0.2%, 0.1%, 3.0%, and 1.3%, respectively, taking into account the momentum and polar angle dependence of the tracks [57]. The overall PID uncertainties are reported as 0.7%, 3.1%, and 1.5% for $\pi^+\pi^-J/\psi$, K^+K^-J/ψ , and $p\bar{p}J/\psi$, respectively.

The uncertainties arising from the MC generator are related to the dynamics of three-body decays. The uncertainty arising from the modeling of the $M(\pi^+\pi^-)$ and $M(K^+K^-)$ distributions is estimated by comparing with the corresponding PHSP spectrum models. The uncertainty related to the modeling of the $M(p\bar{p})$ distribution is evaluated by comparing with a reweighted $M(p\bar{p})$ spectrum model, which is constructed based on the $M(\pi^+\pi^-/K^+K^-)$ results from BESIII and rescaled according to the available size of kinematic phase space [37,61]. The resulting efficiencies are higher by 1% to 7%, depending on the energy point. We use the maximum deviation across all energies in each channel to quote conservative

uncertainties of 4%, 4%, and 7% for $\pi^+\pi^-J/\psi$, K^+K^-J/ψ , and $p\bar{p}J/\psi$, respectively. The MC statistical error on the efficiency is 0.3%. To evaluate the uncertainty arising from the background estimation, we varied the sideband regions used for background determination. The largest difference in the background level among these variations is taken as the uncertainty, which is 3.6%, 4.3%, and 9.5% for the channels $\pi^+\pi^-J/\psi$, K^+K^-J/ψ , and $p\bar{p}J/\psi$, respectively.

Assuming that all sources except for the background estimation are independent, they are combined in quadrature to yield the total multiplicative systematic uncertainty associated with the cross section measurements. The uncertainty arising from background estimation is treated as additive. It is incorporated by varying the number of background events by $\pm 1\sigma$ and taking the largest resulting uncertainty as a conservative estimate within the TRolke statistical method. The final uncertainty thus includes statistical, additive, and multiplicative systematic uncertainties. For the combined results, we combine the multiplicative systematic uncertainties from Belle and Belle II in quadrature, assuming the systematic uncertainties are uncorrelated. This assumption has a negligible impact because the measurements from the two experiments are mainly limited by statistical uncertainties.

To validate our analysis, we also measured the ISR $\psi(2S)$ production rate using the same selection criteria. The cross sections are determined to be $(13.8 \pm 0.2 \pm 0.9)$ pb and $(14.8 \pm 0.2 \pm 1.0)$ pb at $\sqrt{s} = 10.58$ GeV for the $\mu^+\mu^-$ and e^+e^- modes, respectively. The systematic uncertainties here, except for those from the $M(h^+h^-)$ modeling, are the same as those listed in Table I. The uncertainty in the $M(h^+h^-)$ modeling is estimated by varying the dynamic factor for the $\pi^+\pi^-$ system. An additional uncertainty from $\mathcal{B}[\psi(2S) \rightarrow \pi^+\pi^-J/\psi]$ is taken from the world averages [26]. These measurements are consistent within uncertainties with the predicted value of (13.6 ± 0.4) pb at $\sqrt{s} = 10.58$ GeV from Ref. [66], as well as with previous measurements [6,9].

Tables II–IV summarize the final results along with all the relevant information used in the cross section measurements or upper limit calculations for $e^+e^- \rightarrow \pi^+\pi^-J/\psi$, $e^+e^- \rightarrow K^+K^-J/\psi$, and $e^+e^- \rightarrow p\bar{p}J/\psi$, respectively.

TABLE II. Summary of cross sections (σ) of $e^+e^- \rightarrow \pi^+\pi^-J/\psi$. We also list the e^+e^- c.m. energy ($\sqrt{s}$), number of observed events (n^{obs}), number of backgrounds estimated from the normalized J/ψ mass sidebands (n^{bkg}), detection efficiency (ϵ), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for a 20 MeV bin size and $\sqrt{s}$ is the central value of the bin. The uncertainties include both statistical and systematic contributions.

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
3.810	9	1	7.1	31.9	$29.8^{+13.4}_{-11.3}$	4.670	4	3	10.4	42.8	$1.9^{+5.4}_{-1.9}$
3.830	8	2	7.1	32.2	$22.0^{+12.9}_{-11.5}$	4.690	6	1	10.5	43.1	$9.3^{+5.6}_{-4.7}$
3.850	5	1	7.2	32.4	$14.4^{+10.1}_{-8.6}$	4.710	5	1	10.6	43.4	$7.3^{+5.1}_{-4.4}$

(Table continued)

TABLE II. (Continued)

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
3.870	8	3	7.2	32.6	$17.7^{+13.0}_{-12.1}$	4.730	4	1	10.7	43.7	$5.4^{+4.6}_{-4.0}$
3.890	7	2	7.3	32.8	$17.5^{+11.7}_{-10.5}$	4.750	5	3	10.8	44.0	$3.5^{+5.5}_{-3.5}$
3.910	10	2	7.4	33.1	$27.5^{+13.4}_{-11.8}$	4.770	3	3	10.9	44.3	$0.0^{+4.6}_{-0.9}$
3.930	5	3	7.4	33.3	$6.8^{+10.5}_{-6.8}$	4.790	2	3	10.9	44.6	$0.0^{+2.3}_{-0.5}$
3.950	7	2	7.5	33.5	$16.7^{+11.2}_{-10.0}$	4.810	2	2	11.0	44.9	$0.0^{+3.7}_{-0.7}$
3.970	7	1	7.6	33.8	$19.7^{+10.5}_{-8.9}$	4.830	5	2	11.1	45.2	$5.0^{+4.9}_{-4.5}$
3.990	4	2	7.6	34.0	$6.5^{+8.8}_{-6.5}$	4.850	4	1	11.2	45.5	$4.9^{+4.2}_{-3.6}$
4.010	8	2	7.7	34.2	$19.1^{+11.2}_{-10.0}$	4.870	3	2	11.3	45.8	$1.6^{+4.0}_{-1.6}$
4.030	13	1	7.8	34.5	$37.5^{+13.3}_{-11.3}$	4.890	6	2	11.4	46.1	$6.4^{+5.0}_{-4.5}$
4.050	12	2	7.9	34.7	$30.8^{+12.9}_{-11.4}$	4.910	6	2	11.5	46.4	$6.3^{+4.9}_{-4.5}$
4.070	4	3	7.9	34.9	$3.0^{+8.7}_{-3.0}$	4.930	6	3	11.6	46.7	$4.6^{+5.1}_{-4.6}$
4.090	2	1	8.0	35.2	$3.0^{+5.9}_{-3.0}$	4.950	4	1	11.7	47.1	$4.6^{+3.9}_{-3.3}$
4.110	8	1	8.1	35.4	$20.5^{+10.0}_{-8.4}$	4.970	4	2	11.8	47.4	$3.0^{+4.1}_{-3.0}$
4.130	6	1	8.1	35.6	$14.4^{+8.7}_{-7.4}$	4.990	3	2	11.9	47.7	$1.5^{+3.6}_{-1.5}$
4.150	5	3	8.2	35.9	$5.7^{+8.8}_{-5.7}$	5.010	6	3	12.1	48.0	$4.3^{+4.8}_{-4.3}$
4.170	6	3	8.3	36.1	$8.4^{+9.2}_{-8.4}$	5.030	3	2	12.2	48.4	$1.4^{+3.5}_{-1.4}$
4.190	13	1	8.4	36.4	$33.1^{+11.7}_{-9.9}$	5.050	6	2	12.3	48.7	$5.6^{+4.4}_{-4.0}$
4.210	19	2	8.4	36.6	$46.1^{+14.1}_{-12.3}$	5.070	3	2	12.4	49.0	$1.4^{+3.4}_{-1.4}$
4.230	33	2	8.5	36.9	$82.7^{+18.5}_{-16.2}$	5.090	1	2	12.5	49.4	$0.0^{+1.1}_{-0.2}$
4.250	28	4	8.6	37.1	$63.0^{+17.0}_{-15.2}$	5.110	5	2	12.6	49.7	$4.0^{+3.9}_{-3.6}$
4.270	23	4	8.7	37.4	$49.1^{+15.2}_{-13.7}$	5.130	3	3	12.7	50.1	$0.0^{+3.5}_{-0.7}$
4.290	17	3	8.8	37.6	$35.6^{+12.8}_{-11.4}$	5.150	3	2	12.8	50.4	$1.3^{+3.2}_{-1.3}$
4.310	18	3	8.8	37.9	$37.6^{+13.0}_{-11.5}$	5.170	4	3	12.9	50.8	$1.3^{+3.7}_{-1.3}$
4.330	18	2	8.9	38.1	$39.4^{+12.5}_{-10.9}$	5.190	6	2	13.0	51.1	$5.0^{+4.0}_{-3.6}$
4.350	17	2	9.0	38.4	$36.4^{+12.0}_{-10.5}$	5.210	2	1	13.1	51.5	$1.2^{+2.5}_{-1.2}$
4.370	12	4	9.1	38.7	$19.1^{+10.6}_{-9.8}$	5.230	10	3	13.2	51.8	$8.6^{+4.9}_{-4.5}$
4.390	16	2	9.2	38.9	$32.9^{+11.3}_{-9.9}$	5.250	7	2	13.4	52.2	$6.0^{+4.0}_{-3.6}$
4.410	2	5	9.2	39.2	$0.0^{+2.2}_{-0.4}$	5.270	3	2	13.5	52.5	$1.2^{+2.9}_{-1.2}$
4.430	8	3	9.3	39.5	$11.4^{+8.3}_{-7.7}$	5.290	2	3	13.6	52.9	$0.0^{+1.6}_{-0.3}$
4.450	9	1	9.4	39.7	$17.9^{+8.1}_{-6.8}$	5.310	3	4	13.7	53.3	$0.0^{+2.1}_{-0.4}$
4.470	5	2	9.5	40.0	$6.6^{+6.5}_{-6.0}$	5.330	6	2	13.8	53.7	$4.5^{+3.6}_{-3.2}$
4.490	8	1	9.6	40.3	$15.2^{+7.4}_{-6.2}$	5.350	6	1	13.9	54.0	$5.6^{+3.4}_{-2.8}$
4.510	7	3	9.7	40.5	$8.6^{+7.5}_{-7.0}$	5.370	3	3	14.0	54.4	$0.0^{+2.9}_{-0.6}$
4.530	11	1	9.8	40.8	$21.1^{+8.3}_{-7.0}$	5.390	2	1	14.2	54.8	$1.1^{+2.1}_{-1.1}$
4.550	8	1	9.8	41.1	$14.5^{+7.1}_{-6.0}$	5.410	4	2	14.3	55.2	$2.1^{+2.9}_{-2.1}$
4.570	4	1	9.9	41.4	$6.1^{+5.2}_{-4.5}$	5.430	8	3	14.4	55.6	$5.2^{+3.8}_{-3.6}$
4.590	11	2	10.0	41.6	$18.1^{+8.1}_{-7.1}$	5.450	4	1	14.5	56.0	$3.1^{+2.6}_{-2.3}$
4.610	9	2	10.1	41.9	$13.8^{+7.3}_{-6.5}$	5.470	3	2	14.6	56.4	$1.0^{+2.5}_{-1.0}$
4.630	5	1	10.2	42.2	$7.8^{+5.4}_{-4.6}$	5.490	4	2	14.8	56.8	$2.0^{+2.7}_{-2.0}$
4.650	4	2	10.3	42.5	$3.8^{+5.2}_{-3.8}$						

TABLE III. Summary of cross sections (σ) of $e^+e^- \rightarrow K^+K^-J/\psi$. We also list the e^+e^- c.m. energy ($\sqrt{s}$), number of observed events (n^{obs}), number of backgrounds estimated from the normalized J/ψ mass sidebands (n^{bkg}), detection efficiency (ϵ), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for a 50 MeV bin size and $\sqrt{s}$ is the central value of the bin. The uncertainties include both statistical and systematic contributions.

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
4.175	0	0	3.0	90.5	$0.00^{+1.56}_{-0.62}$	5.125	6	0	12.0	124.9	$3.35^{+1.61}_{-1.20}$
4.225	2	1	4.0	92.0	$2.26^{+4.48}_{-2.26}$	5.175	2	2	12.1	127.1	$0.00^{+1.19}_{-0.24}$
4.275	2	0	5.0	93.6	$3.58^{+3.20}_{-1.98}$	5.225	7	1	12.2	129.3	$3.19^{+1.72}_{-1.45}$
4.325	0	1	5.9	95.2	$0.00^{+0.75}_{-0.30}$	5.275	4	0	12.3	131.6	$2.07^{+1.24}_{-0.88}$
4.375	2	0	6.7	96.8	$2.58^{+2.31}_{-1.43}$	5.325	0	1	12.4	133.9	$0.00^{+0.25}_{-0.10}$
4.425	2	1	7.4	98.5	$1.15^{+2.28}_{-1.15}$	5.375	1	0	12.5	136.3	$0.49^{+0.67}_{-0.34}$
4.475	9	2	8.1	100.2	$7.25^{+3.87}_{-3.43}$	5.425	1	1	12.6	138.7	$0.00^{+0.77}_{-0.15}$
4.525	3	3	8.7	101.9	$0.00^{+2.51}_{-0.50}$	5.475	1	1	12.7	141.1	$0.00^{+0.75}_{-0.15}$
4.575	2	3	9.2	103.6	$0.00^{+1.21}_{-0.24}$	5.525	6	0	12.8	143.7	$2.73^{+1.31}_{-0.98}$
4.625	0	1	9.7	105.4	$0.00^{+0.41}_{-0.16}$	5.575	3	2	13.0	146.2	$0.44^{+1.09}_{-0.44}$
4.675	1	1	10.1	107.2	$0.00^{+1.24}_{-0.25}$	5.625	2	1	13.2	148.9	$0.43^{+0.85}_{-0.43}$
4.725	1	2	10.4	109.0	$0.00^{+0.60}_{-0.12}$	5.675	1	1	13.4	151.6	$0.00^{+0.66}_{-0.13}$
4.775	7	0	10.7	110.9	$4.93^{+2.18}_{-1.66}$	5.725	3	0	13.7	154.3	$1.19^{+0.84}_{-0.57}$
4.825	3	1	11.0	112.7	$1.35^{+1.55}_{-1.35}$	5.775	0	1	14.0	157.2	$0.00^{+0.19}_{-0.08}$
4.875	1	0	11.3	114.7	$0.65^{+0.89}_{-0.45}$	5.825	1	1	14.3	160.1	$0.00^{+0.58}_{-0.12}$
4.925	2	2	11.5	116.7	$0.00^{+1.37}_{-0.27}$	5.875	2	2	14.7	163.0	$0.00^{+0.76}_{-0.15}$
4.975	3	0	11.6	118.7	$1.82^{+1.29}_{-0.87}$	5.925	2	1	15.1	166.1	$0.33^{+0.66}_{-0.33}$
5.025	0	0	11.8	120.7	$0.00^{+0.29}_{-0.12}$	5.975	0	0	15.6	169.2	$0.00^{+0.16}_{-0.06}$
5.075	1	2	11.9	122.8	$0.00^{+0.47}_{-0.09}$						

TABLE IV. Summary of cross sections (σ) and upper limit at 90% CL of cross sections $\sigma^{\text{U.L.}}$ of $e^+e^- \rightarrow p\bar{p}J/\psi$. We also list the e^+e^- c.m. energy ($\sqrt{s}$), number of observed events (n^{obs}), number of backgrounds estimated from the normalized J/ψ mass sidebands (n^{bkg}), detection efficiency (ϵ), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for a 100 MeV bin size and $\sqrt{s}$ is the central value of the bin. The uncertainties include both statistical and systematic contributions.

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sigma^{\text{U.L.}}$ (pb)
5.050	1	0	4.8	243.5	$0.72^{+0.99}_{-0.50}$	2.67
5.150	0	0	7.3	252.0	$0.00^{+0.23}_{-0.09}$	0.91
5.250	0	0	9.5	260.9	$0.00^{+0.17}_{-0.07}$	0.67
5.350	0	1	11.6	270.1	$0.00^{+0.13}_{-0.05}$	0.35
5.450	2	0	13.3	279.8	$0.45^{+0.40}_{-0.25}$	1.21
5.550	2	0	14.9	289.9	$0.39^{+0.35}_{-0.21}$	1.04
5.650	1	1	16.3	300.4	$0.00^{+0.28}_{-0.06}$	0.51
5.750	2	0	17.5	311.5	$0.31^{+0.28}_{-0.17}$	0.83
5.850	0	0	18.5	323.1	$0.00^{+0.07}_{-0.03}$	0.28
5.950	1	0	19.3	335.3	$0.13^{+0.18}_{-0.09}$	0.48
6.050	0	1	20.1	348.0	$0.00^{+0.06}_{-0.02}$	0.16
6.150	2	1	20.6	361.5	$0.11^{+0.23}_{-0.11}$	0.52

(Table continued)

TABLE IV. (*Continued*)

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sigma^{\text{U.L.}}$ (pb)
6.250	1	2	21.1	375.6	$0.00^{+0.09}_{-0.02}$	0.24
6.350	1	0	21.5	390.6	$0.10^{+0.14}_{-0.07}$	0.37
6.450	1	2	21.7	406.3	$0.00^{+0.08}_{-0.02}$	0.21
6.550	1	1	21.9	423.0	$0.00^{+0.15}_{-0.03}$	0.27
6.650	0	0	22.1	440.6	$0.00^{+0.04}_{-0.02}$	0.17
6.750	1	0	22.2	459.3	$0.08^{+0.11}_{-0.06}$	0.30
6.850	2	1	22.2	479.1	$0.08^{+0.16}_{-0.08}$	0.37
6.950	0	1	22.3	500.1	$0.00^{+0.04}_{-0.02}$	0.10

TABLE V. Combined cross sections σ of $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ of Belle [9] and Belle II measurements. We also list the e^+e^- c.m. energy ($\sqrt{s}$), number of observed events (n^{obs}), number of backgrounds estimated from the normalized J/ψ mass sidebands (n^{bkg}), detection efficiency (ϵ), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for a 20 MeV bin size and $\sqrt{s}$ is the central value of the bin. The uncertainties include both statistical and systematic contributions.

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
3.810	30	9	6.9	104.1	$24.40^{+8.68}_{-7.80}$	4.670	19	13	11.1	139.5	$2.87^{+3.76}_{-2.87}$
3.830	24	9	7.1	104.8	$16.56^{+7.91}_{-6.55}$	4.690	18	13	11.2	140.4	$2.66^{+3.29}_{-2.66}$
3.850	23	8	7.2	105.6	$15.75^{+7.85}_{-5.76}$	4.710	21	9	11.3	141.4	$5.96^{+3.65}_{-2.72}$
3.870	35	8	7.4	106.3	$28.18^{+9.36}_{-6.91}$	4.730	21	9	11.3	142.4	$6.23^{+3.26}_{-3.04}$
3.890	24	8	7.5	107.0	$16.69^{+6.90}_{-6.27}$	4.750	23	13	11.4	143.3	$4.96^{+3.66}_{-3.19}$
3.910	28	8	7.6	107.8	$20.34^{+7.28}_{-6.52}$	4.770	14	9	11.5	144.3	$2.37^{+2.86}_{-2.37}$
3.930	27	8	7.8	108.5	$18.87^{+6.97}_{-6.27}$	4.790	15	12	11.5	145.3	$2.00^{+2.36}_{-2.00}$
3.950	19	7	7.9	109.3	$10.99^{+6.33}_{-4.57}$	4.810	13	10	11.6	146.3	$1.32^{+2.77}_{-1.32}$
3.970	35	10	8.0	110.0	$23.70^{+7.73}_{-6.92}$	4.830	26	13	11.6	147.3	$6.36^{+3.51}_{-3.32}$
3.990	27	9	8.2	110.8	$16.69^{+6.56}_{-5.95}$	4.850	18	13	11.7	148.3	$2.09^{+3.31}_{-2.09}$
4.010	32	8	8.3	111.5	$21.48^{+7.28}_{-5.88}$	4.870	17	8	11.8	149.3	$4.30^{+2.70}_{-2.54}$
4.030	45	9	8.4	112.3	$31.99^{+8.37}_{-7.30}$	4.890	19	10	11.8	150.3	$4.25^{+2.87}_{-2.74}$
4.050	28	10	8.5	113.1	$15.09^{+6.90}_{-5.19}$	4.910	15	10	11.9	151.3	$2.02^{+2.90}_{-2.02}$
4.070	29	10	8.6	113.9	$15.93^{+6.59}_{-5.45}$	4.930	21	9	11.9	152.4	$5.23^{+3.20}_{-2.39}$
4.090	24	10	8.7	114.6	$11.16^{+6.19}_{-4.68}$	4.950	19	11	12.0	153.4	$3.65^{+2.81}_{-2.71}$
4.110	34	8	8.8	115.4	$20.80^{+7.08}_{-5.22}$	4.970	19	10	12.0	154.5	$3.76^{+3.04}_{-2.31}$
4.130	29	11	9.0	116.2	$14.50^{+5.99}_{-5.50}$	4.990	20	13	12.1	155.5	$2.97^{+3.02}_{-2.66}$
4.150	22	14	9.1	117.0	$6.33^{+5.34}_{-5.22}$	5.010	17	12	12.1	156.6	$1.91^{+2.93}_{-1.91}$
4.170	29	11	9.2	117.8	$13.73^{+6.04}_{-5.05}$	5.030	14	11	12.2	157.7	$1.31^{+2.40}_{-1.31}$
4.190	46	9	9.3	118.6	$27.74^{+7.80}_{-5.84}$	5.050	17	11	12.2	158.8	$2.30^{+2.83}_{-2.20}$
4.210	69	7	9.4	119.4	$46.04^{+9.88}_{-7.45}$	5.070	20	13	12.3	159.8	$2.98^{+2.74}_{-2.69}$
4.230	111	8	9.4	120.2	$75.77^{+13.44}_{-10.79}$	5.090	23	12	12.4	161.0	$5.06^{+2.42}_{-3.13}$
4.250	98	13	9.5	121.0	$61.46^{+11.93}_{-9.67}$	5.110	19	14	12.4	162.1	$1.81^{+2.94}_{-1.81}$
4.270	90	12	9.6	121.9	$55.47^{+11.03}_{-8.93}$	5.130	17	11	12.5	163.2	$2.47^{+2.43}_{-2.38}$

(Table continued)

TABLE V. (*Continued*)

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
4.290	88	15	9.7	122.7	$50.84^{+10.89}_{-8.45}$	5.150	15	12	12.5	164.3	$0.95^{+2.61}_{-0.95}$
4.310	68	12	9.8	123.5	$38.51^{+8.78}_{-7.14}$	5.170	12	15	12.6	165.4	$0.40^{+0.67}_{-0.40}$
4.330	68	13	9.9	124.4	$37.24^{+8.64}_{-7.05}$	5.190	25	12	12.6	166.6	$5.06^{+2.92}_{-2.50}$
4.350	72	10	10.0	125.2	$41.15^{+9.08}_{-6.92}$	5.210	11	11	12.7	167.8	$0.39^{+1.62}_{-0.39}$
4.370	45	14	10.1	126.0	$20.49^{+6.30}_{-5.65}$	5.230	28	18	12.7	168.9	$3.77^{+3.15}_{-2.82}$
4.390	50	12	10.1	126.9	$24.53^{+6.80}_{-5.57}$	5.250	20	15	12.8	170.1	$1.93^{+2.55}_{-1.93}$
4.410	29	15	10.2	127.8	$10.69^{+3.20}_{-6.38}$	5.270	14	11	12.8	171.3	$1.02^{+2.23}_{-1.02}$
4.430	38	15	10.3	128.6	$14.13^{+5.94}_{-4.65}$	5.290	25	16	12.9	172.5	$3.65^{+2.49}_{-2.93}$
4.450	25	7	10.4	129.5	$11.22^{+4.18}_{-3.74}$	5.310	19	17	12.9	173.7	$1.00^{+2.24}_{-1.00}$
4.470	25	9	10.5	130.4	$9.84^{+4.19}_{-3.83}$	5.330	23	11	13.0	174.9	$4.32^{+2.59}_{-2.20}$
4.490	28	9	10.5	131.3	$11.12^{+4.77}_{-3.55}$	5.350	14	12	13.0	176.1	$1.83^{+0.95}_{-1.83}$
4.510	33	12	10.6	132.2	$12.16^{+5.18}_{-3.97}$	5.370	15	14	13.0	177.4	$0.12^{+2.38}_{-0.12}$
4.530	29	11	10.7	133.0	$10.23^{+4.78}_{-3.64}$	5.390	18	16	13.1	178.6	$0.48^{+2.55}_{-0.48}$
4.550	25	9	10.7	134.0	$9.32^{+3.96}_{-3.63}$	5.410	16	14	13.1	179.9	$0.71^{+2.14}_{-0.71}$
4.570	33	11	10.8	134.9	$12.45^{+4.76}_{-3.95}$	5.430	16	11	13.2	181.1	$1.75^{+2.02}_{-1.75}$
4.590	29	12	10.9	135.8	$9.45^{+4.44}_{-3.75}$	5.450	15	12	13.2	182.4	$1.04^{+1.99}_{-1.04}$
4.610	24	11	11.0	136.7	$7.28^{+3.81}_{-3.57}$	5.470	18	15	13.3	183.7	$0.92^{+2.30}_{-0.92}$
4.630	22	9	11.0	137.6	$6.82^{+3.91}_{-2.91}$	5.490	15	13	13.3	185.0	$0.68^{+1.98}_{-0.68}$
4.650	24	8	11.1	138.6	$8.73^{+3.61}_{-3.28}$						

TABLE VI. Combined cross sections σ of $e^+e^- \rightarrow K^+K^-J/\psi$ of Belle [40] and Belle II measurements. We also list the e^+e^- c.m. energy ($\sqrt{s}$), number of observed events (n^{obs}), number of backgrounds estimated from the normalized J/ψ mass sidebands (n^{bkg}), detection efficiency (ϵ), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for a 50 MeV bin size and $\sqrt{s}$ is the central value of the bin. The uncertainties include both statistical and systematic contributions.

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ϵ (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
4.175	1	0	1.7	297.5	$1.67^{+2.31}_{-1.17}$	5.125	15	2	11.3	410.9	$2.34^{+0.88}_{-0.75}$
4.225	3	1	2.8	302.0	$1.99^{+2.30}_{-1.99}$	5.175	8	5	11.5	418.1	$0.52^{+0.69}_{-0.52}$
4.275	3	2	3.8	307.6	$1.44^{+1.07}_{-1.44}$	5.225	12	4	11.8	425.3	$1.34^{+0.76}_{-0.70}$
4.325	0	1	4.7	313.2	$0.00^{+0.29}_{-0.11}$	5.275	13	7	12.0	432.6	$0.97^{+0.81}_{-0.78}$
4.375	2	0	5.5	317.8	$0.97^{+0.88}_{-0.54}$	5.325	6	8	12.3	439.9	$0.00^{+0.31}_{-0.06}$
4.425	6	1	6.2	323.5	$2.10^{+1.30}_{-1.08}$	5.375	18	2	12.6	447.3	$2.39^{+0.81}_{-0.68}$
4.475	21	2	6.8	329.2	$7.12^{+2.20}_{-1.86}$	5.425	8	8	12.8	455.7	$0.00^{+0.63}_{-0.13}$
4.525	11	5	7.4	334.9	$2.04^{+1.53}_{-1.44}$	5.475	4	4	13.0	464.1	$0.00^{+0.42}_{-0.08}$
4.575	5	5	7.9	340.6	$0.31^{+0.76}_{-0.31}$	5.525	13	4	13.3	471.7	$1.20^{+0.63}_{-0.57}$
4.625	9	3	8.3	346.4	$2.04^{+0.86}_{-1.33}$	5.575	8	6	13.6	480.2	$0.26^{+0.53}_{-0.26}$
4.675	8	2	8.7	352.2	$1.64^{+0.99}_{-0.87}$	5.625	5	7	13.8	488.9	$0.12^{+0.09}_{-0.12}$
4.725	4	5	9.1	358.0	$0.00^{+0.57}_{-0.11}$	5.675	5	2	14.1	497.6	$0.36^{+0.36}_{-0.33}$
4.775	23	1	9.4	363.9	$5.38^{+1.50}_{-1.24}$	5.725	5	3	14.3	507.3	$0.35^{+0.25}_{-0.35}$

(Table continued)

TABLE VI. (Continued)

$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ε (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)	$\sqrt{s}$ (GeV)	n^{obs}	n^{bkg}	ε (%)	$\mathcal{L}$ (pb $^{-1}$)	σ (pb)
4.825	5	1	9.7	370.7	$0.93^{+0.66}_{-0.56}$	5.775	3	5	14.5	516.2	$0.00^{+0.11}_{-0.02}$
4.875	6	2	10.0	376.7	$0.89^{+0.71}_{-0.64}$	5.825	5	5	14.8	526.1	$0.00^{+0.37}_{-0.07}$
4.925	11	6	10.3	383.7	$1.06^{+0.98}_{-0.94}$	5.875	7	8	15.0	536.0	$0.00^{+0.33}_{-0.07}$
4.975	15	3	10.6	389.7	$2.44^{+1.01}_{-0.88}$	5.925	6	6	15.2	546.1	$0.10^{+0.28}_{-0.10}$
5.025	7	4	10.8	396.7	$0.59^{+0.72}_{-0.59}$	5.975	3	4	15.4	556.2	$0.00^{+0.18}_{-0.04}$
5.075	12	4	11.1	403.8	$1.69^{+0.67}_{-0.97}$						

The combined results from Belle [9,40] and Belle II measurements are presented in Tables V and VI.

VII. SUMMARY

In summary, the cross sections for the processes $e^+e^- \rightarrow h^+h^-J/\psi$ at c.m. energies ranging from 3.8 GeV or the production threshold up to 5.5/6.0/7.0 GeV for $h = \pi/K/p$ are measured using a 427.9 fb $^{-1}$ data sample collected by Belle II. The total cross sections and their uncertainties are calculated to compare the results from different experiments. The measured cross sections of $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ and $e^+e^- \rightarrow K^+K^-J/\psi$ agree with previous experimental results within 1σ and 2σ uncertainties, respectively. The combined cross sections from Belle and Belle II differ from the BESIII results [31,32] by less than 1σ . The measurement precision is comparable to that achieved by BABAR [33] and Belle using ISR. However, the measurement is less precise than the BESIII results obtained from dedicated “XYZ” energy scans, which have a total integrated luminosity of about 500 pb $^{-1}$ at each energy point with energy steps of approximately 20 MeV, yielding precisions of about 5% and 10% for the $\pi^+\pi^-J/\psi$ and K^+K^-J/ψ processes, respectively. The corresponding effective ISR luminosity at Belle II over the same energy range and step size is only 30 to 50 pb $^{-1}$.

In the $\pi^+\pi^-J/\psi$ invariant mass distribution, an enhancement around 4.26 GeV is seen, indicative of the $Y(4230/4320)$ state. A global coupled-channel analysis [34] suggests a possible $\psi(4040)$ -like enhancement in the $M(\pi^+\pi^-J/\psi)$ distribution, and we find a small excess near 4.1 GeV with a statistical significance of 2.0σ . For the K^+K^-J/ψ invariant mass distribution, no significant structure is found, although the statistical power of the data is poor. For the first time, the process $e^+e^- \rightarrow p\bar{p}J/\psi$ is investigated, but the yield is not significant and no clear structure is observed in the $p\bar{p}J/\psi$ cross section. Upper limits on the cross sections for $e^+e^- \rightarrow p\bar{p}J/\psi$ from the production threshold up to 7.0 GeV are established. Our result near 6 GeV (< 0.16 pb) is consistent with the theoretical prediction at $\mathcal{O}(4 \text{ fb})$ [41], and is expected to provide valuable input for future theoretical studies. A clear

signal with a significance of 5.3σ for the $Z_c(3900)^\pm$ is observed in the $\pi^\pm J/\psi$ system; however, no structure is found in the $K^\pm J/\psi$ system. These results are consistent with previous measurements performed by Belle and BESIII [6,9,36,37]. A larger Belle II data sample will be crucial for further investigations of the structures in the $h^\pm J/\psi$ and h^+h^-J/ψ systems, which may help clarify the nature of these exotic states.

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DATA AVAILABILITY

The data are not publicly available. The data are available from the authors upon reasonable request.

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- [1] M. Gell-Mann, *Phys. Lett.* **8**, 214 (1964).
 [2] H. Fritzsch, M. Gell-Mann, and H. Leutwyler, *Phys. Lett.* **47B**, 365 (1973).

- [3] N. Brambilla, S. Eidelman, C. Hanhart, A. Nefediev, C. P. Shen, C. E. Thomas, A. Vairo, and C. Z. Yuan, *Phys. Rep.* **873**, 1 (2020).

- [4] H. X. Chen, W. Chen, X. Liu, Y. R. Liu, and S. L. Zhu, *Rep. Prog. Phys.* **86**, 026201 (2023).
- [5] B. Aubert *et al.* (BABAR Collaboration), *Phys. Rev. Lett.* **95**, 142001 (2005).
- [6] C. Z. Yuan *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **99**, 182004 (2007).
- [7] X. L. Wang *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **99**, 142002 (2007).
- [8] G. Pakhlova *et al.* (Belle Collaboration), *Phys. Rev. D* **83**, 011101 (2011).
- [9] Z. Q. Liu *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **110**, 252002 (2013).
- [10] X. L. Wang *et al.* (Belle Collaboration), *Phys. Rev. D* **91**, 112007 (2015).
- [11] S. Jia *et al.* (Belle Collaboration), *Phys. Rev. D* **100**, 111103 (2019).
- [12] S. Jia *et al.* (Belle Collaboration), *Phys. Rev. D* **101**, 091101 (2020).
- [13] S. K. Choi *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **100**, 142001 (2008).
- [14] R. Mizuk *et al.* (Belle Collaboration), *Phys. Rev. D* **80**, 031104 (2009).
- [15] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **110**, 252001 (2013).
- [16] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **96**, 032004 (2017).
- [17] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **126**, 102001 (2021).
- [18] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **115**, 072001 (2015).
- [19] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **122**, 222001 (2019).
- [20] R. Aaij *et al.* (LHCb Collaboration), *Sci. Bull.* **66**, 1278 (2021).
- [21] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **128**, 062001 (2022).
- [22] R. Aaij *et al.* (LHCb Collaboration), *Phys. Rev. Lett.* **131**, 031901 (2023).
- [23] A. Esposito, A. Pilloni, and A. D. Polosa, *Phys. Rep.* **668**, 1 (2017).
- [24] F. K. Guo, C. Hanhart, U. G. Meißner, Q. Wang, Q. Zhao, and B. S. Zou, *Rev. Mod. Phys.* **90**, 015004 (2018) **94**, 029901(E) (2022).
- [25] H. X. Chen, W. Chen, X. Liu, Y. R. Liu, and S. L. Zhu, *Rep. Prog. Phys.* **86**, 026201 (2023).
- [26] S. Navas *et al.* (Particle Data Group), *Phys. Rev. D* **110**, 030001 (2024).
- [27] Q. Wang, C. Hanhart, and Q. Zhao, *Phys. Rev. Lett.* **111**, 132003 (2013).
- [28] J. J. Wu, R. Molina, E. Oset, and B. S. Zou, *Phys. Rev. Lett.* **105**, 232001 (2010).
- [29] J. J. Wu, R. Molina, E. Oset, and B. S. Zou, *Phys. Rev. C* **84**, 015202 (2011).
- [30] X. H. Liu, Q. Wang, and Q. Zhao, *Phys. Lett. B* **757**, 231 (2016).
- [31] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **118**, 092001 (2017).
- [32] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **106**, 072001 (2022).
- [33] J. P. Lees *et al.* (BABAR Collaboration), *Phys. Rev. D* **86**, 051102 (2012).
- [34] S. X. Nakamura, X. H. Li, H. P. Peng, Z. T. Sun, and X. R. Zhou, *Phys. Rev. D* **112**, 054027 (2025).
- [35] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **97**, 071101 (2018).
- [36] M. Ablikim *et al.* (BESIII Collaboration), *Chin. Phys. C* **46**, 111002 (2022).
- [37] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **131**, 211902 (2023).
- [38] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **107**, 092005 (2023).
- [39] C. Z. Yuan *et al.* (Belle Collaboration), *Phys. Rev. D* **77**, 011105 (2008).
- [40] C. P. Shen *et al.* (Belle Collaboration), *Phys. Rev. D* **89**, 072015 (2014).
- [41] X. Y. Zhang, Y. L. Song, and F. K. Guo, *Phys. Lett. B* **872**, 140007 (2026).
- [42] I. Adachi *et al.* (Belle II Collaboration), *Chin. Phys. C* **49**, 013001 (2025).
- [43] K. Akai, K. Furukawa, and H. Koiso (SuperKEKB Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **907**, 188 (2018).
- [44] T. Abe *et al.* (Belle II Collaboration), [arXiv:1011.0352](https://arxiv.org/abs/1011.0352).
- [45] K. Adamczyk *et al.* (Belle II SVD Collaboration), *J. Instrum.* **17**, P11042 (2022).
- [46] V. Bertacchi *et al.* (Belle II Tracking Group), *Comput. Phys. Commun.* **259**, 107610 (2021).
- [47] D. Kotchetkov *et al.*, *Nucl. Instrum. Methods Phys. Res., Sect. A* **941**, 162342 (2019).
- [48] G. Rodrigo, H. Czyż, J. H. Kühn, and M. Szopa, *Eur. Phys. J. C* **24**, 71 (2002).
- [49] F. Campanario, H. Czyż, J. Gluza, T. Jeliński, G. Rodrigo, S. Tracz, and D. Zhuridov, *Phys. Rev. D* **100**, 076004 (2019).
- [50] D. J. Lange, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [51] E. Barberio, B. van Eijk, and Z. Was, *Comput. Phys. Commun.* **66**, 115 (1991).
- [52] S. Agostinelli *et al.*, *Nucl. Instrum. Methods Phys. Res., Sect. A* **506**, 250 (2003).
- [53] T. Sjöstrand, S. Ask, J. R. Christiansen, R. Corke, N. Desai, P. Ilten, S. Mrenna, S. Prestel, C. O. Rasmussen, and P. Z. Skands, *Comput. Phys. Commun.* **191**, 159 (2015).
- [54] S. Jadach, B. F. L. Ward, and Z. Was, *Comput. Phys. Commun.* **130**, 260 (2000).
- [55] S. Jadach, J. H. Kuhn, and Z. Was, *Comput. Phys. Commun.* **64**, 275 (1990).
- [56] T. Kuhr *et al.* (Belle II Framework Software Group), *Comput. Software Big Sci.* **3**, 1 (2019); Repository: [10.5281/zenodo.5574115](https://zenodo.org/record/5574115).
- [57] I. Adachi *et al.* (Belle II Collaboration), *Eur. Phys. J. C* **85**, 1237 (2025).
- [58] K. Zhu, C. Z. Yuan, and R. G. Ping, *Phys. Rev. D* **78**, 036004 (2008).
- [59] R. H. Dalitz, *Phys. Rev.* **94**, 1046 (1954).
- [60] A. Bondar *et al.* (Belle Collaboration), *Phys. Rev. Lett.* **108**, 122001 (2012).
- [61] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. D* **112**, 092013 (2025).
- [62] S. S. Wilks, *Ann. Math. Stat.* **9**, 60 (1938).

- [63] E. Kou *et al.* (Belle II Collaboration), *Prog. Theor. Exp. Phys.* **2019**, 123C01 (2019).
- [64] M. Ablikim *et al.* (BESIII Collaboration), *J. High Energy Phys.* **10** (2021) 177.
- [65] I. Adachi *et al.* (Belle II Collaboration), *Phys. Rev. Lett.* **130**, 091902 (2023).
- [66] E. A. Kuraev and V. S. Fadin, *Yad. Fiz.* **41**, 733 (1985) [*Sov. J. Nucl. Phys.* **41**, 466 (1985)].
- [67] J. Z. Bai *et al.* (BES Collaboration), *Phys. Rev. D* **62**, 032002 (2000).
- [68] R. Brun and F. Rademakers, *Nucl. Instrum. Methods Phys. Res., Sect. A* **389**, 81 (1997).
- [69] W. A. Rolke, A. M. Lopez, and J. Conrad, *Nucl. Instrum. Methods Phys. Res., Sect. A* **551**, 493 (2005).
- [70] Belle II Collaboration, Systematic corrections framework, <https://syscorr-fw.readthedocs.io/en/latest/index.html>.